

X-ray diffraction

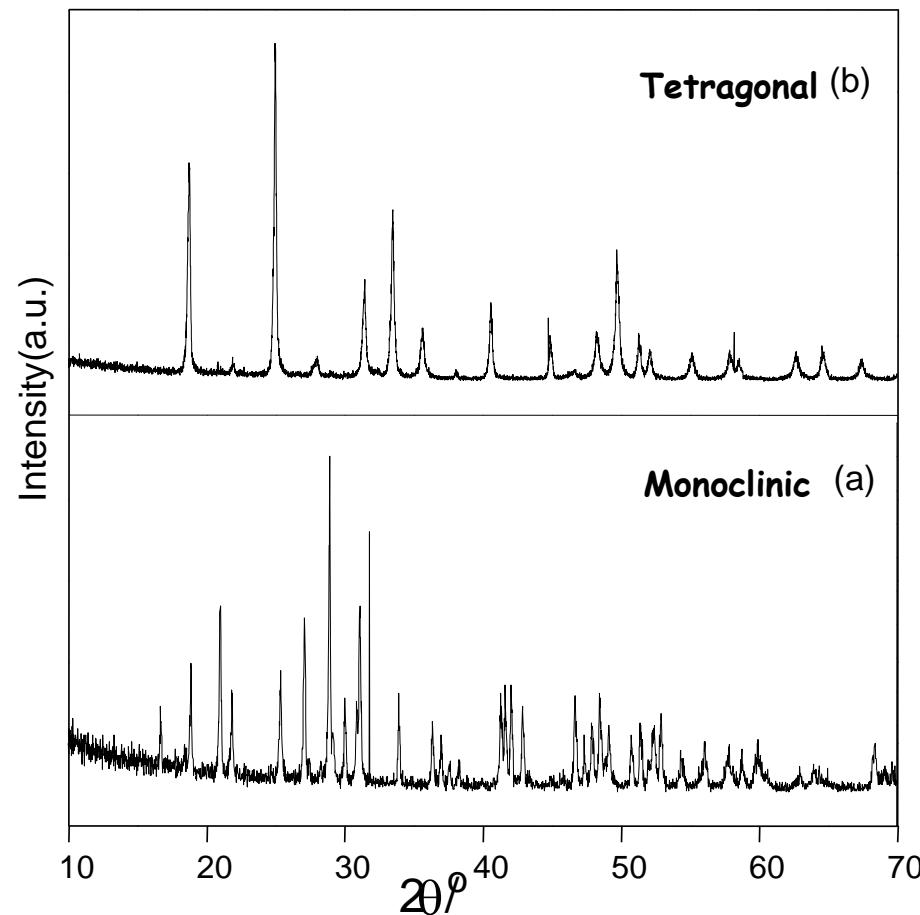
Examples

MISS T. U. URUNKAR

**DEPARTMENT OF PHYSICS
VIVEKANAND COLLEGE, KOLHAPUR**

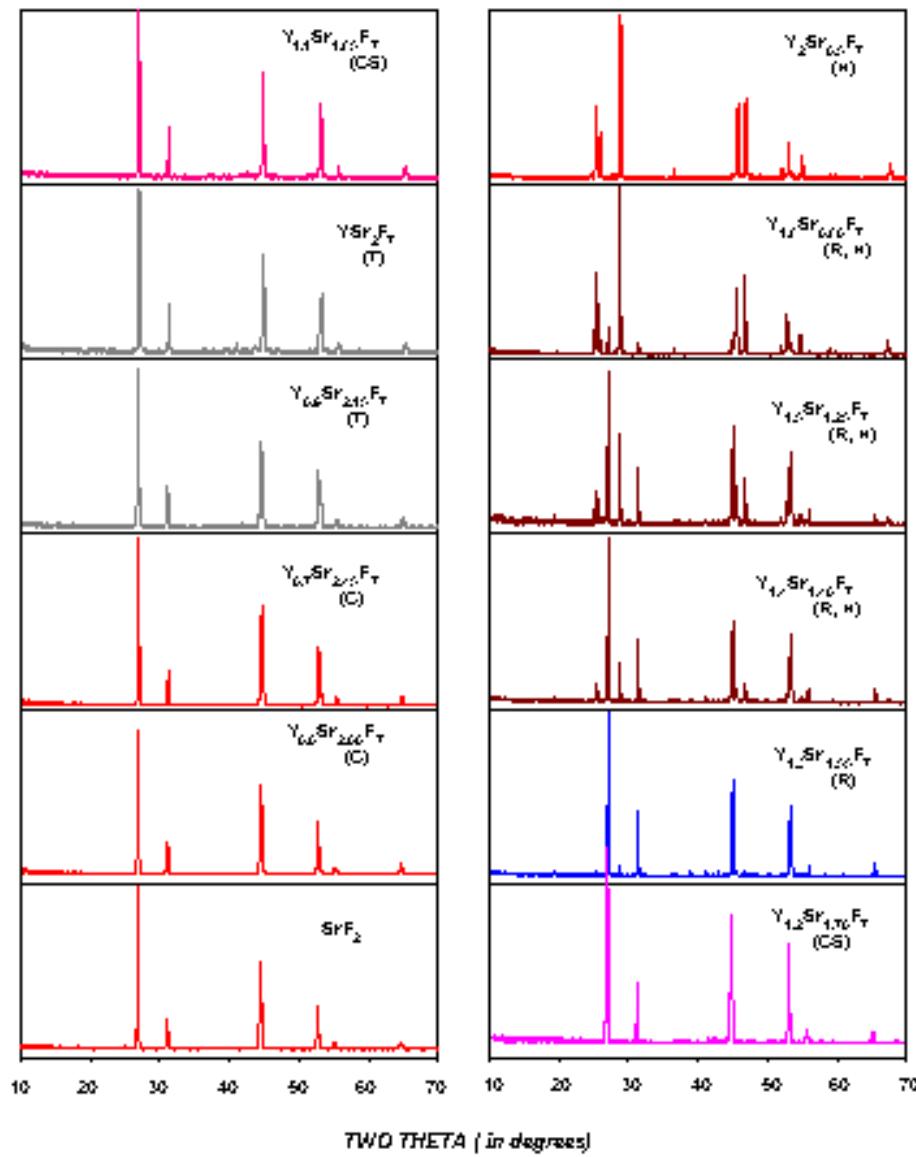
DATE:- 23/08/2018

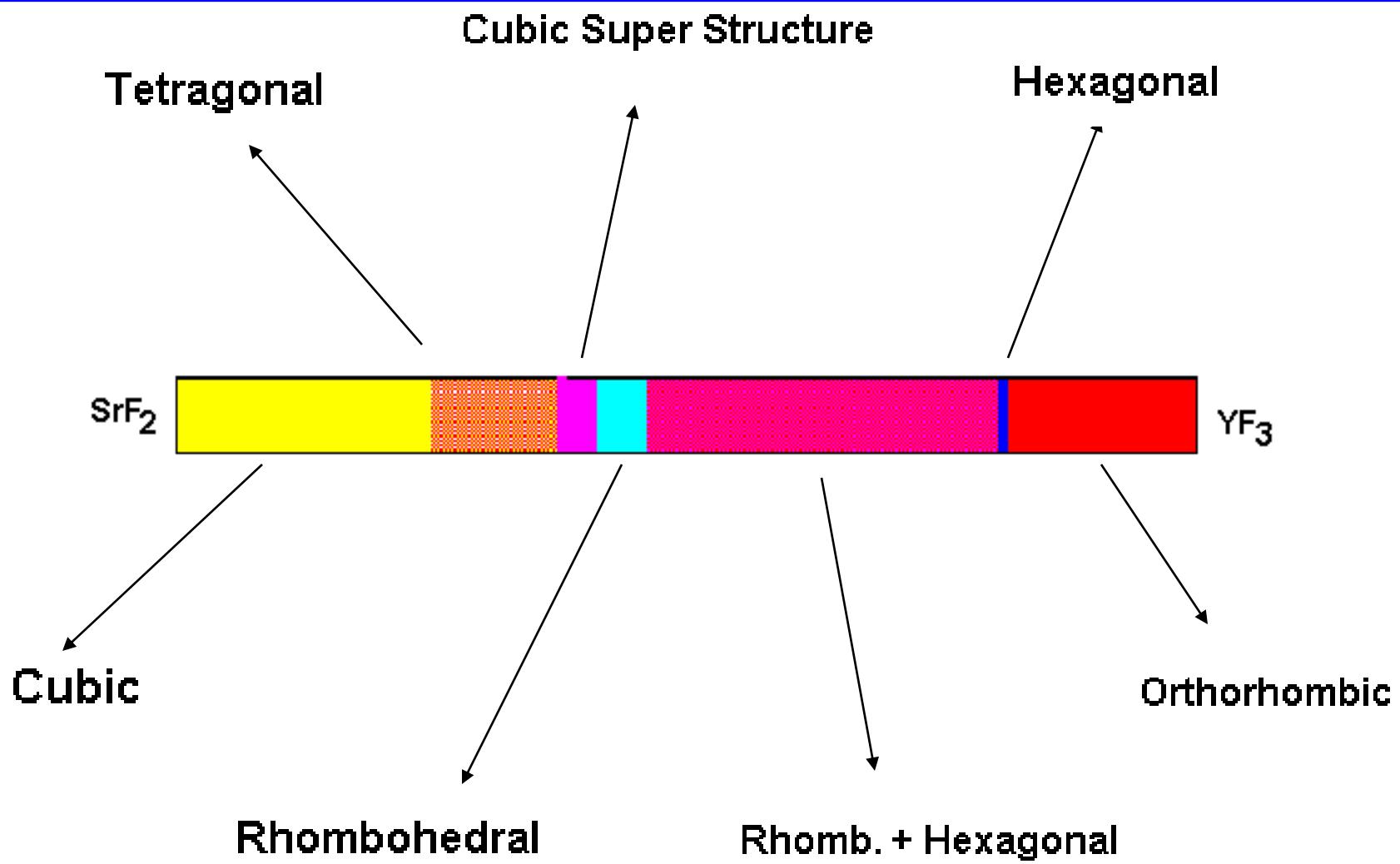
Effect of substitution on unit cell



SrF₂-YF₃ SYSTEM

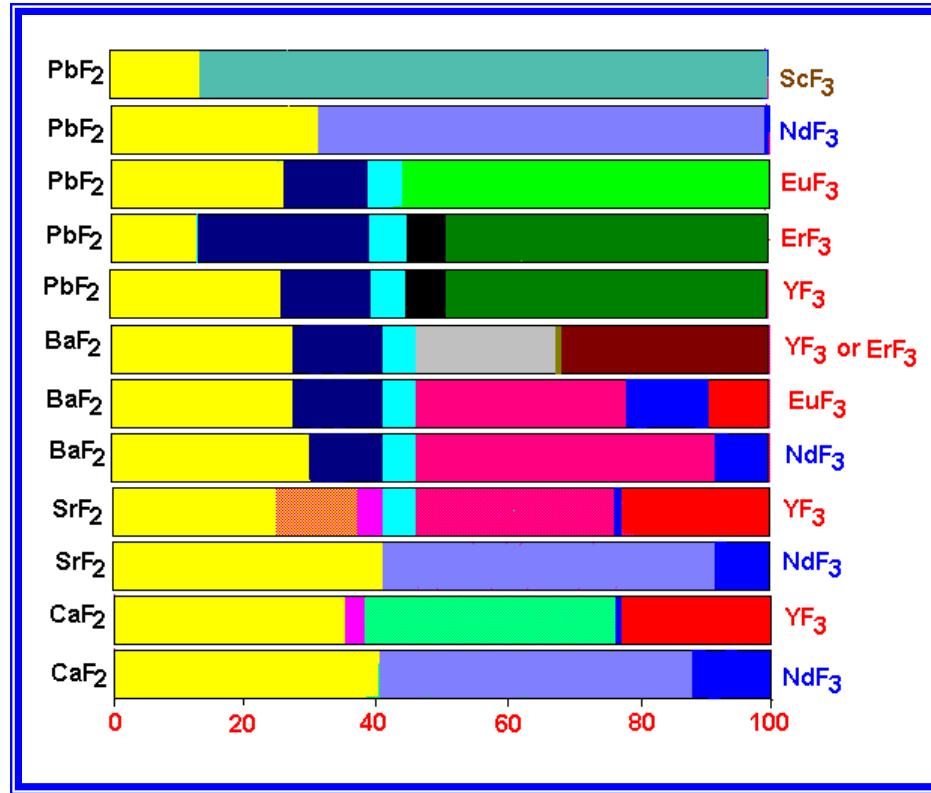
Intensity (a. u.)





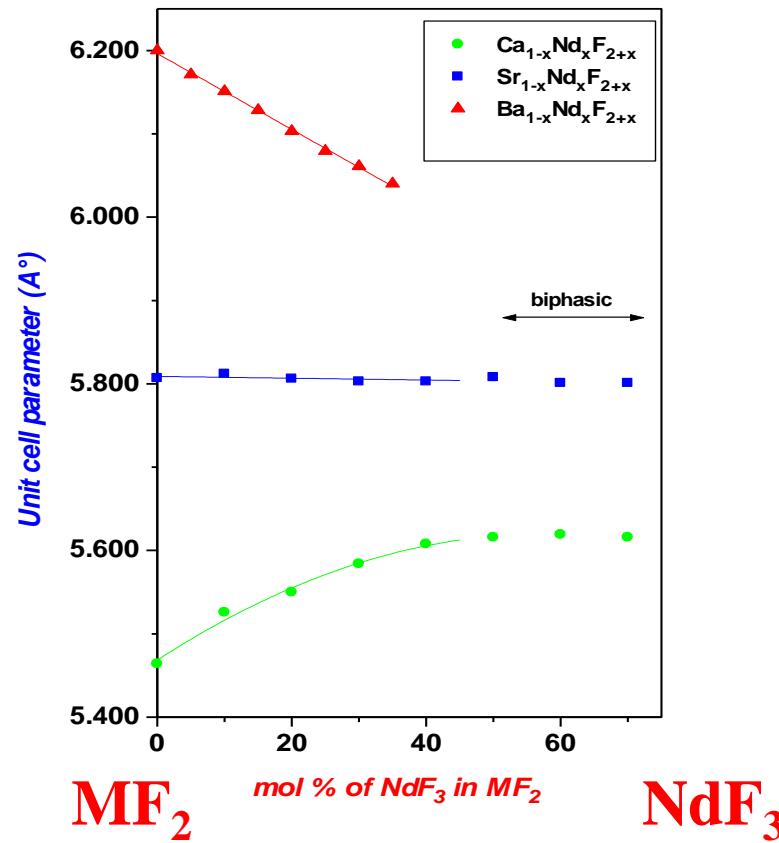
Phase fields present in SrF_2 - YF_3 system

MF₂-M'F₃ Phase Relation



- [Yellow] Fluorite type S.S. (Cubic - I)
- [Dark Blue] Tysonite or Tysonite type S.S. (Hexa.)
- [Light Blue] Rhombohedral
- [Light Green] C.S. + Tysonite
- [Orange] Tetragonal - I
- [Dark Blue] Cubic - I + Rhomb.
- [Olive Green] M₂BaF₈ (Mono.)
- [Grey] Rhomb. + M₂BaF₈
- [Green] Rhomb. + MF₃ (Ortho.)
- [Teal] Fluorite + ScF₃
- [Pink] Cubic - II (C.S.)
- [Red] Tysonite + MF₃ (Ortho.)
- [Magenta] Rhomb. + Tysonite
- [Maroon] M₂BaF₈ + MF₃ (Ortho.)
- [Black] Tetragonal - II

