"Dissemination of Education for Knowledge, Science and Culture" - Shikshanmaharshi Dr. Bapuji Salunkhe

# Shri Swami Vivekanand Shikshan Sanstha's Vivekanand College, Kolhapur (Autonomous) 



## DEPARTMENT OF MATHEMATICS

B.Sc. Part - I<br>Semester-I \& II

## SYLLABUS

## Under Choice Based Credit System

## B.Sc. I (Sem -I and II) Mathematics

## Course Structure

B. Sc. Part-I [ Semester I ]

| Course code | Title o the <br> course | Instructions <br> Lectures <br> /Week | Duration <br> of term <br> end <br> exa <br> $\mathbf{m}$ | Mark <br> $\mathbf{s}$ <br> Term <br> end <br> exa <br> $\mathbf{m}$ | Marks <br> (Internal) <br> Continuous <br> Assessment | Credit |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DSC -1003 A | Differentia <br> l Calculus | 5 | 3 hours | 80 | 20 | 4 |

B. Sc. Part-I [ Semester II ]

| Course code | Title o the <br> course | Instructions <br> Lectures <br> /Week | Duration <br> of term <br> end <br> exa <br> $\mathbf{m}$ | Mark <br> s <br> Term <br> end <br> exa <br> $\mathbf{m}$ | Marks <br> (nternal) <br> Continuous <br> Assessment | Credit |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DSC-1003 B | Differential <br> equations | 5 | 3 hours | 80 | 20 | 4 |

## Computational Mathematics Lab- DSC 1003(PR) Total Credit 04

| Cours <br> $\mathbf{e}$ <br> code | Title of the course | Instructi <br> ons <br> Lectures <br> /Week | Duration of term <br> end exam | Marks <br> [End of <br> academic <br> year] | Credit |
| :--- | :--- | :---: | :---: | :---: | :---: |
| DSC 3A | Differential Calculus | 4 | 3 hours | 50 | 4 |
| DSC 3B | Differential Equations | 4 | 3 hours | 50 |  |

## B. Sc. Mathematics Part - I CBCS <br> Semester - I Paper- I <br> Differential Calculus (DSC -1003A)

Theory: 60Hours (75 lectures of 48 minutes) - Credits -4
Course Outcomes: After the completion of the course the student will be able to -
CO1: Understand higher order derivative and its application
CO2: Identify a asymptote of function and sketch the graph of the function
CO3: Understand the consequences of various mean value theorems on differentiable functions
CO4: Calculate the limit and examine the continuity of a function at a point
CO5: Employ the theorem on properties of continuity in various examples
CO6: Understand the geometrical interpretation of mean value theorem

| Unit | Syllabus | Lectures/ <br> Teaching <br> Hours | Credi ts |
| :---: | :---: | :---: | :---: |
| Module 1 | Higher order Derivatives: <br> Successive Differentiation: $\mathrm{n}^{\text {th }}$ order derivative of standard functions: $y=(a x+b)^{m}, y=e^{a x}, y=a^{m x}$, $y=1 /(a x+b), y=\log (a x+b), y=\sin (a x+b), y=\cos (a x+b), y=$ $e^{a x} \sin (b x+c), y=e^{a x} \cos (b x+c)$, Examples on $n^{\text {th }}$ order derivatives, Leibnitz's theorem, Partial differentiation, Chain rule (without proof) and its examples, Euler's theorem on homogenous functions, Maxima and Minima for functions of two variables, Lagrange's method of undetermined multipliers | 15 | 1 |
| Module 2 | Tracing of Curves and its rectification: <br> Introduction, Definition of Terms: Tangents, Normals, Curvature, Asymptotes, Singular Points, Procedure for tracing of curve given in Cartesian form, Common Curves, Parametric representation of curves and tracing of parametric curves, Polar representation of curves and tracing of polar curves, Rectification of the curves Length of the arc of a curve given by $y=f(x)$, Length of the arc of the curve given by $\mathrm{r}=\mathrm{f}(\theta)$ | 15 | 1 |
| Module 3 | Mean Value Theorem and Indeterminate Forms : <br> Rolle's Theorem, Geometrical interpretation of Rolle's Theorem, Examples on Lagrange's Mean Value Theorem ( L.M.V.T. ), Geometrical interpretation of L.M.V.T., Examples on L.M.V.T., Cauchy's Mean Value Theorem ( C.M.V.T. ), Examples on C.M.V.T., Taylor's Theorem with Lagrange's and Cauchy's form of remainder, Maclaurin's Theorem with Lagrange's and Cauchy's form of remainder, Maclaurin's series for $\sin x, \cos x, \mathrm{e}^{\mathrm{x}}$, $\log (1+x),(1+x)^{m}$, Examples on Maclaurin's series, | 15 | 1 |