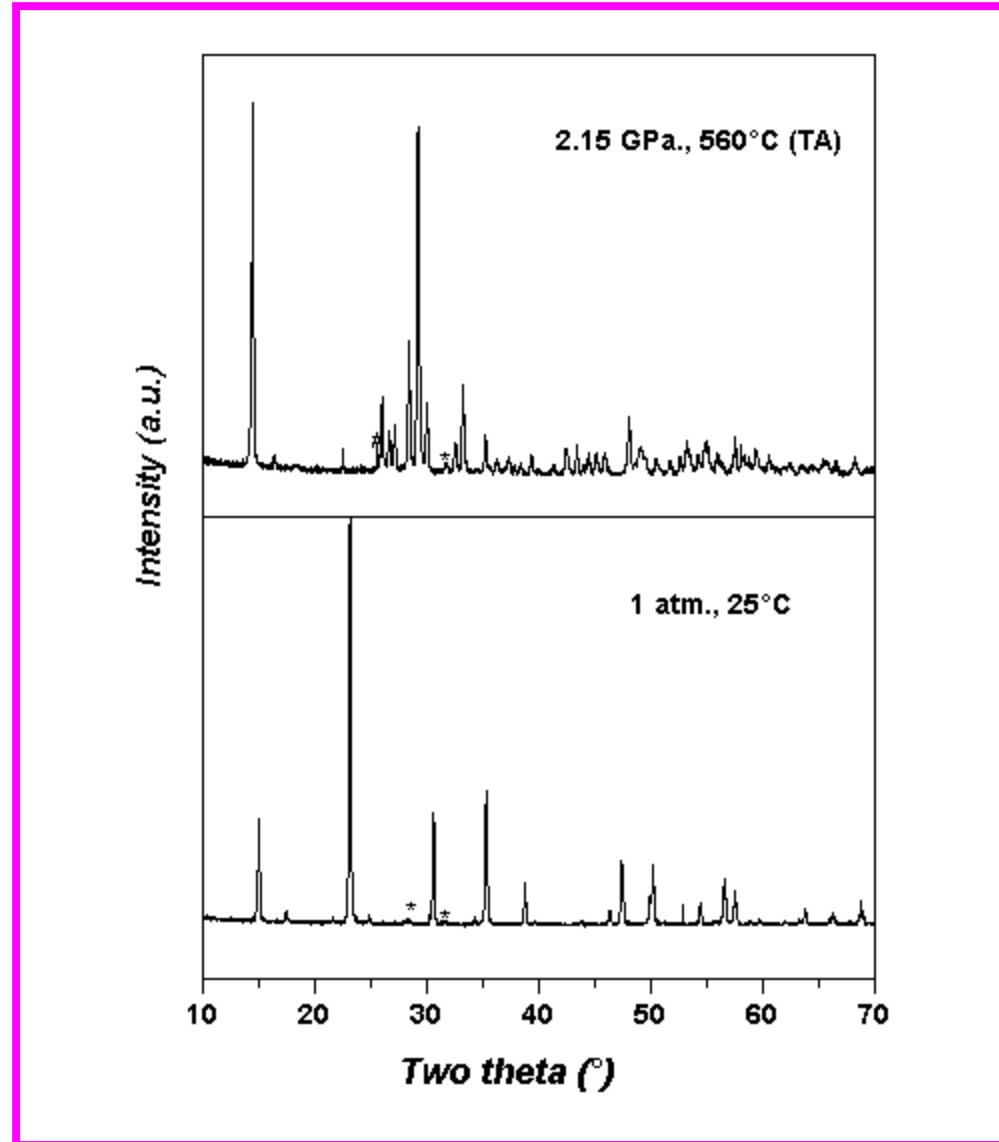
Solubility limit of a guest ion in a host lattice

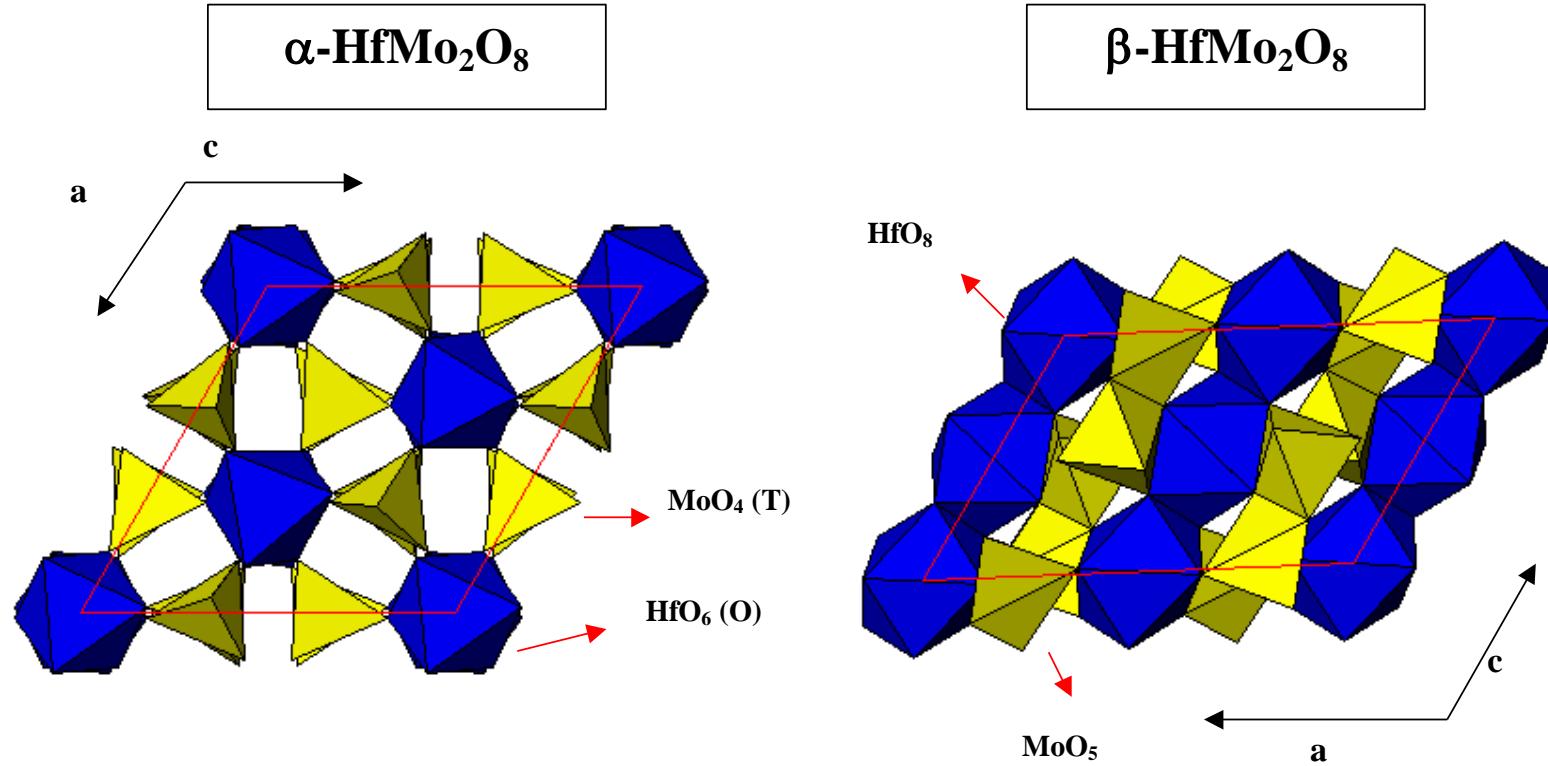


Powder
XRD
pattern of
 HfMo_2O_8

α (below)

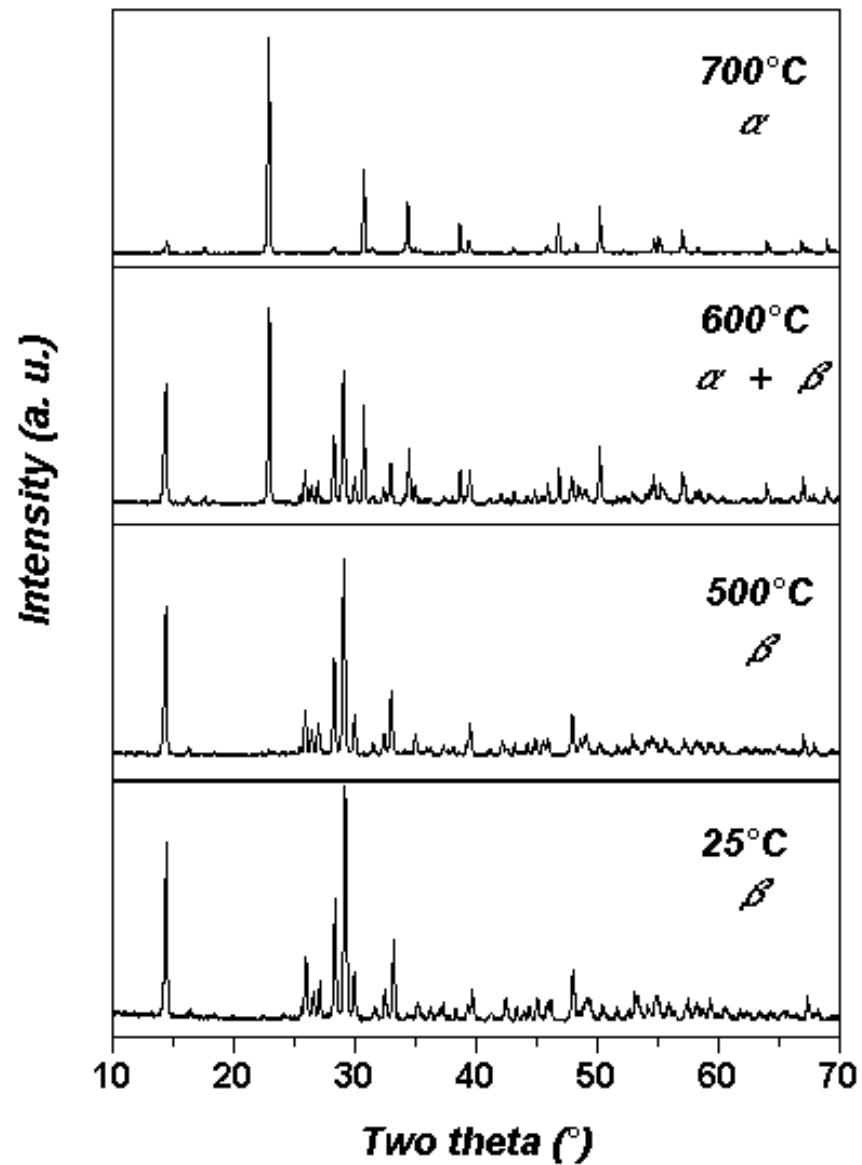
β (upper)





Sp. Gr. P-3 1 C
 $a = 10.1058(2)$ & $c = 11.7492(3)$ Å
 $V = 1039.15(4)$ Å³, $Z = 6$

Sp. Gr. C 2/c
 $a = 11.4138(6)$, $b = 7.9105(4)$, $c = 7.4395(3)$ Å
and $\beta = 122.35(0)^\circ$, $V = 567.45(5)$ Å³, $Z = 4$



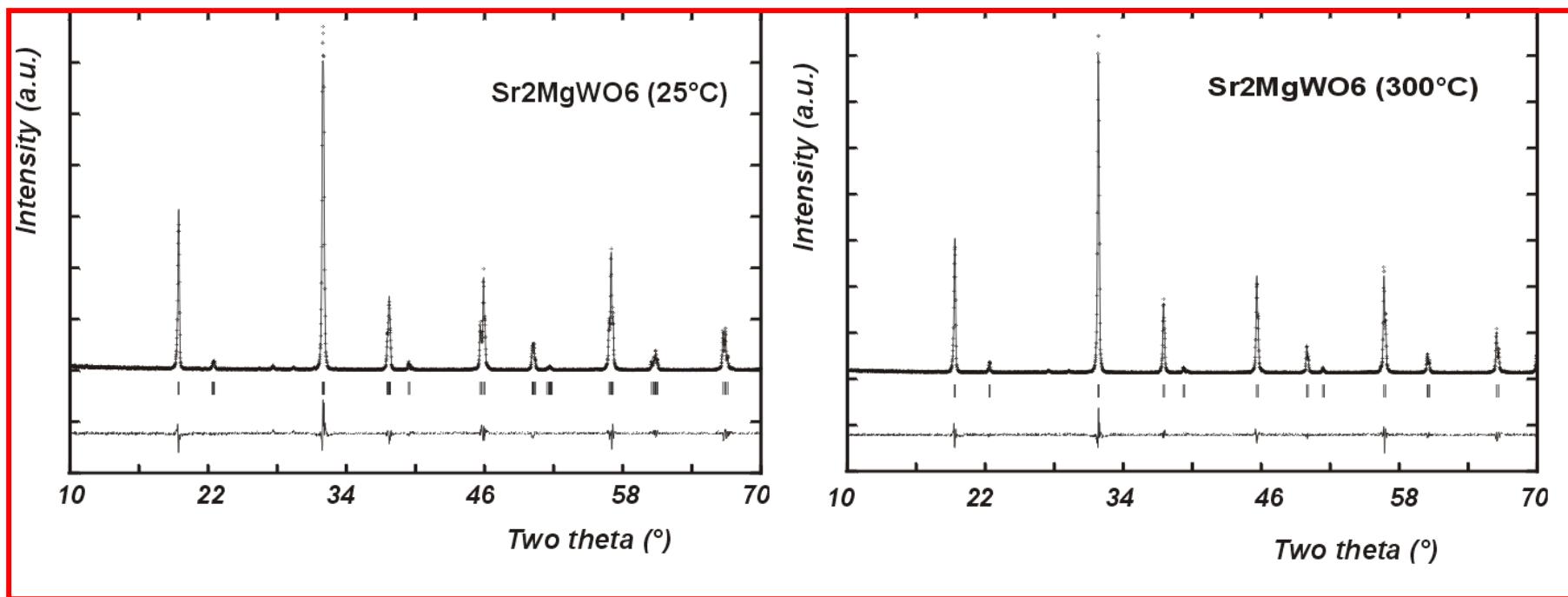
HT-XRD Studies on β -HfMo₂O₈

STUDIES IN ThO₂-UO₂ SYSTEM

Temp(K)	ThO ₂	ThO ₂ -2 % UO ₂	ThO ₂ -4 % UO ₂	ThO ₂ -6 % UO ₂
293	5.599	5.591	5.589	5.585
423	5.605	5.597	5.595	5.593
573	5.612	5.605	5.603	5.601
723	5.620	5.613	5.611	5.608
873	5.628	5.620	5.618	5.615
1023	5.636	5.628	5.626	5.624
1173	5.644	5.637	5.635	5.634
1323	5.654	5.646	5.644	5.642
1473	5.662	5.653	5.653	5.652
1623	5.671	5.664	5.664	5.662
$\alpha_a \times 10^6*$ (293-1623 K)	9.67	9.82	10.09	10.37

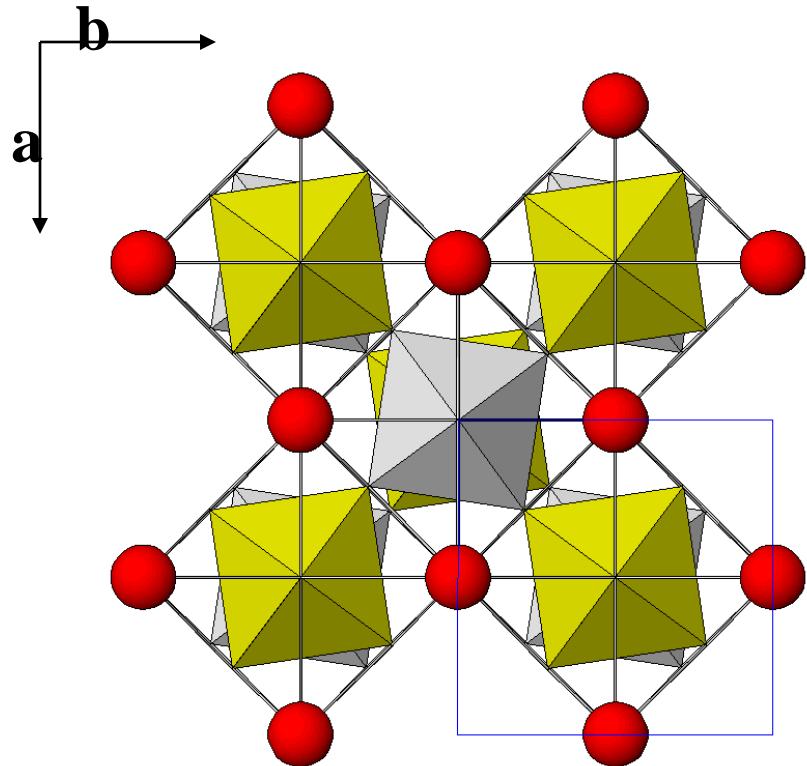
*Unit:K⁻¹

High temperature structural studies on Sr_2MgWO_6

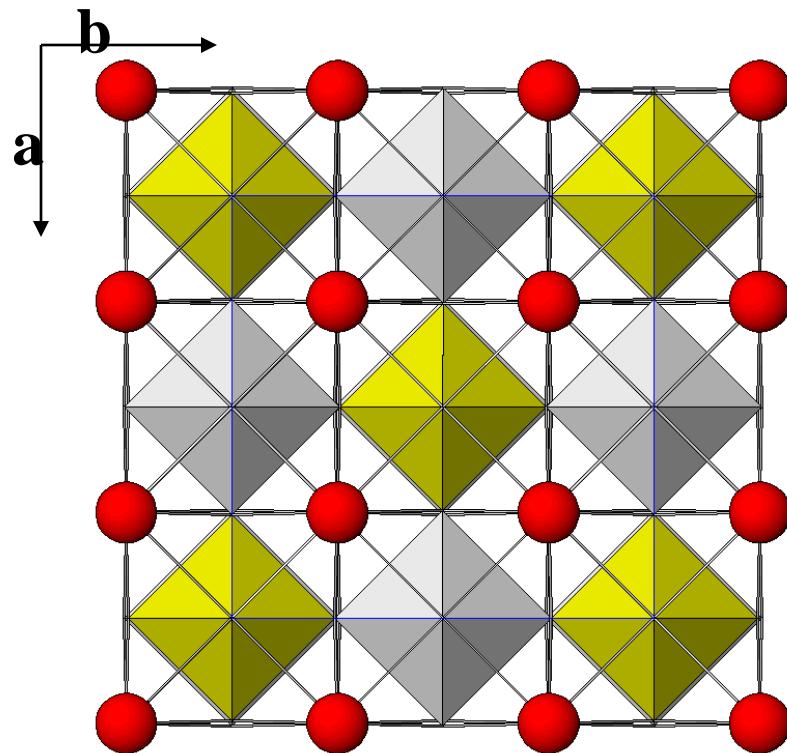


Sr_2MgWO_6			Ba_2MgWO_6		
Temp (°C)	$\alpha_a \times 10^6$ (/°C)	$\alpha_c \times 10^6$ (/°C)	$\alpha_v \times 10^6$ (/°C)	$\alpha_a \times 10^6$ (/°C)	$\alpha_v \times 10^6$ (/°C)
25-200	16.5	-0.58	32.5	10.7	32.2
25-300	-	-	48.1	11.1	33.2
300-1200	12.1	-	36.5	12.2	37.1
25-1200	-	-	39.6	12.0	36.4

Crystal structure of Sr_2MgWO_6

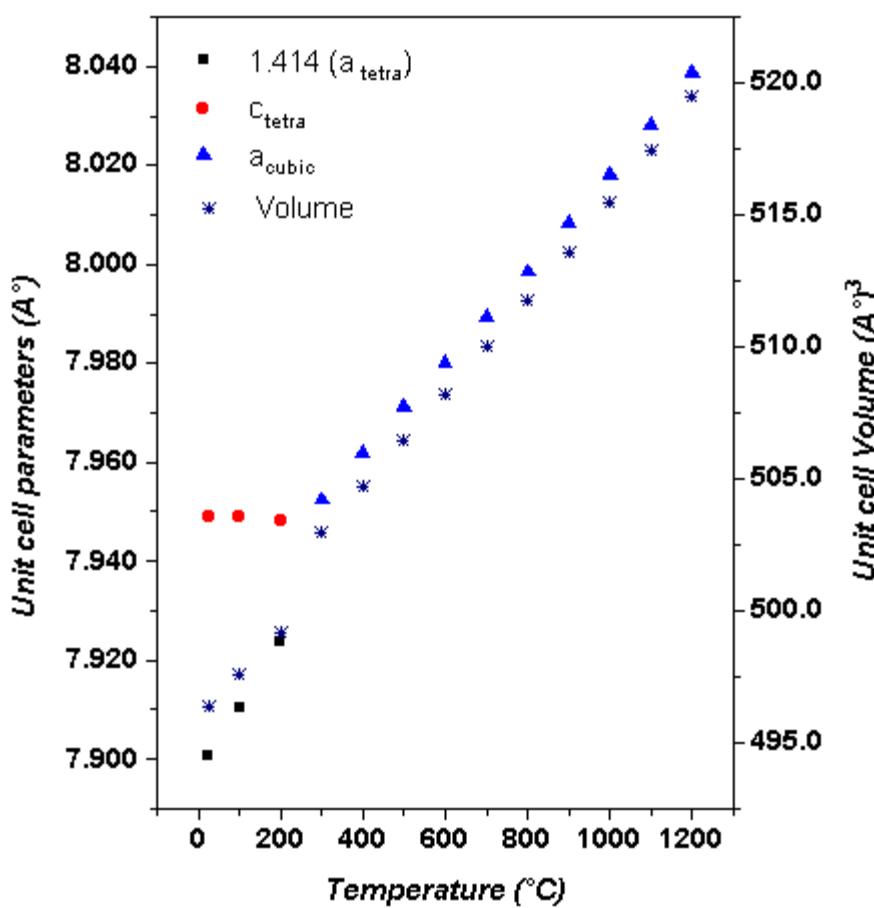


$T = 25^\circ\text{C}, P = 1 \text{ atm.}$
Tetragonal, Sp.Gr. = I4/m (No. 87),
 $a = 5.5876(1)$, $c = 9.9490(3) \text{ \AA}$
 $V = 248.18(1) \text{ \AA}^3$, $Z = 2$

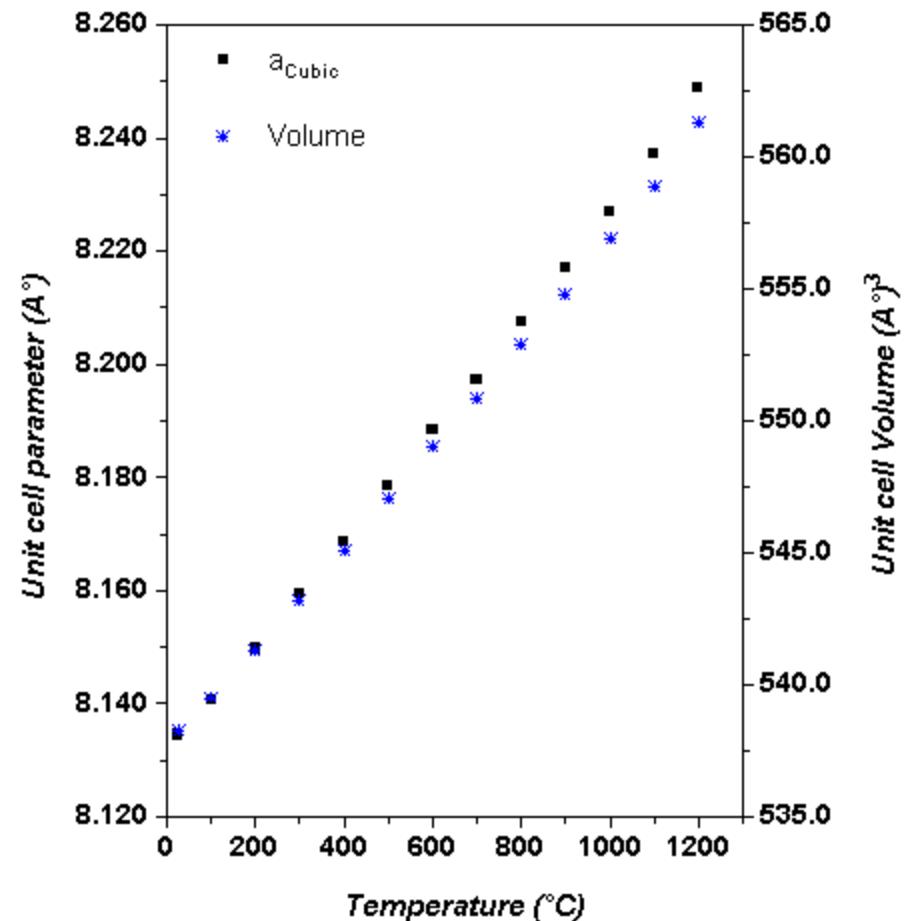


$T = 300^\circ\text{C}, P = 1 \text{ atm.}$
Cubic, Sp.Gr. = Fm3m (No. 225)
 $a = 5.5876(1) \text{ \AA}$
 $V = 248.18(1) \text{ \AA}^3$, $Z = 2$

Variation of unit cell parameters with Temperature



Sr_2MgWO_6



Ba_2MgWO_6

Crystal structure of Er_2BaF_8 (Monoclinic)



Atom	site	x	y	z	U_{iso} (\AA^2)	Occ.
Ba	$2a$	0	0	0	0.0302(11)	1.0
		0	0	0	0.0301(11)	
Er	$4h$	0	0.67630(8)	0.5	0.0258(8)	1.0
		0	0.67635(8)	0.5	0.0259(8)	
F1	$8j$	0.1904(6)	0.1399(3)	0.5645(9)	0.029(4)	1.0
		0.1906(6)	0.1399(3)	0.5644(9)	0.027(4)	
F2	$4i$	0.3859(8)	0	0.2201(12)	0.020(2)	1.0
		0.3859(8)	0	0.2200(12)	0.020(2)	
F3	$4g$	0	0.7452(5)	0	0.043(6)	1.0
	$8j$	0.0353(18)	0.7454(6)	0	0.021(3)	0.5

Sp. Gr. C2/m (No. 12)

$$a = 6.9620(2), b = 10.4860(3)$$

$$c = 4.2541(1) \text{ \AA} \text{ and } \beta = 99.6846(5)^\circ$$

$$V = 306.14(1) \text{ \AA}^3, Z = 2$$

$$\mathbf{R}_{\mathbf{B}} \quad \mathbf{R}_{\mathbf{F}}$$

Ord. 3.9 % 3.6 %

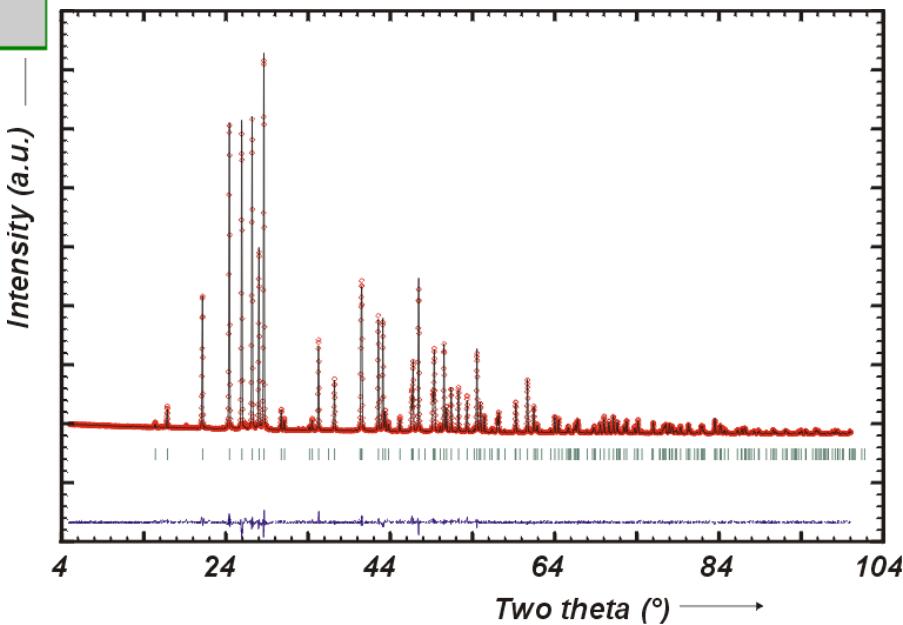
Disord. 4.0 % 3.6 %

(900°C/18 hrs)

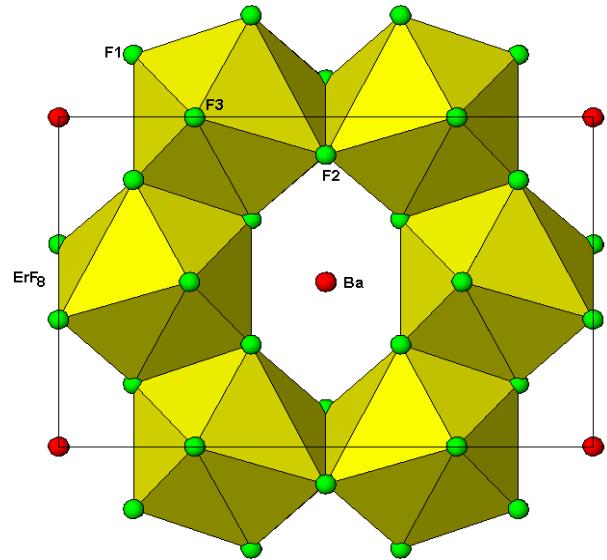
$\text{M}'_2\text{BaF}_8$ (0.68 mol % of M'F₃)

Orthorhombic: Pnma

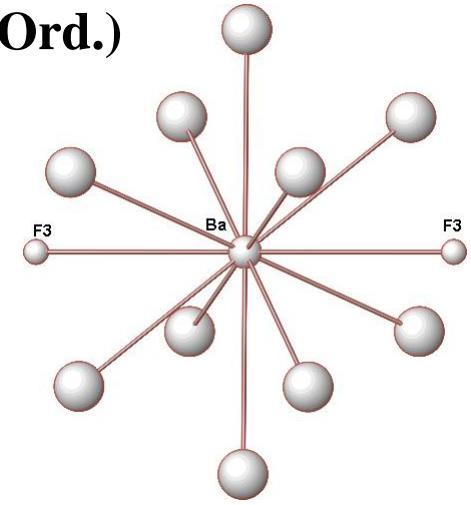
Monoclinic : C2/m



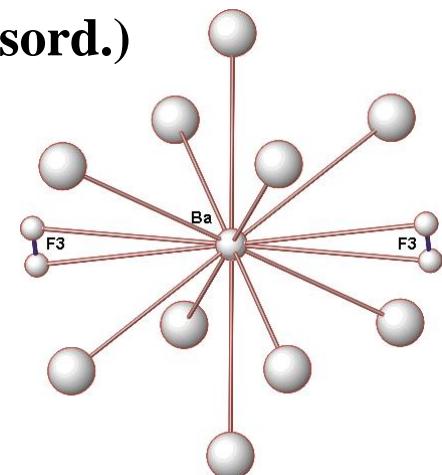
a
b



(Ord.)



(Disord.)

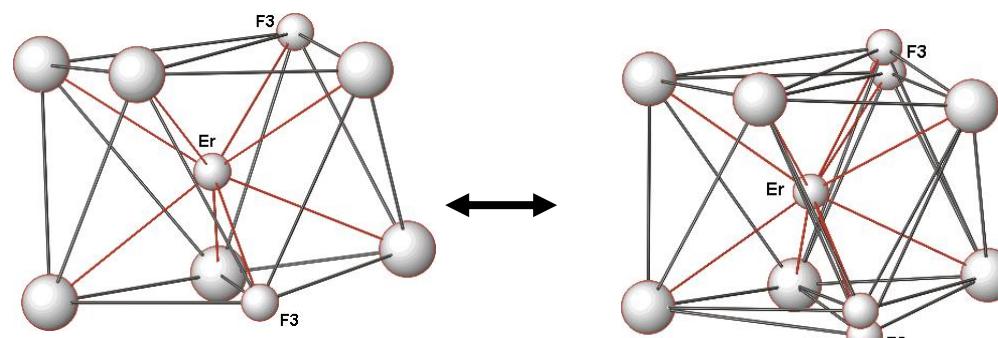


(Ord.)