|  | Examples on maxima and minima of function, Indeterminate Forms |  |  |
| :---: | :---: | :---: | :---: |
| Module 4 | Limits and Continuity of real valued functions : <br> $\in-\delta$ definition of the limit of a function of one variable, Left hand sides limit and right hand sides limit, Theorem om limits(statement only), Continuous function and their properties, If $f$ and $g$ are two real valued functions of a real variables which are continuous at $\mathrm{x}=\mathrm{c}$ <br> i) $f+g$ ii) $f-g$ iii)f.g are continuous at $x=c$. and iv) $f / g$ is continuous at $x=c, g(c) \neq 0$, Composite function of two continuous functions is continuous, Classification of discontinuities ( First and second kind ), simple discontinuities ,Removable discontinuity, Jump discontinuity of first kind, Jump discontinuity of second kind, Differentiability at a point, left hand derivative, right hand derivative, differentiability in the interval [a, b], Theorem: Continuity is necessary but not a sufficient condition of differentiability, If function $f$ is continuous in closed interval $[a, b]$, then it is bounded in $[a, b]$, If function f is continuous in closed interval $[\mathrm{a}, \mathrm{b}]$, then it attains its bounds at least one in [a, b].If a function $f$ is continuous in a closed interval $[a, b]$ and if $f(a), f(b)$ are of opposite signs then there exists $c \in[a, b]$ such that $f(c)$ $=0$, If a function $f$ is continuous in a closed interval $[a, b]$ and if $f(a) \neq f(b)$ then $f$ assumes every value between $f(a)$ and $f(b)$. | 15 | 1 |

## Reference Books:

1) H. Anton, I. Birens and Davis, Calculus, John Wiley and Sons, Inc. 2002.
2) G. B. Thomas and R. L. Finney, Calculus and Analytical Geometry, Pearson Education,2007.
3) Maity and Ghosh, Differential Calculus, New Central Book Agency (P) limited,Kolkata,India. 2007.
4) Shanti Narayana and P. K. Mittal, A Course of mathematical Analysis, S. Chand andCompany, New Delhi. 2004.
5) S. C. Malik and Savita arora, Mathematical Analysis (second Edition), New AgeInternational Pvt. Ltd., New Delhi, Pune, Chennai.

## B. Sc. Mathematics Part - I CBCS <br> Semester - I Paper- I <br> Differential Equationa (DSC -1003b)

Theory: 60 Hours ( 75 lectures of 48 minutes) - Credits $\mathbf{- 4}$
Course Outcomes: After the completion of the course the student will be able to -
CO1: Learn various techniques of getting exact solutions of solvable first order differential equations and linear differential equations of higher order
CO2: Calculate P. I. and C.F. of different types of differential equations
CO3: Solve homogeneous and non - homogeneous partial differential equation
CO4: Solve homogeneous and non homogeneous differential equation.
CO5: Solve the differential equation of degree more than one
CO6: Classify the partial differential equations