ErF_8

(Disord.)

BaF_{12}

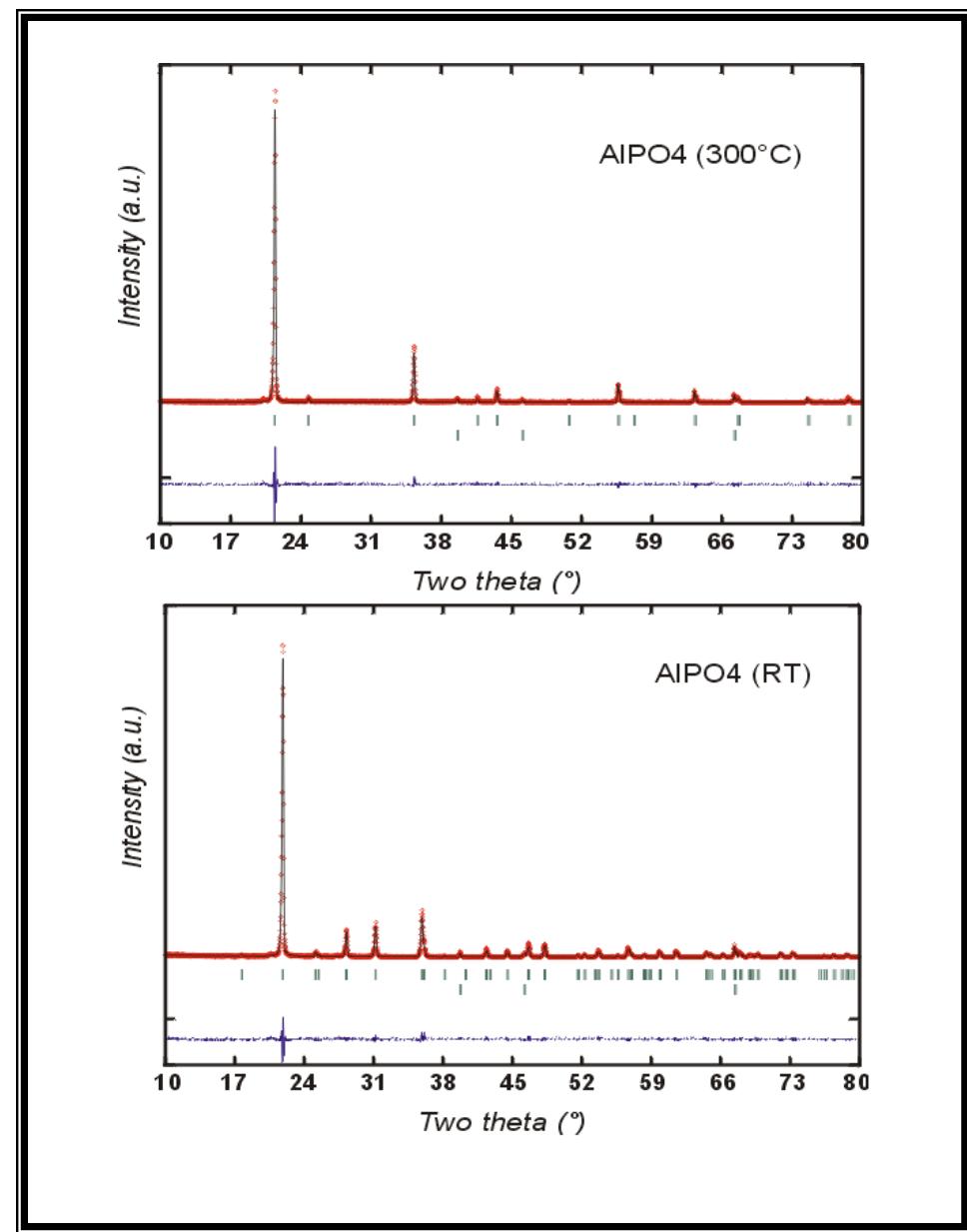


HT-XRD STUDIES ON $\text{Al}_{1-x}\text{Ga}_x\text{PO}_4$

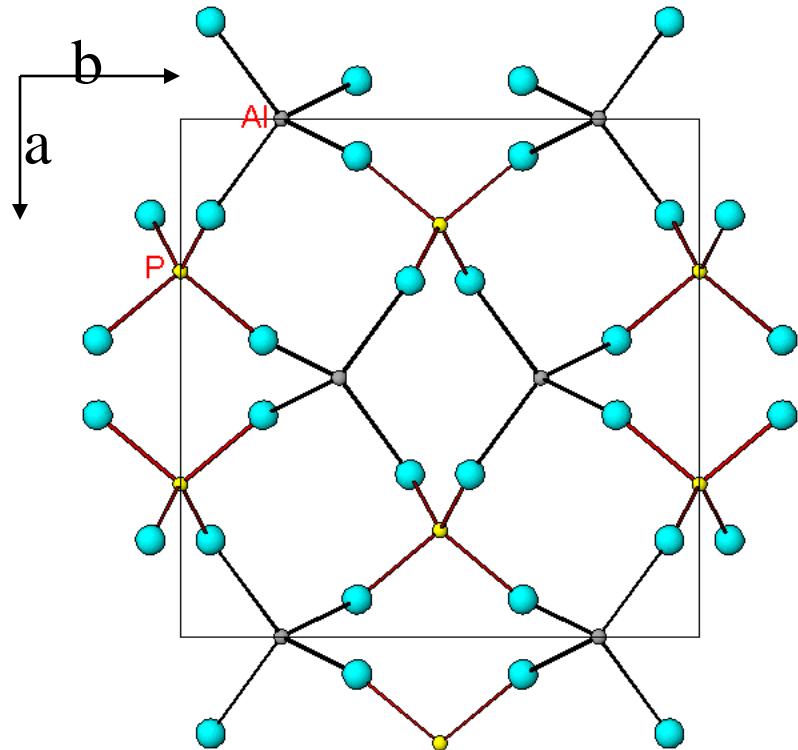
$\beta\text{-AlPO}_4$ (Cubic)

Powder XRD
pattern of
cristobalite type
 AlPO_4

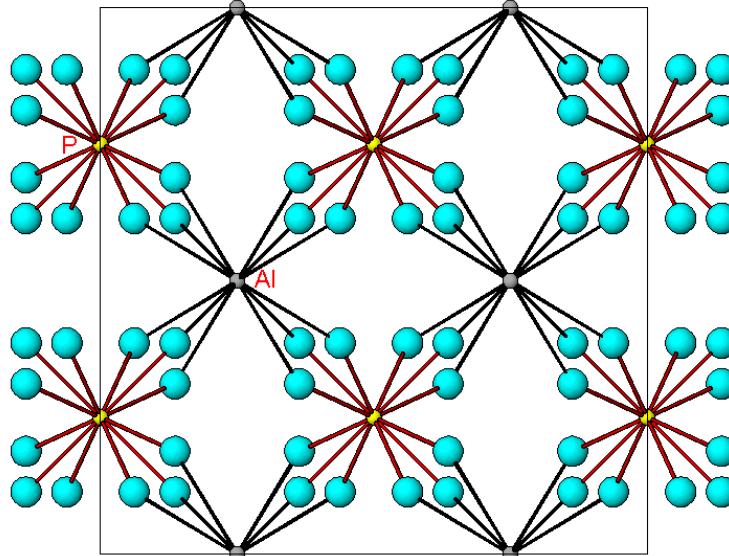
$\alpha\text{-AlPO}_4$ (Ortho.,)



Crystal structure of cristobalite type AlPO_4



$T = 25^\circ\text{C}, 1\text{Atm.}$



$T = 300^\circ\text{C}, 1\text{Atm.}$

Low Cristobalite type

S.Gr. $C222_1$

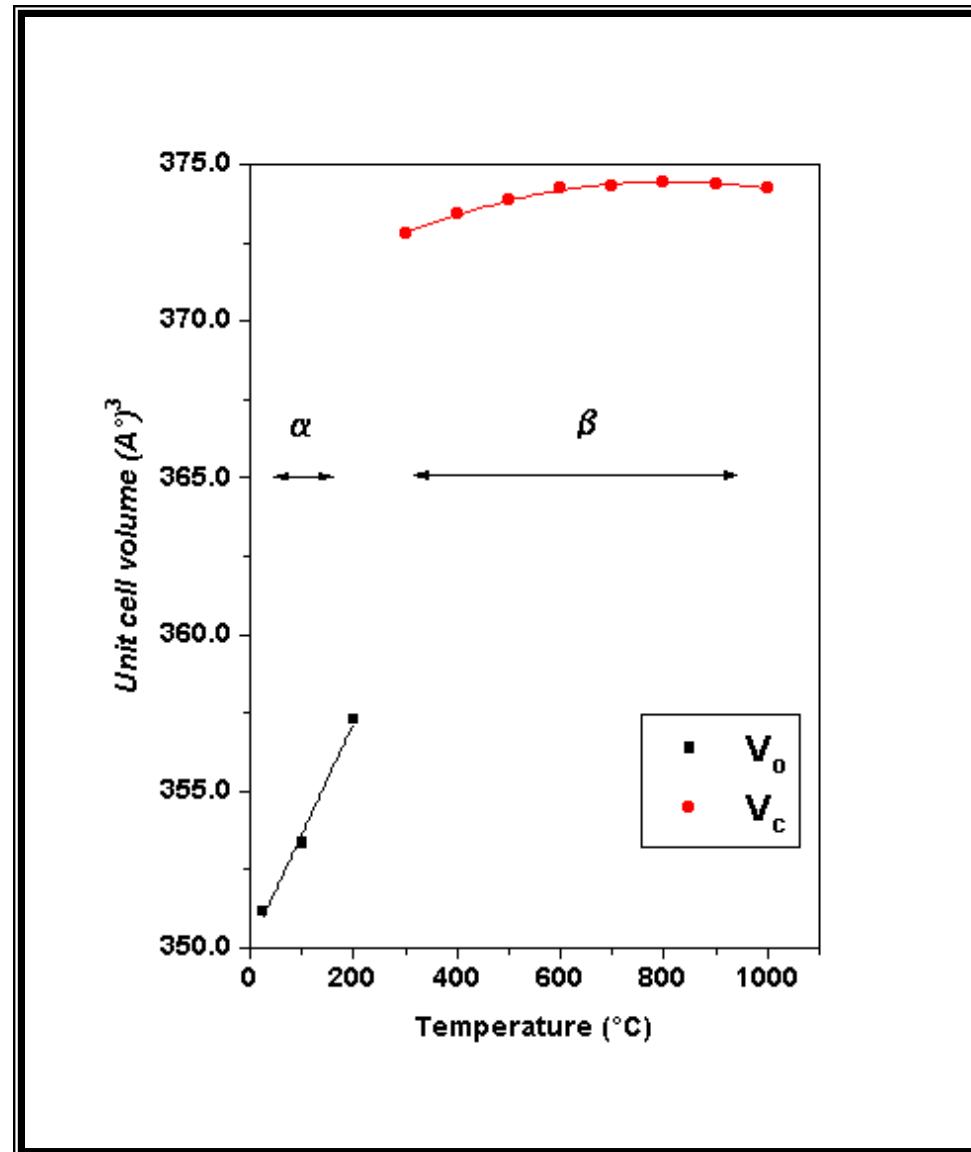
$7.0843(14), 7.0823(13), 6.9989(4)\text{\AA}$
 $V = 351.22(1) \text{\AA}^3, Z = 4$

High Cristobalite type

S.Gr. $F4-3m$

$a = 7.1969(2) \text{\AA}, V = 372.77(1) \text{\AA}^3$
 $Z = 4$

Variation of unit cell Volume of AlPO_4 with Temperature



HT-XRD STUDIES ON BPO₄ (Tetragonal, cristobalite type)

$$a = 4.3447(2) \text{ \AA}$$

$$c = 6.6415(5) \text{ \AA}$$

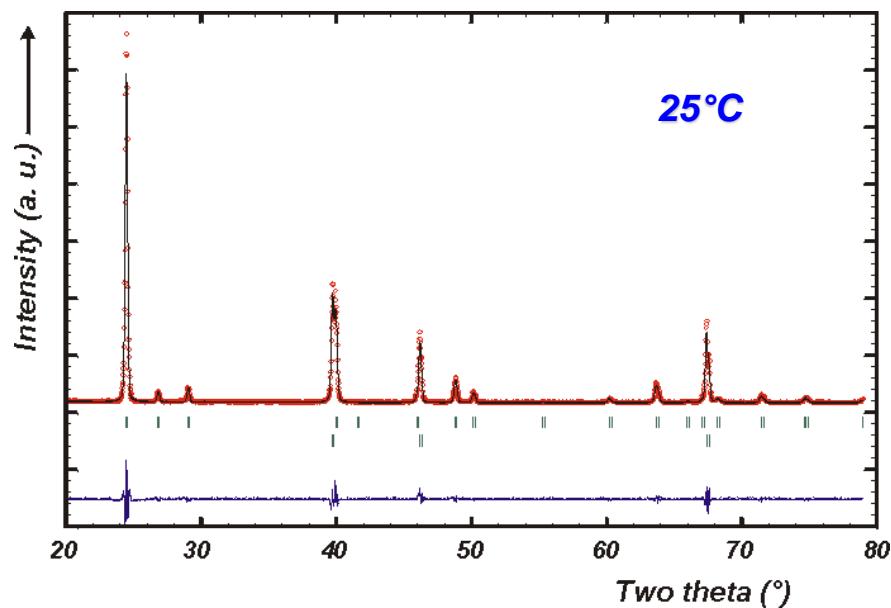
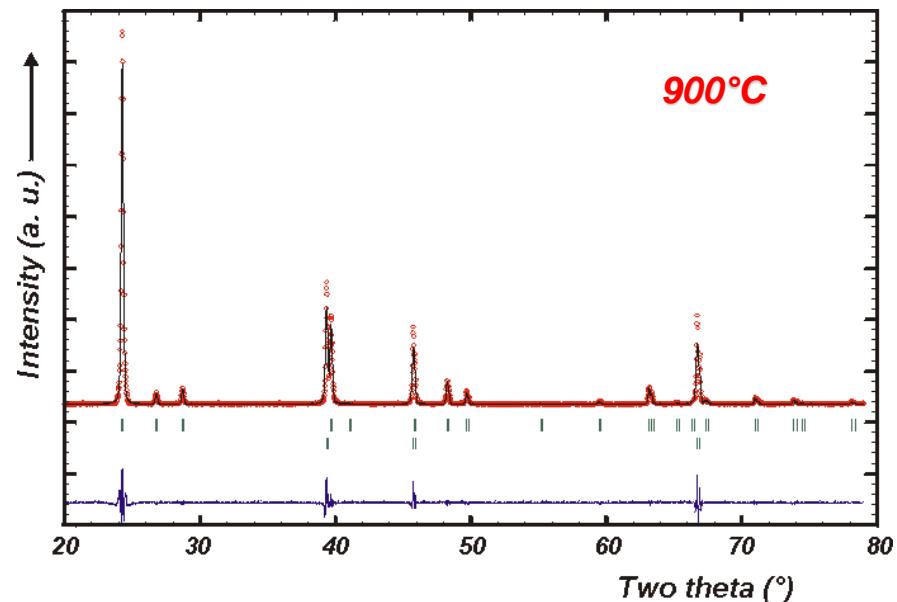
$$V = 125.37(1) \text{ \AA}^3$$

Rietveld refinement
plot of powder XRD

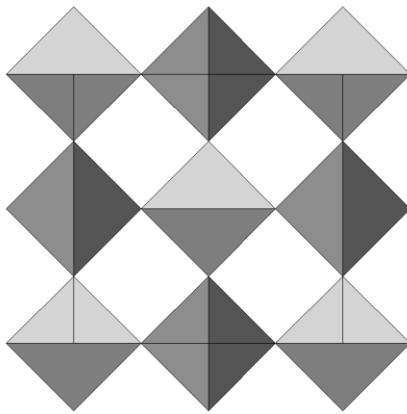
$$a = 4.3939(2) \text{ \AA}$$

$$c = 6.6539(6) \text{ \AA}$$

$$V = 128.46(1) \text{ \AA}^3$$

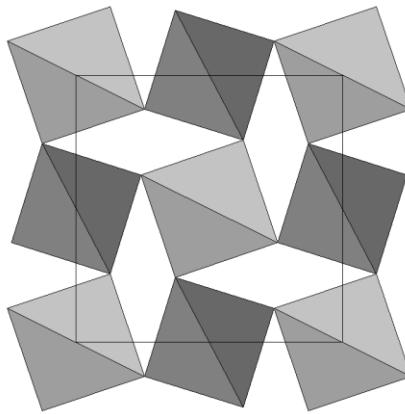


Ideal C9



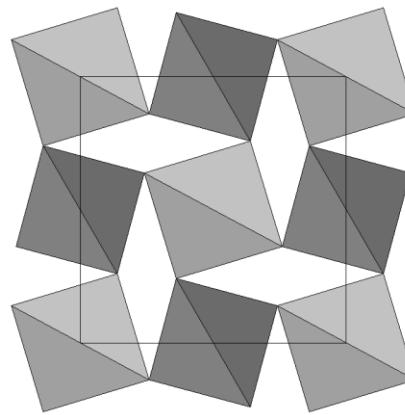
$$\phi = 0^\circ$$

BPO₄ (900°C)



T
↔
P

BPO₄ (25°C)

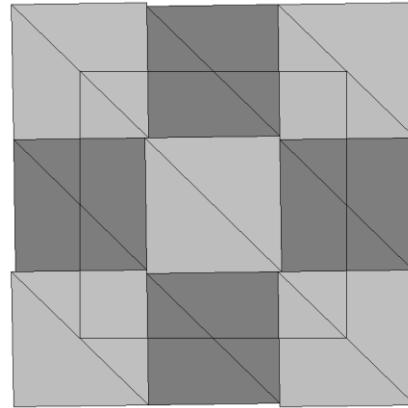


P

$$\phi = 27^\circ$$

$$\phi = 29^\circ$$

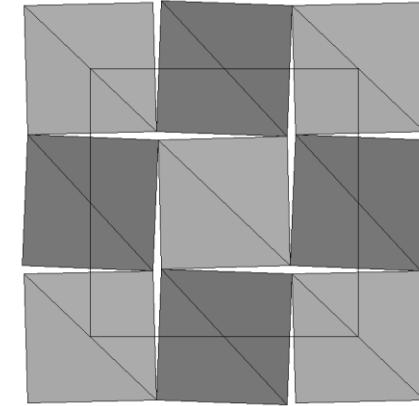
P
↔
T



$$\phi = 45^\circ$$

ZnCl₂

P
↔
T



BPO₄ (50 GPa)

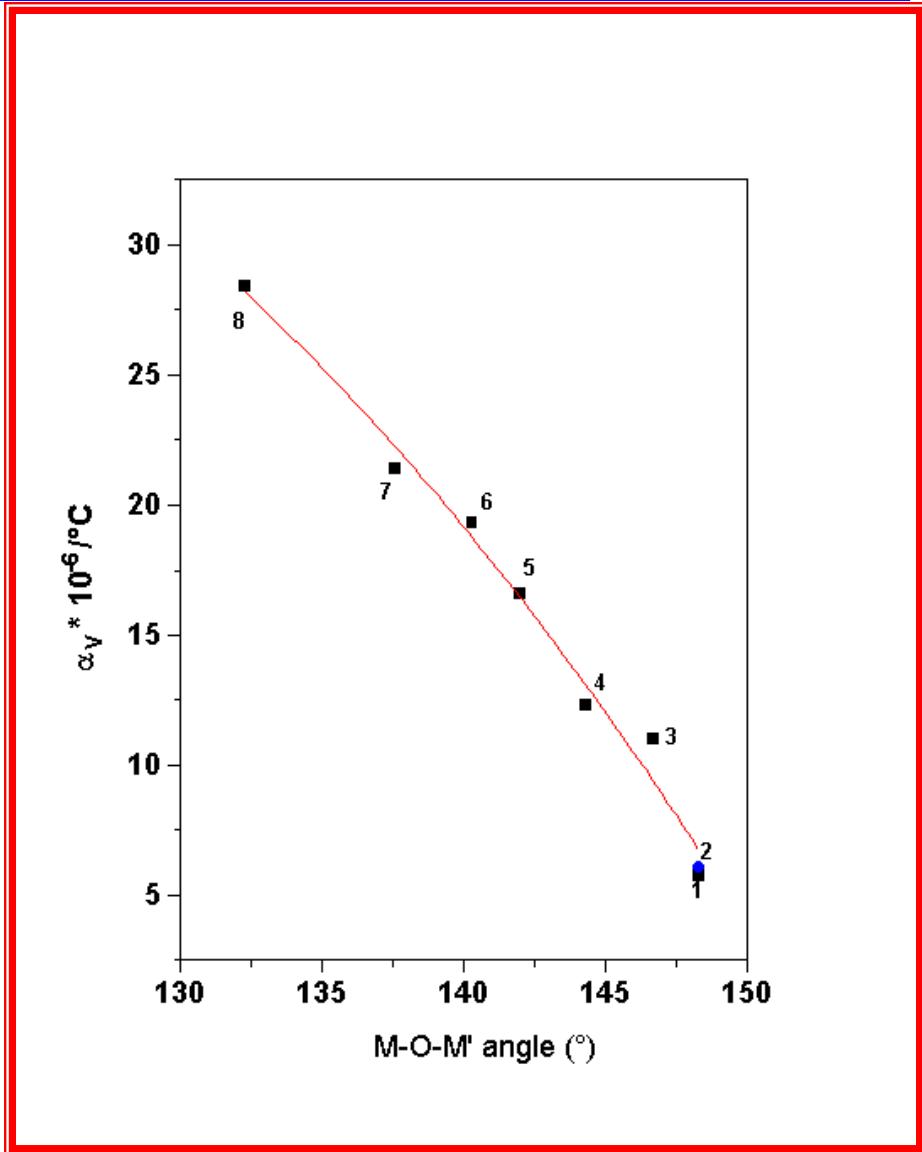
$$\phi = 43^\circ$$

Transformation topology for cristobalite frame with Temp. /Press.

Variation thermal expansion coefficients with inter-polyhedral angle of *Cristobalite* type compounds

$$\alpha_v (\text{}/^\circ\text{C}) = -191.32 + 4.33 \times [\theta] \\ - 0.02 \times [\theta]^2$$

1. AlPO₄ (at 300°C)
2. AlPO₄ (at 300°C) (*lit. data*)
3. SiO₂ (at 300°C) (*lit. data*)
4. Al_{0.8}Ga_{0.2}PO₄ (300°C)
5. Al_{0.5}Ga_{0.5}PO₄ (400°C)
6. Al_{0.2}Ga_{0.8}PO₄ (600°C)
7. GaPO₄ (700°C)
8. BPO₄ (25°C)



Crystal structure of α -VO(PO_3)₂

Space Group: C2/c (No. 15)

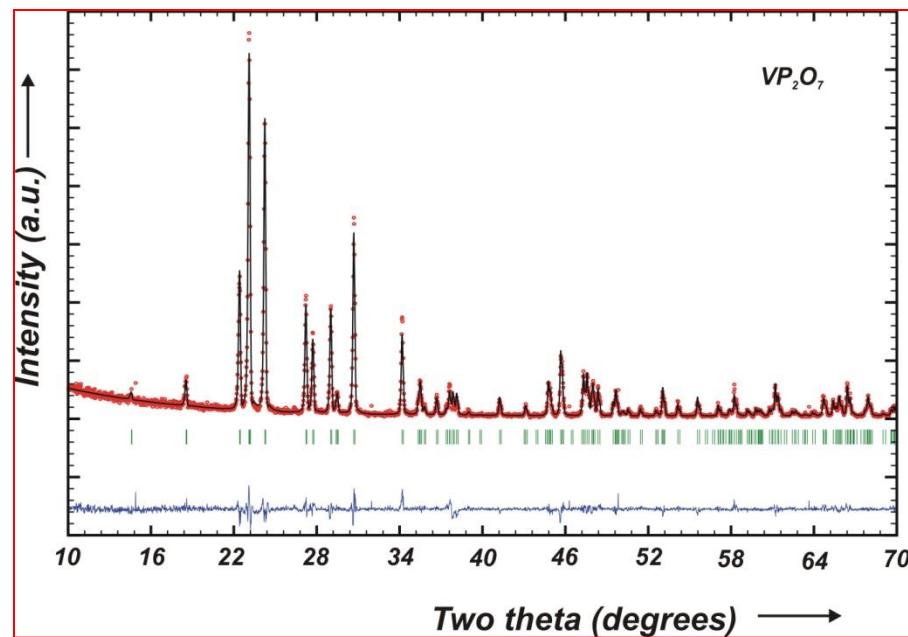
$$a = 15.0924(4)$$

$$b = 4.1919(1)$$

$$c = 9.5706(3) \text{ \AA}$$

$$\beta = 126.464(2)^\circ$$

$$V = 486.95(3) \text{ \AA}^3$$



Atom	site	x	y	z
V	4e	0	0.2551(4)	0.25
P	8f	0.3290(1)	0.0067(4)	0.8468(2)
O1	8f	0.4105(4)	0.159(1)	0.8307(8)
O2	8f	0.2376(4)	0.253(1)	0.8061(5)
O3	8f	0.3674(5)	-0.147(1)	0.0125(5)
O4	4e	0	-0.1342(4)	0.25

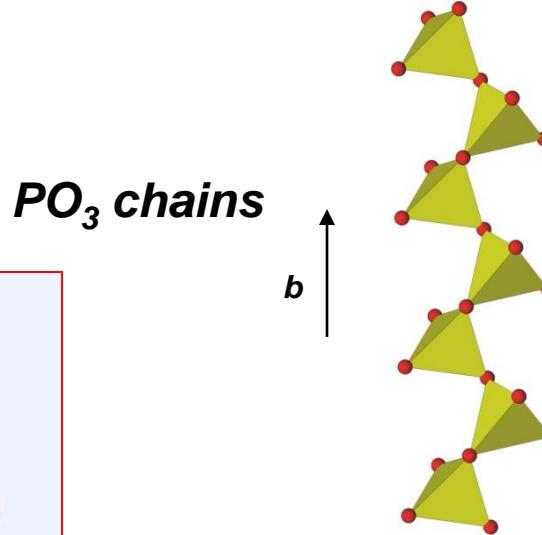
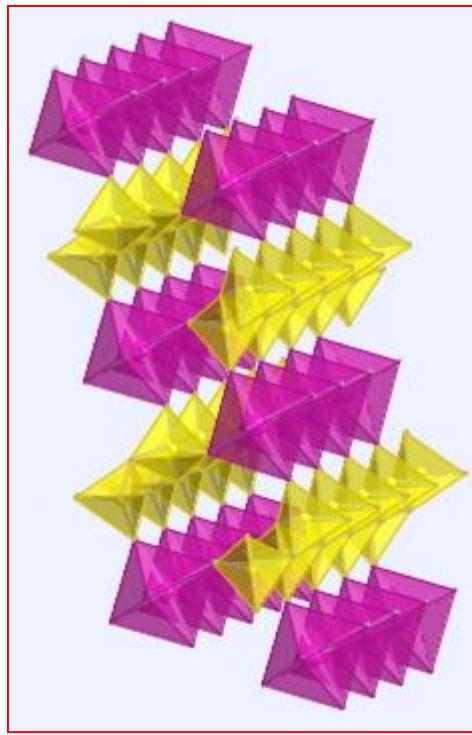
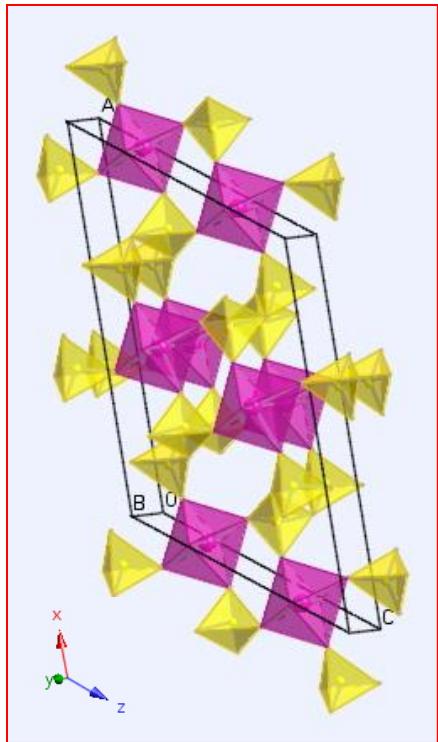
R_p : 10.8 %, R_{wp} : 14.9 %, R_{exp} : 11.5 %

χ^2 : 1.68

R_B : 6.04 %, R_F : 5.19 %

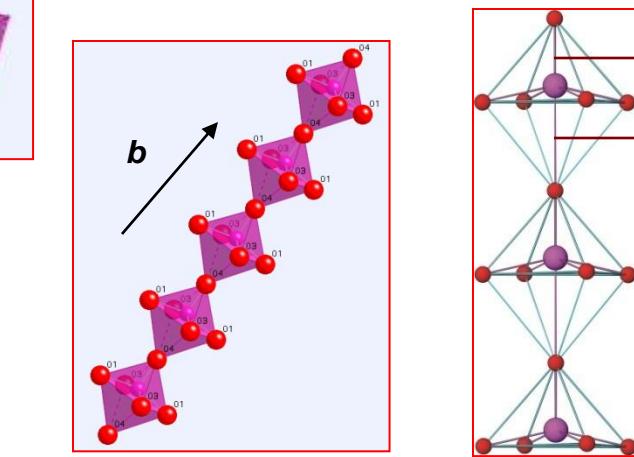
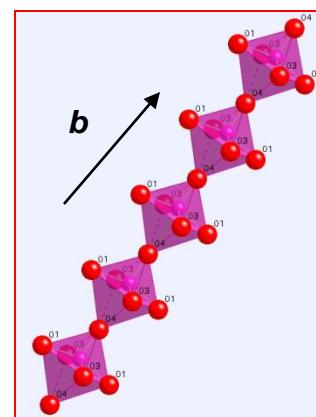
$$B_{\text{overall}} = 1.83(7) \text{ \AA}^2$$