| Unit | Syllabus | Lectures/ <br> Teaching <br> Hours | Credi <br> ts |
| :--- | :--- | :--- | :--- |
| Module 1 | Differential Equations of First Order and First <br> Degree:Exact Differential Equations: <br> Necessary and Sufficient condition for exactness, <br> Working Rule for solving an Exact Differential Equation, <br> Integrating Factors, Integrating Factor by Inspection and <br> examples, Integrating Factor by using Rules (Without <br> Proof) and examples, Linear Differential Equations: <br> Definition, Method of Solution and Examples, Bernoulli's <br> Equation: Definition, Method of Solution and Examples. <br> Differential Equations of First Order But Not of First <br> Degree: Equation solvable for p, equation solvable for x, <br> equation solvable for y, Clairaut's form, equation <br> reducible to Clairaut's equation | 1 |  |
| Module 2 | Linear Differential Equations With Constant <br> Coefficients:: Introduction. <br> General Solution, Determination of Complementary <br> Function, The Symbolic Function 1/f(D):Definition., <br> Theorems about 'D' Determination of Particular <br> Integral, General Method of Getting P.I, Short Methods <br> of Finding P.I. when X is in the form eax, sin ax, cos ax, <br> $x^{m}(m$ being a Positive Integer), eaxV, x V where Vis a <br> function of x, Examples. Homogeneous Linear <br> Differential Equations (The Cauchy-Euler Equations): <br> Introduction, Method of Solution, Legendre's Linear <br> Equations. Method of Solution of Legendre's Linear <br> Equations.Examples | 15 | 1 |
| Module 3 | Second Order Linear Differential <br> Ser | 15 |  |



|  | equations, Only $\mathrm{p}, \mathrm{q}$ and z present, $f(x, p)=g(y, q)$, <br> examples |  |  |
| :--- | :--- | :--- | :--- |

## Reference Books:

1) M. D. Raisinghania, Ordinary and Partial Differential Equations, Eighteenth Revisededition 2016; S. Chand and Company Pvt. Ltd. New Delhi
2) Shepley L. Ross, Differential Equations, Third Edition 1984; John Wiley and Sons, NewYork
3) Ian Sneddon, Elements of Partial Differential Equations, Seventeenth Edition, 1982;Mcgraw-Hill International Book Company, Auckland
4) R. K. Ghosh and K. C, Maity, An Introduction to Differential Equations, Seventh Edition,2000; Book and Allied (P) Ltd
5) D. A. Murray, Introductory course in Differential Equations, Khosala Publishing House, Delhi.

## B. Sc. Part - I CBCS <br> Semester - I and II

## COMPUTATIONAL MATHEMATICS LAB (I)

## DSC-1003A(PR)DSC 3A: DIFFERENTIAL CALCULUS

## 60 Hours (75 Lectures) credits 2

1) Examples on Leibnitz's theorem
2) Examples on Euler's theorem
3) Applications of De Moivre's Theorem
4) Tracing of curves in Cartesian form
5) Polar coordinates and tracing of curves in polar form
6) Radius of curvature for Cartesian curve i.e. For $y=f(x)$ or $x=f(y)$.
7) Radius of curvature for Parametric curve (i.e. $x=f(t), y=g(t))$ and radius ofcurvature for polar curve (i.e. $r=f(\square)$ )
8) Examples on Lagrange's Mean Value theorem
9) Examples on Cauchy's Mean Value theorem
10) L'Hospital Rule:- ${\underset{0}{\prime}}_{\prime}^{\infty}, \infty-\infty, 0^{\infty}, 1^{\infty}, \infty^{\infty}$.

## COMPUTATIONAL MATHEMATICS LAB

 (II)DSC 3B: DIFFERENTIAL EQUATIONS60 Hours (75 Lectures) credits 2

1) Orthogonal trajectories (Cartesian)
2) Orthogonal trajectories (Polar)
3) Simultaneous Differential Equations
4) Total differential Equations
5) Examples on Linear Differential Equations with Constant Coefficients
6) Examples on Exact Differential Equations
7) Examples on Charpit's method.
8) Examples on Clairaut' s Forms.
9) Plotting family of solutions of second order differential equations
10) Plotting of Curves.

Structure of B. Sc. I ( Semester I\&II) ( Mathematics)

| B. Sc. I | Subject (Core Course) | No. <br> of <br> Lect. | Hours | Credit |
| :---: | :--- | :---: | :---: | :---: |
| Semester-I | MATHEMATICS-DSC 1003A : <br> DIFFERENTIAL CALCULUS | 5 | 4 | 4 |
|  | MATHEMATICS LAB(I): DSC 1003(PR) : <br> DIFFERENTIAL CALCULUS | 4 | 3.2 | 2 |
|  | MATHEMATICS -DSC 1003B: | DIFFERENTIAL EQUATIONS | 5 | 4 |
|  | MATHEMATICS LAB(II)- DSC 1003B(PR): <br> DIFFERENTIAL EQUATIONS | 4 | 3.2 | 2 |

SCHEME OF MARKING (THEORY)

| Sem. | DSC | Marks | Evaluation | Sections | Answer <br> Books | Standardof <br> passing |
| :---: | :--- | :---: | :---: | :---: | :---: | :---: |
| I | DSC1003 A | 80 | Semeste <br> rwise | Two <br> sections <br> each of <br> 40marks | As per <br> Instructi <br> on | $35 \%$ <br> $(28$ <br> marks) |
| II | DSC1003 B | 80 | Semeste <br> rwise | Two <br> sections <br> each of 40 <br> marks | As per <br> Instructi <br> on | $35 \%$ <br> $(28$ marks $)$ |

SCHEME OF MARKING (CIE) Continuous Internal Evaluation

| Sem. | DSC | Marks | Evaluatio <br> $\mathbf{n}$ | Sections | Answe <br> $\mathbf{r}$ <br> Books | Standar <br> dof <br> passing |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I | DSC1003 <br> A | 20 | Concurre <br> nt | - | As per <br> Instructi <br> on | $35 \%$ <br> $(7$ marks $)$ |
| II | DSC1003 B | 20 | Concurre <br> nt | - | As per <br> Instructi <br> on | $35 \%$ <br> $(7$ marks $)$ |

SCHEME OF MARKING (PRACTICAL)

| Sem. | DSC | Marks | Evaluation | Sections | Standard <br> ofpassing |
| :--- | :--- | :--- | :--- | :--- | :---: |
| I AND II | DSC1003 A (pr) | 50 | Annual | As per <br> Instructi <br> on | $35 \%$ <br> $(18$ |
|  | DSC1003 A (pr) |  |  | marks) |  |

## Nature of Question Paper

Instructions: 1) All the questions are compulsory.
2) Answers to the two sections should be written in same answer book.
3) Figures to the right indicate full marks.
4) Draw neat labeled diagrams wherever necessary.
5) Use of $\log$ table/calculator is allowed.

Time : $\mathbf{3}$ hours
Total Marks: 80

## SECTION-I

## Q.1. Choose correct alternative.

i)
A)
B)
C)
D)
ii)
iii) A)
B)
C)
D)
iv)
A)
B)
C)
D)
v)
A)
B)
C)
D)
vi)
A)
B)
C)
D)
vii)
A)
B)
C)
D)
viii)
A)
A)
B)
B)
C)
C)
D)
D)

## Q.2. Attempt any two.

A)
B)
C)
Q.3. Attempt any four.
A)
B)
C)
D)
E)
F)

## SECTION-II

$\begin{array}{ll}\text { Q.4. Choose correct alternative. } & 8\end{array}$
i)
A)
B)
C)
D)
ii)
iii) A)
B)
C)
D)
iv) $A$ )
B)
C)
D)
v)
A)
B)
C)
D)
A)
B)
C)
D)
vi)
A)
B)
C)
D)
vii)
A)
B)
C)
D)
viii)
A)
B)
C)
D)

## Q.5. Attempt any two. <br> A) <br> B) <br> C)

Q.6. Attempt any four.
A)
B)
C)
D)
E)
F)
$\qquad$