Crystal structure of α -VO(PO₃)₂



**Structural
features of
VO(PO₃)₂**

VO₅ chains

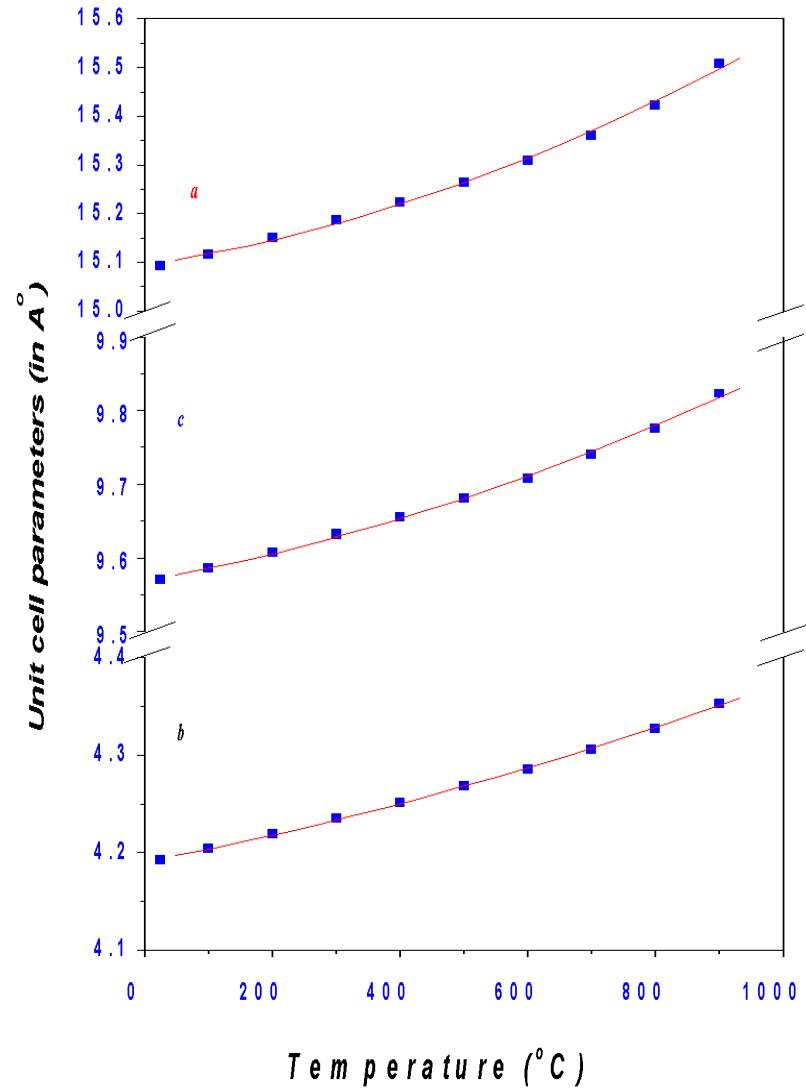


1.63 Å
2.56 Å

Variation of unit cell parameters with temperature

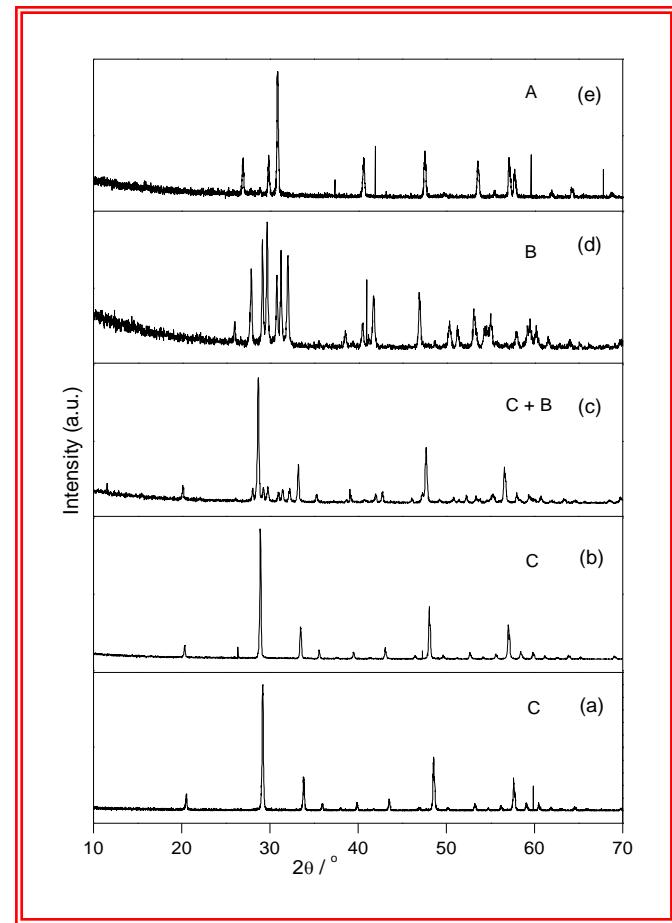
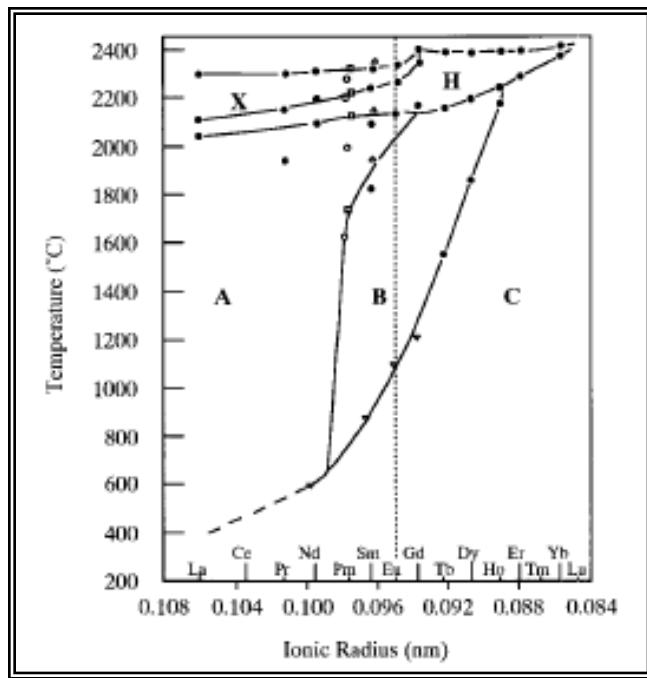
Coefficients of thermal expansion ($/^{\circ}\text{C}$)

$$\begin{aligned}\alpha_a &= 31.4 \times 10^{-6} \\ \alpha_b &= 43.8 \times 10^{-6} \\ \alpha_c &= 30.2 \times 10^{-6} \\ \alpha_V &= 87.5 \times 10^{-6}\end{aligned}$$



Crystal structure of stabilized monoclinic phase of $Nd_{2-x}Y_xO_3$

Most common crystal structure of Rare-earth sesquioxides are hexagonal monoclinic and cubic

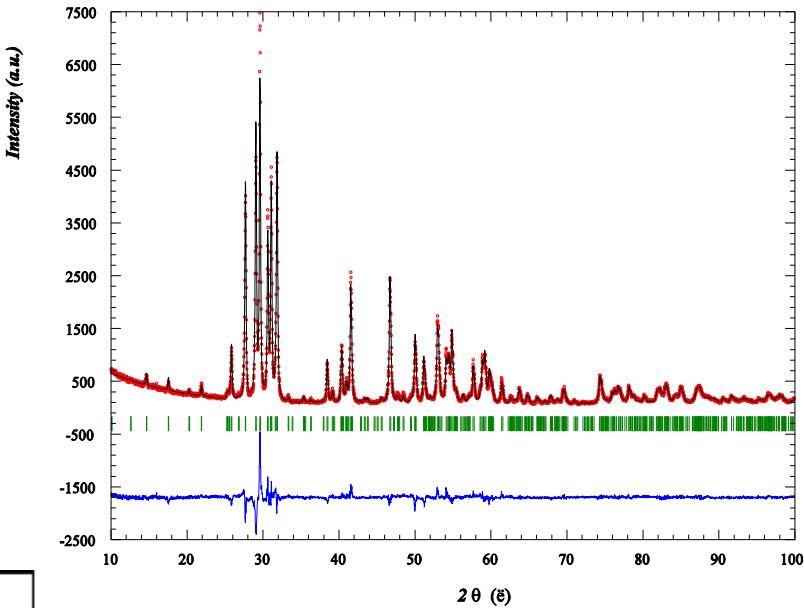


C = C-type cubic, B = Monoclinic, A = Hexagonal

Crystal structure of stabilized monoclinic phase of $Nd_{2-x}Y_xO_3$

Space Group: C2/m (12)

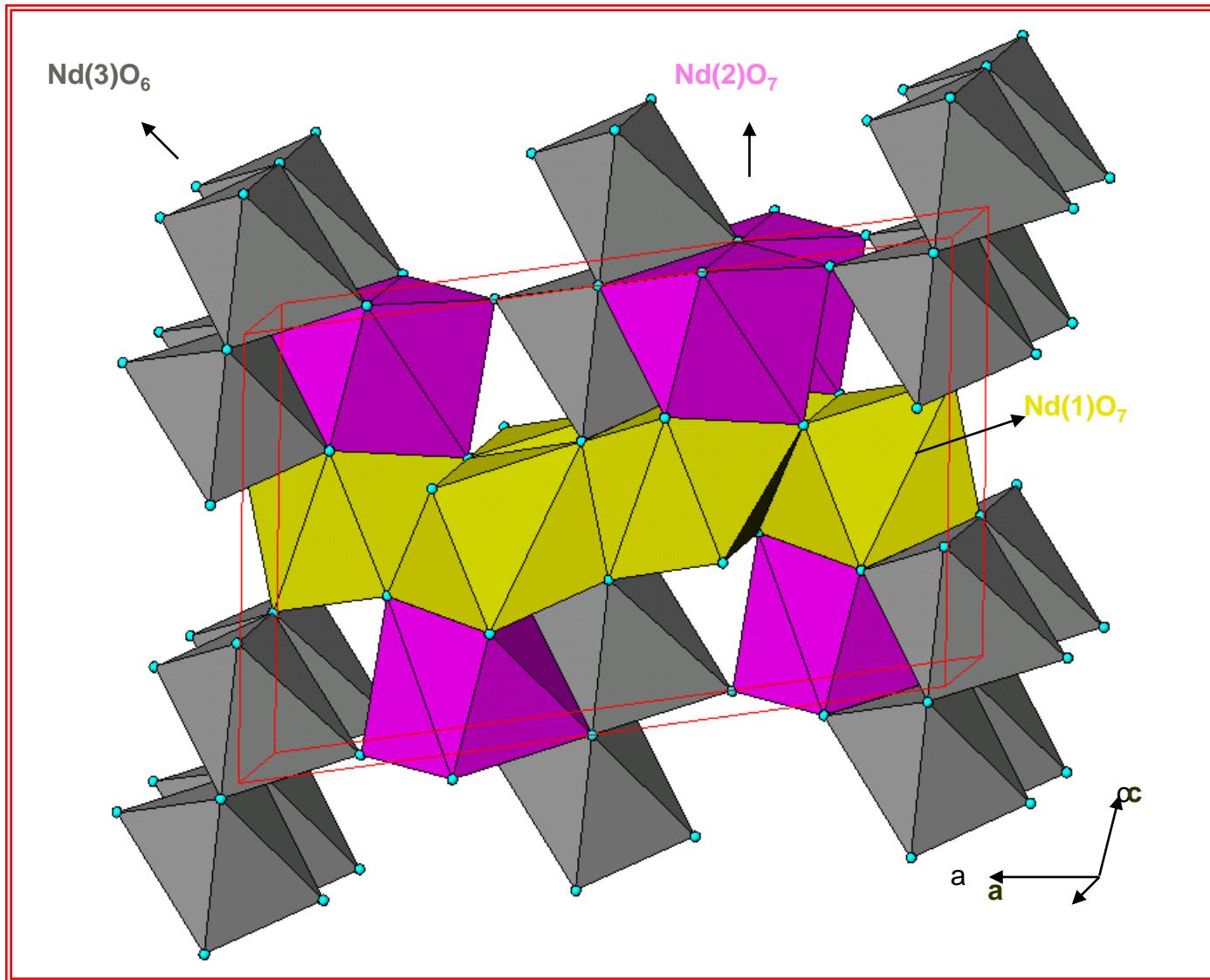
$a = 14.2761(3)$, $b = 3.6449(1)$, $c = 8.9022(2)$ Å, $\beta = 100.391(2)^\circ$
 $V = 455.62(2)$ Å 3 , $Z = 6$



Atoms	site	x	y	z	B_{iso} (Å) 2	occ.
Nd1	4i	0.1336(2)	0.5	0.4922(2)	0.75(7)	1
Nd2	4i	0.1885(2)	0.5	0.1379(2)	0.24(8)	1
Nd3	4i	0.4651(2)	0.5	0.1884(3)	0.72(6)	0.83(2)
Y	4i	0.4651(2)	0.5	0.1884(3)	0.72(6)	0.17(2)
O1	4i	0.1220(6)	0	0.2857(14)	0.6(2)	1
O2	4i	0.3279(5)	0.5	0.0270(10)	0.6(2)	1
O3	4i	0.2932(7)	0.5	0.3729(10)	0.6(2)	1
O4	4i	0.4795(7)	0.0	0.3416(11)	0.6(2)	1
O2	2b	0.0	0.5	0.0	0.6(2)	1

Y selectively occupy the six coordinated site of B-type rare-earth oxide lattice

Crystal structure of stabilized monoclinic phase of $Nd_{2-x}Y_xO_3$



Crystal structure thorium metavanadate

Crystal system: Tetragonal

Space Group: I 4₁/a (No. 88)

a = 8.5771(1) Å

c = 28.9739(4) Å

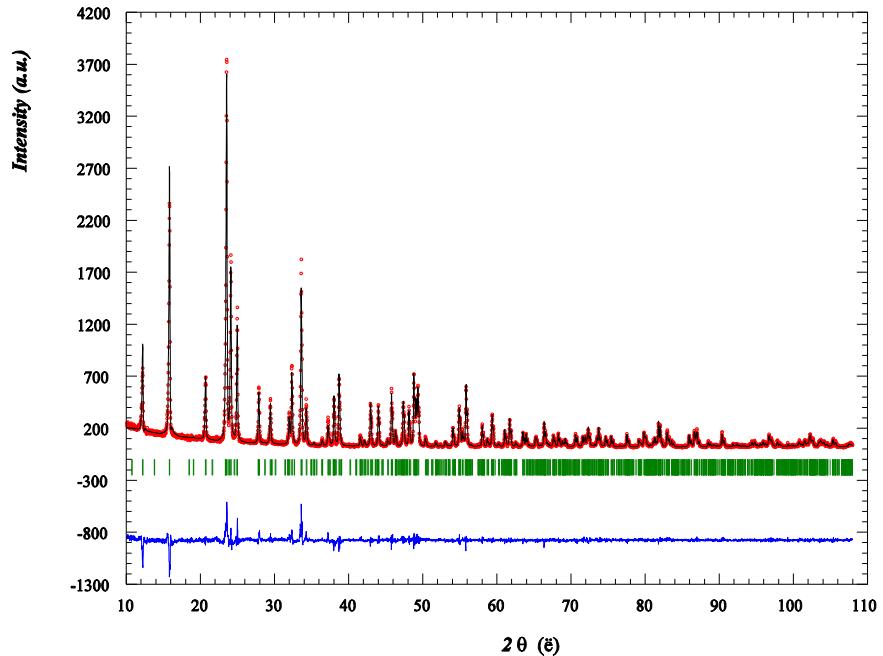
V = 2131.51(4) Å³

Z = 8

Density (x-ray) : 3.91 g/cc

R_p = 10.1 %, **R_{wp}** = 12.9 %, (χ^2) = 1.8 %

RB = 7.04 %, **RF** = 4.62 %



Structural formula

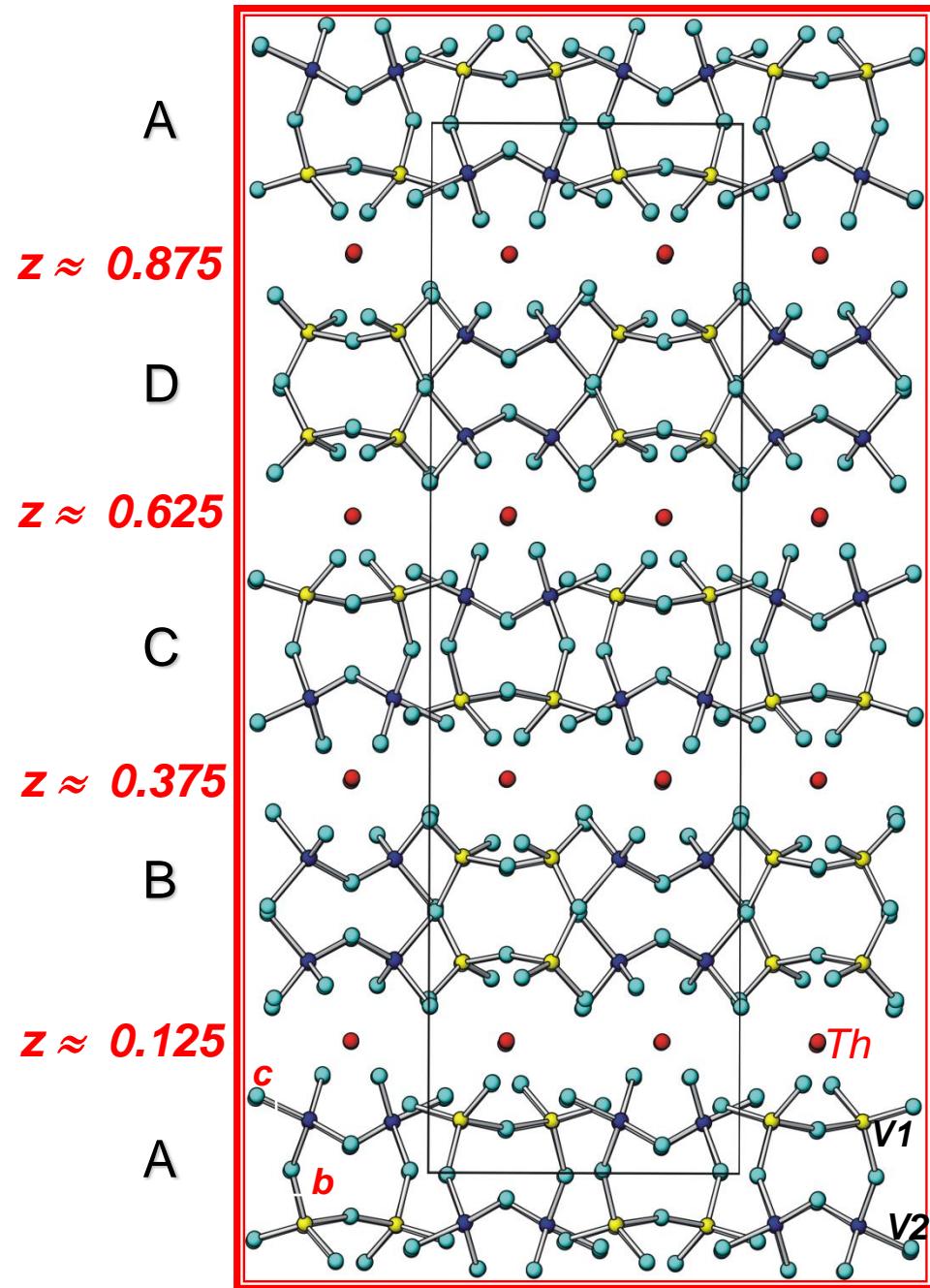
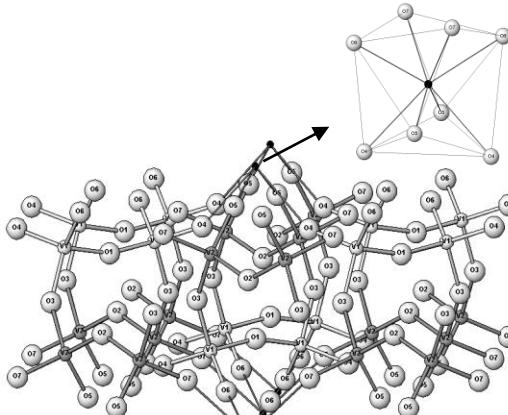
ThV(1)2V(2)2O(1)O(2)O(3)2O(4)2O(5)2O(6)2(O7)2

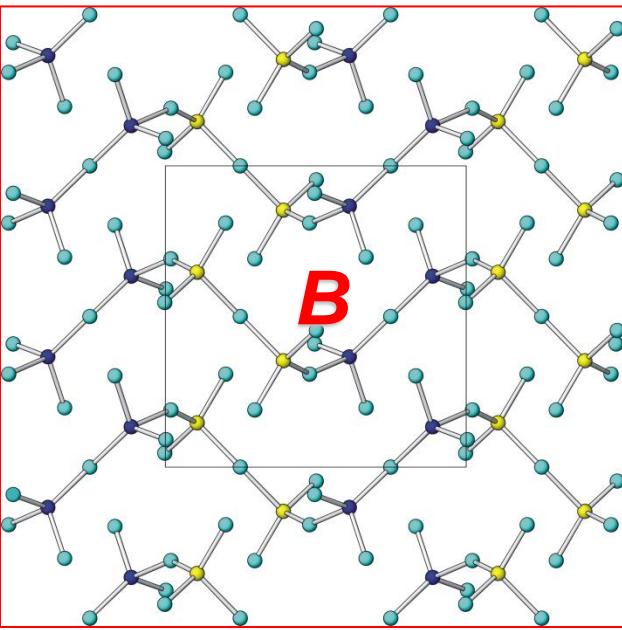
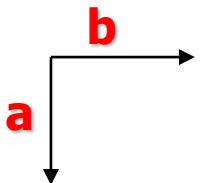
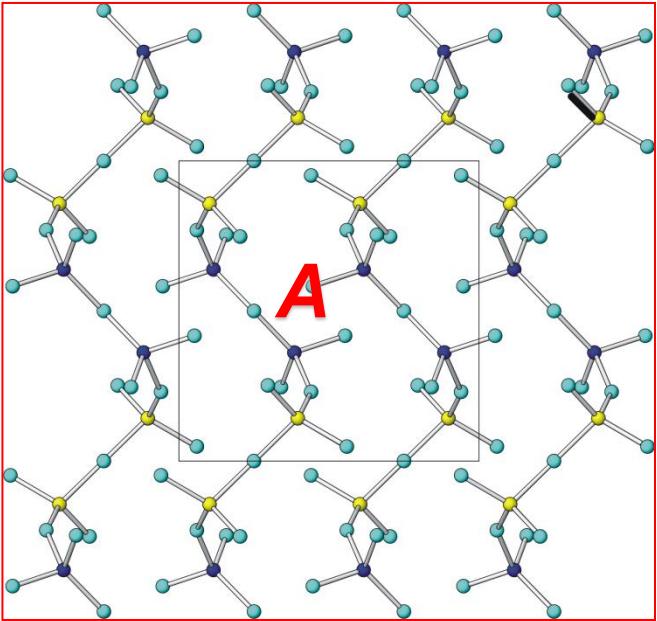
**Thorium have eight coordinated polyhedra and
Vanadium have tetrahedral coordination**

Crystal structure of $\text{Th}(\text{VO}_3)_4$

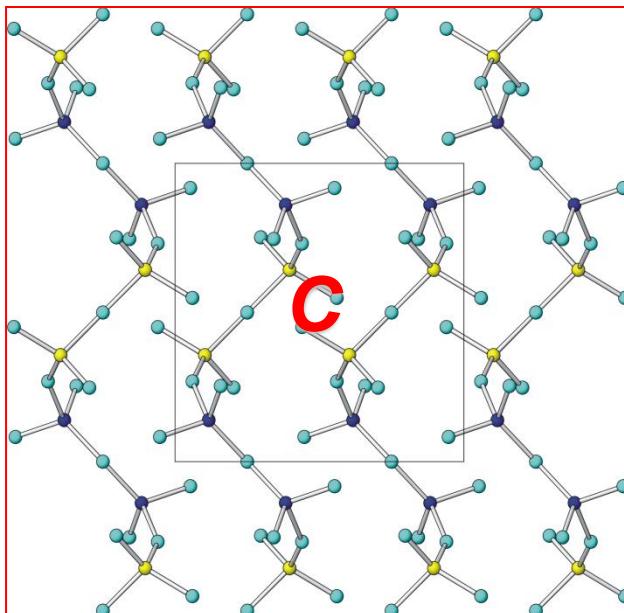
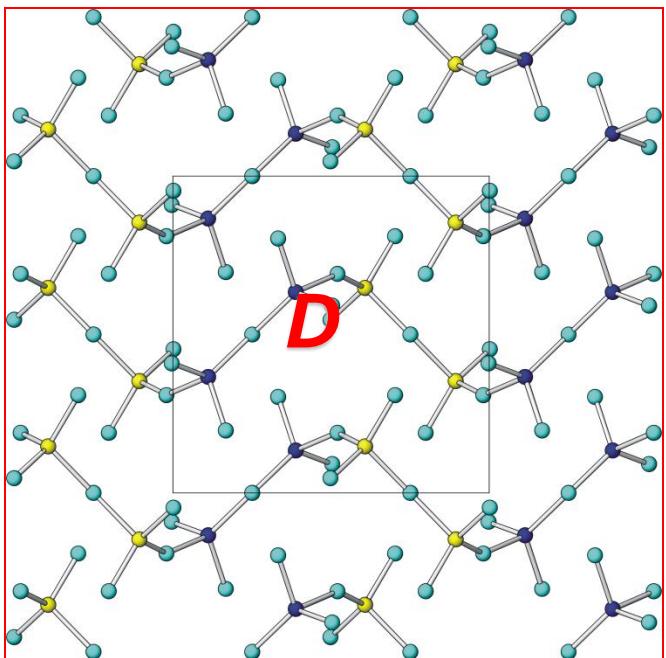
(projected along 001 direction)

Thorium atoms are sandwiched between the layers of VO_3 chains

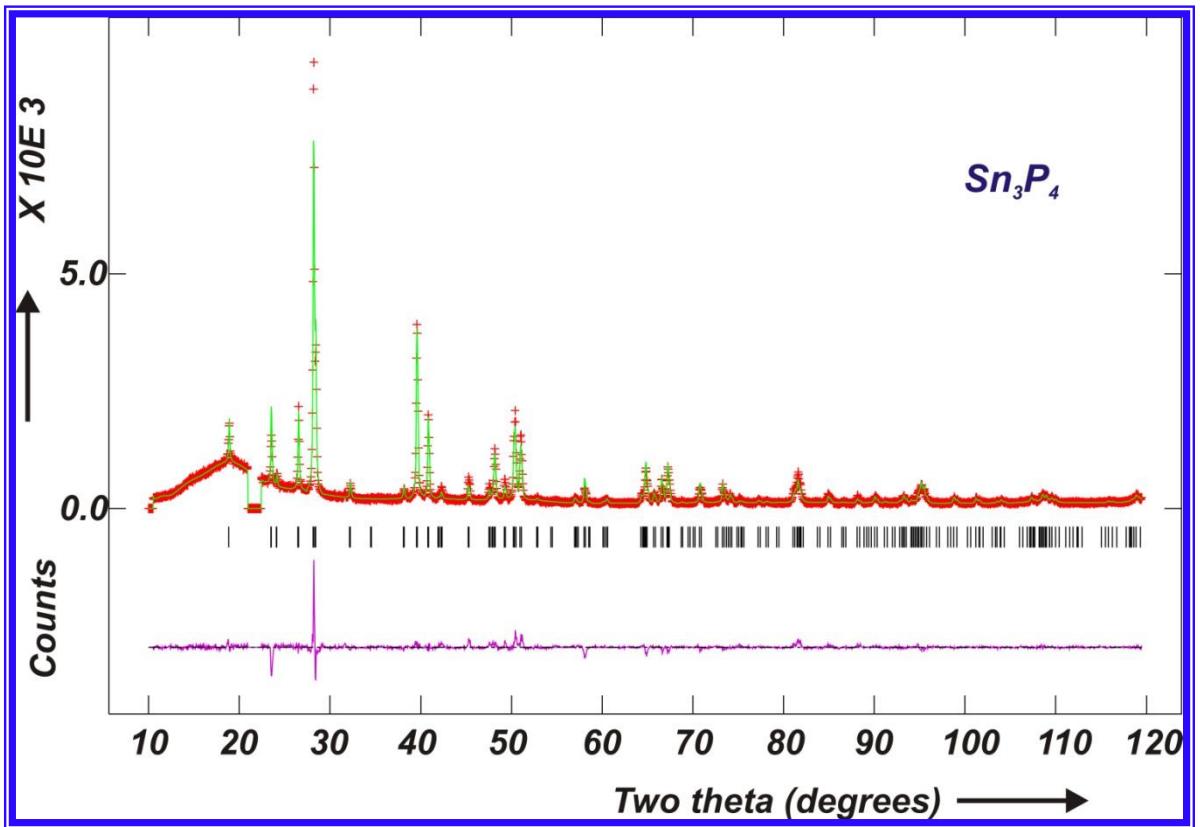




Propagation of VO_3 chains in different layers of $\text{Th}(\text{VO}_3)_4$ crystal structure

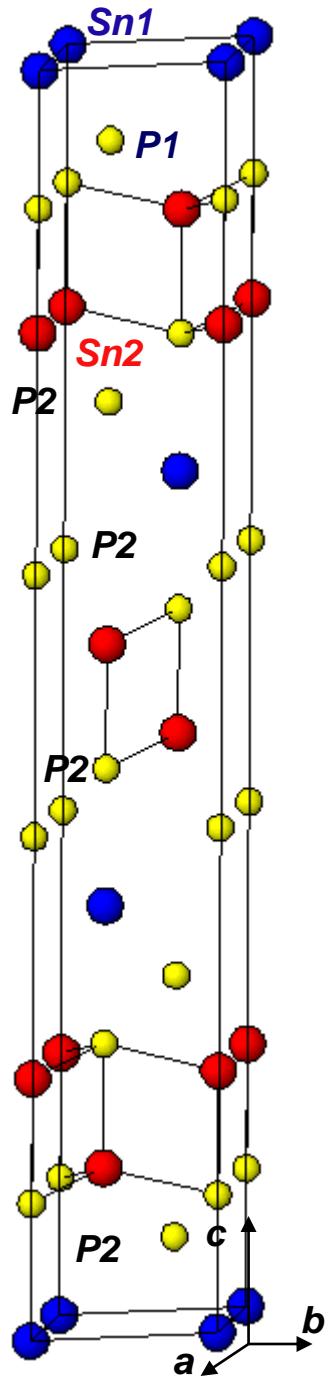


Crystal structure of Sn_3P_4

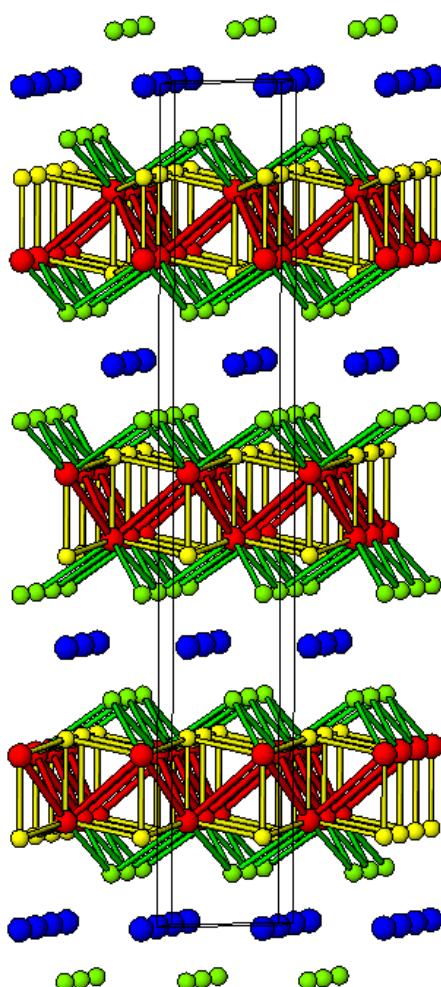
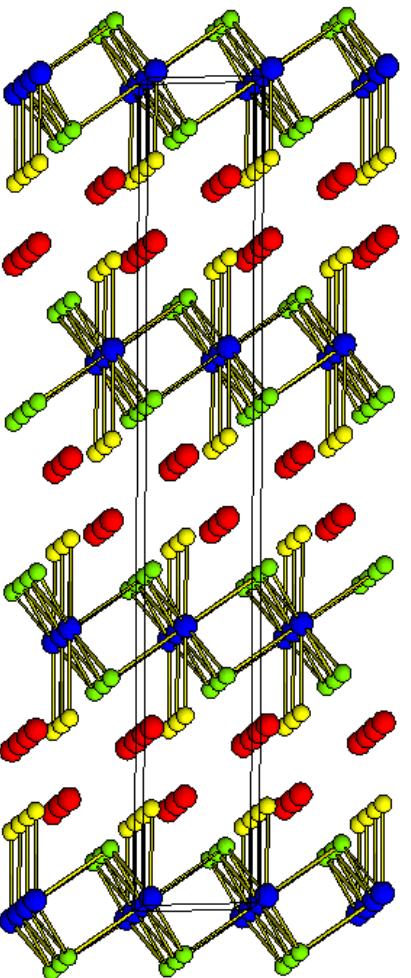
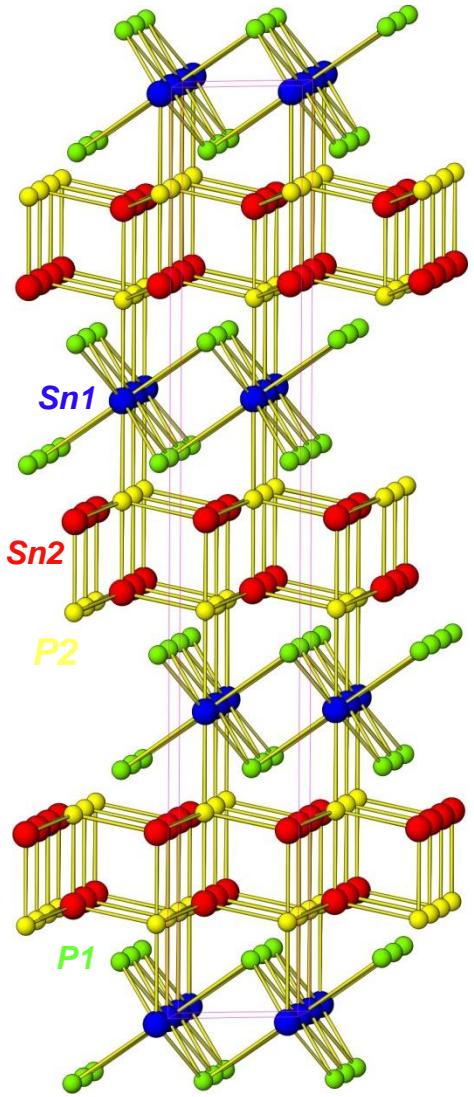


Rhombohedral (R-3m), No. 166
 $a = 4.4362(1)$ and $c = 28.4220(5)$ Å

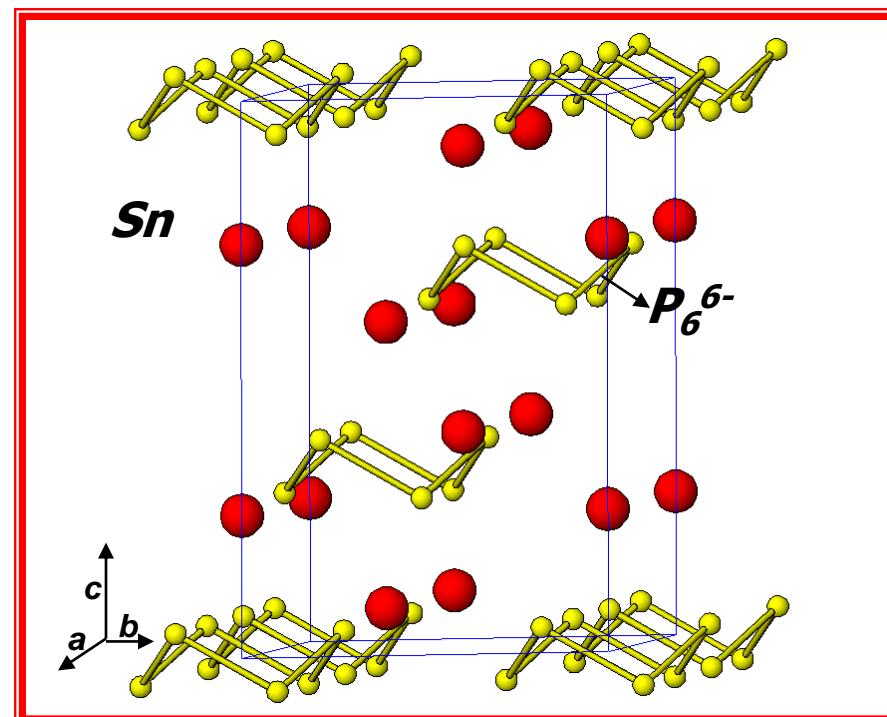
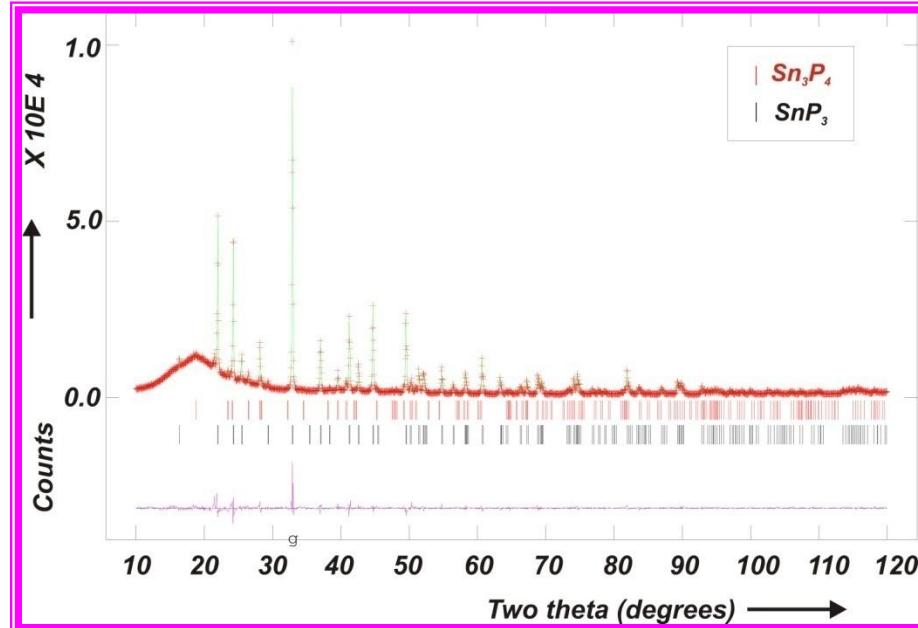
Atom	Wyck.	z	U_{11}	U_{22}	U_{33}	U_{12}
$\text{Sn}1$	3a	0	0.0079(10)	0.0079(10)	0.0153(4)	0.0040(5)
$\text{Sn}2$	6c	0.79371(6)	0.0258(8)	0.0258(8)	0.0215(7)	0.0129(4)
$P1$	6c	0.8918(14)	0.80(4)	0.80(4)	0.80(5)	0.40(2)
$P2$	6c	0.6030(6)	0.24(1)	0.24(1)	0.24(1)	0.120(6)



Crystal structure of Sn_3P_4



Crystal structure of SnP_3

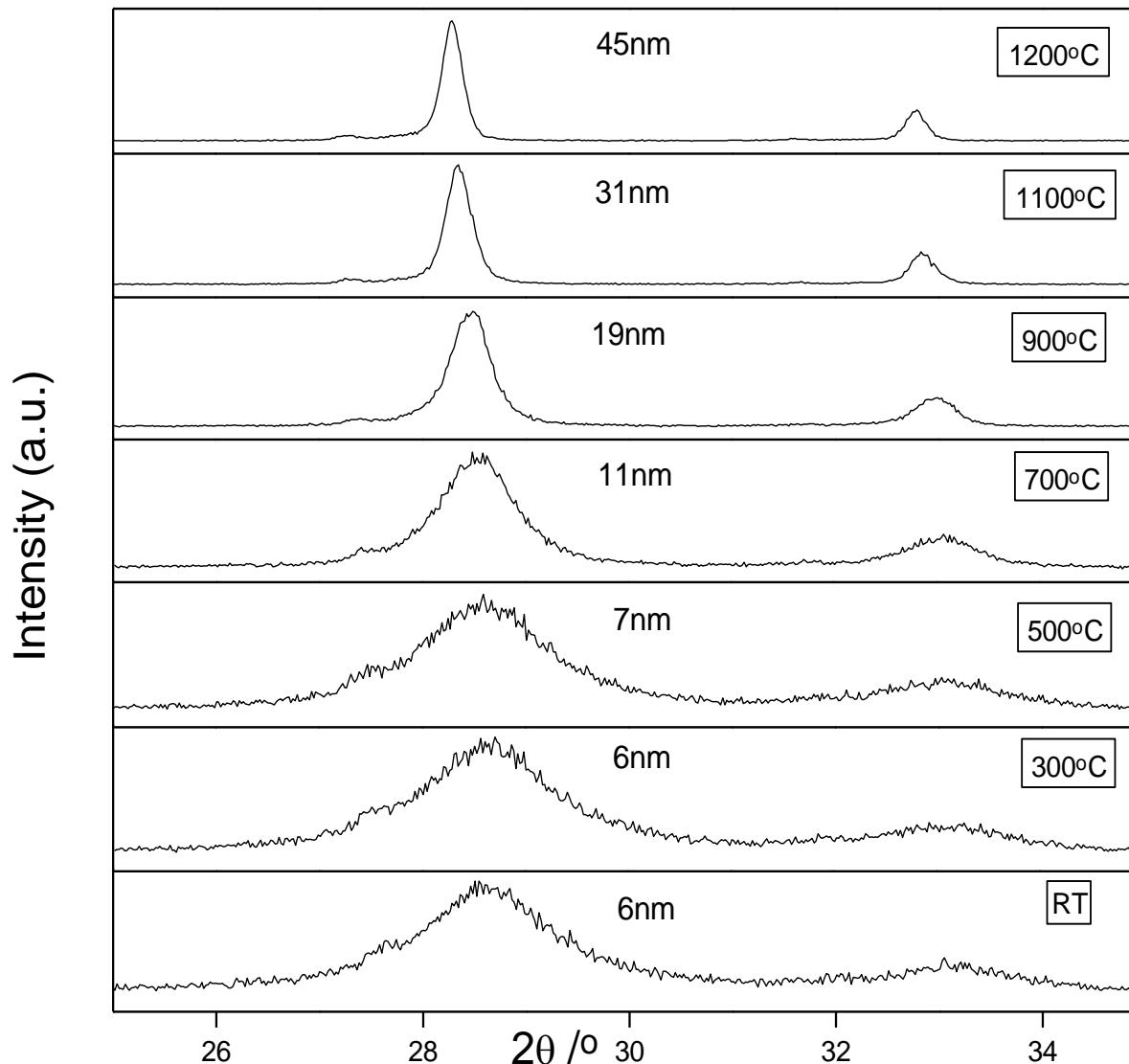


Rhombohedral (R-3m), No. 166
 $a = 7.3730(1)$ and $c = 10.5361(4)$

Atom	Wyck.	x	y	z
$\text{Sn}1$	$6c$ $(0,0,z)$	0	0	$0.2569(3)$
$\text{P}1$	$18h$ $(x-x,z)$	$0.5135(2)$	$0.4865(2)$	$0.2820(3)$

U_{11}	U_{22}	U_{33}	U_{12}	U_{13}	U_{23}
$0.0152(6)$	$0.0152(6)$	$0.022(2)$	$0.0076(3)$	0	0
$0.016(1)$	$0.016(1)$	$0.017(2)$	$0.009(2)$	$-0.0011(8)$	$0.0011(8)$

High Temperature XRD data for nc-Ce_{0.55}Y_{0.45}O_{1.775}



► Noticeable grain growth begins at 700°C

Crystallite size and strain in nano ZrO₂ powders

Tetragonal ZrO₂

(P42/nmc, Z = 2)

a = 3.5970(3), c = 5.1804(9) Å

V = 67.03(1) Å³

RB = 1.04 an RF = 0.90 %

Monoclinic ZrO₂

(P21/c, Z = 4)

a = 5.1420, b = 5.2010, c = 5.3111

and β = 99.2°, V = 140.2 Å³

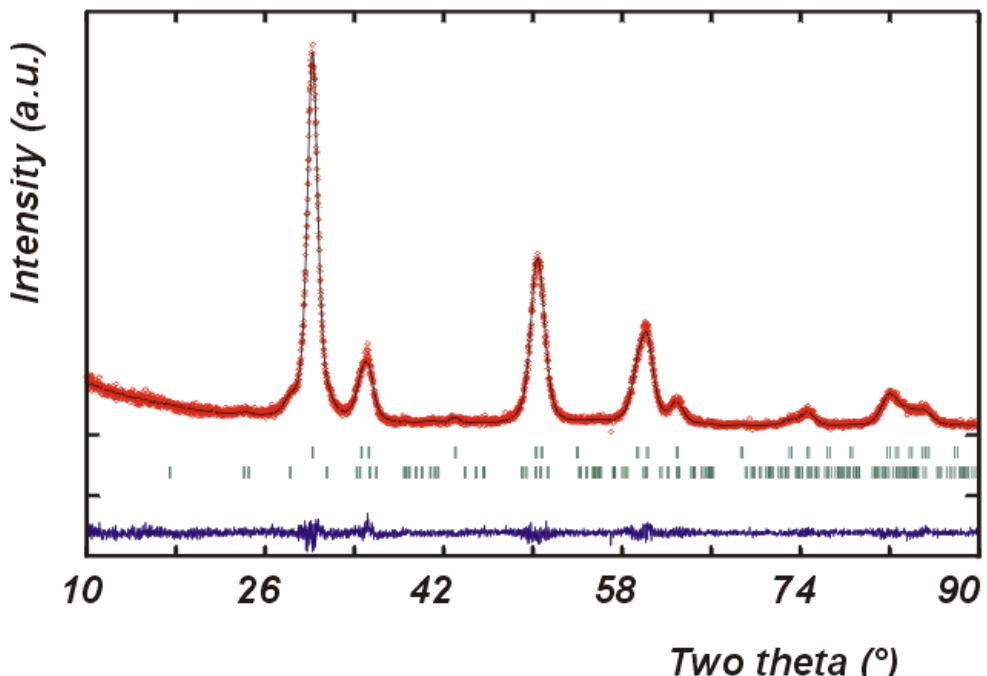
RB = 4.10 an RF = 2.1 %

R_p = 6.2, R_{wp} = 8.7, R_{exp} = 7.9 %

χ² = 1.21

Tetragonal ZrO₂ = 93.0(7)

Monoclinic ZrO₂ = 7.0(3)



$$V_S = K \frac{S_S^{(0)/\lambda} \times V_S}{S}$$

$$W_j = \frac{\frac{H \times \cos \theta}{\lambda} S_j Z_j M_j \bar{M}_j \bar{V}_j + 2\varepsilon \frac{\sin \theta}{\lambda}}{\sum (S_i Z_i M_i V_i / t_i)}$$

Tetragonal ZrO₂: Crystallite sizes 86 Å and strain ¹ 0.4 %

Property	X-ray diffraction	Neutron diffraction
Location of low Z elements	Not favourable	Favourable
Neighbouring elements	Difficult to distinguish	Easy to distinguish
Penetration	10-100 μm	Few cm
Sample size	Few mg	5-10 gm
Resolution	Good	Very good
Single crystal work	Easy to do	Not so easy
Monochromatization	Easy	Difficult
Isotopes	Cannot be differentiated	Can be differentiated
Magnetic structure	Cannot be obtained	Can be obtained
Study of lattice vibrations (dynamic)	Not possible	Possible
Preferred orientation	Problem	No effect
Intensity	Drops as angle increases	No correlation with angle

Thank you very much