

"Dissemination of Education for Knowledge, Science and Culture"  
-Shikshanmaharshi Dr. Bapuji Salunkhe  
Shri Swami Vivekanand Shikshan Sanstha, Kolhapur

**Vivekanand College, Kolhapur (Autonomous)**  
**Department of Physics**

**M.Sc. Part- I**  
**Classical Mechanics**  
**Surprise Test**

**Date : 19/10/2018**  
**Day: - Saturday**

**Total Marks: 20**  
**Time :- 2pm to 3pm**

**Instructions:-**

- 1) All questions are compulsory.
- 2) Figures to the right indicate full marks.
- 3) Use of log table and calculator is allowed.

**Q.1 Choose the correct alternative**

**(05)**

1. Many different ..... may correspond to the same microstate.  
(a) microstates (b) phase points (c) phase densities (d) space point
2. The microstates which are allowed under given restriction are called .....  
(a) allowed microstate (b) permitted microstates  
(c) accessible microstates (d) occupied microstates
3. For the distribution to be most probable.....  
(a)  $W = 0$  (b)  $\ln W$  ( $\ln W$ )=0  
(c)  $\delta (\ln W) = 0$  (d)  $\delta W=0$
4. The entropy has its maximum value for a thermodynamic assembly in... state.  
(a) an equilibrium (b) an inequilibrium  
(c) a normal (d) an excited
5. Canonical in symbol is related to ---  
(a) size to the system (b) number of particles in the system  
(c) thermal equilibrium of the system (d) freedom of the system

**Q.2 Attempt any one**

**(05)**

1. Verify Liouville's Theorem in classical presentation.
2. Derive an expression for the total probability of particular distribution.

**Q3 Attempt any one**

**(10)**

1. Explain microstate and macrostate with suitable examples.
2. Discuss concept of ensemble with its types.





"Dissemination of Education for Knowledge, Science and Culture"  
-Shikshanmaharshi Dr. Bapuji Salunkhe  
Shri Swami Vivekanand Shikshan Sanstha, Kolhapur

**Vivekanand College, Kolhapur (Autonomous)**  
**Department of Physics**

**M.Sc. I**  
**Classical Mechanics**  
**Surprise Test**  
**Result**

Date : 19/10/2018

Roll. No.	Marks	Roll. No.	Marks
1331	09	1355	-
1332	13	1356	12
1333	10	1357	11
1334	08	1358	-
1335	11	1359	-
1336	-	1360	-
1337	-	1361	-
1338	-	1362	-
1339	-	1363	09
1340	09	1364	09
1341	07		
1342	-		
1343	-		
1344	-		
1345	-		
1346	10		
1347	-		
1348	-		
1349	-		
1350	-		
1351	11		
1352	-		
1353	12		
1354	-		

Teacher Incharge.....  
(Mr. A.V. Shinde)

  
Head of the  
Department of Physics  
Vivekanand College, Kolhapur.

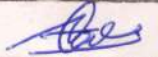


shradha sanjay chougale

" ज्ञान, विज्ञान आणि सुसंस्कार यांसाठी शिक्षण प्रसार "

- शिक्षणमहर्षी डॉ. बापूजी साबुंबे

Signature of Supervisor



Shri Swami Vivekanand Shikshan Sanstha's  
**VIVEKANAND COLLEGE (Autonomous), KOLHAPUR**

Class M.Sc-I Div - Roll No. 1332

Suppliment No. \_\_\_\_\_ Subject Physics

Test / Tutorial No. \_\_\_\_\_

Q1

1) Microstates,

2) accessible microstate

3)  $\delta(\ln w) = 0$

4) an equilibrium

5) thermal equilibrium of the system

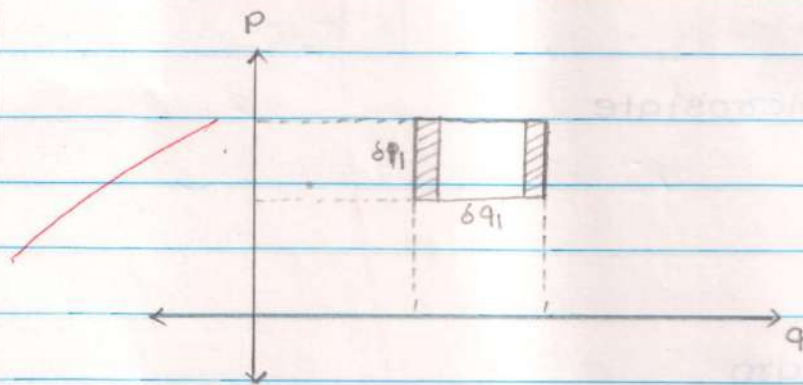
Q2. 2.

Infinitesimal hyper volume of phase point is certain density of the time.

$$\frac{dD}{dt} = 0$$

$$dJ = dq_1, dq_2, \dots, dq_f \cdot dp_1, dp_2, \dots, dp_f$$

$$dJ(q, p, t) = 0$$



The two dimensional phase space

$$\frac{dD}{dt} = \frac{dD}{dq_1} dq_1 + \dots$$

$$= \frac{dD}{dq_1} dq_1 + dt dq_2 \dots dp_f$$

$$= D \dot{q}_1 dt dq_2 \dots dp_f \quad \text{--- (1)}$$

this is the entire phase space.

The leaving is,

$$= D \dot{q}_1 dt dq_2 \dots dp_f + \frac{dD}{dq_1} dq_1$$

$$\left( D \dot{q}_1 dt dq_2 \dots dp_f \right)$$

$$= D \dot{q}_1 dt dq_2 \dots dp_f + \left[ \frac{dD}{dq_1} \dot{q}_1 dt + \frac{dD}{dt} \dot{q}_1 dt \right]$$

$dq_2 \dots dp_f$

(2)



$$Dq_1 dt dq_2 \dots dq_n - \left[ \frac{d\dot{q}_1}{dt} \dot{q}_1 dt + \frac{dD}{dt} dq_1 dt \right] dq_2 \dots$$

$$+ Dq_1 dt dq_2 \dots dq_n - dp_f.$$

$$Dq_1 dt dq_2 \dots dq_n - dp_f - Dq_1 dt dq_2 \dots dq_n +$$

$$\left[ \frac{d\dot{q}_1}{dt} \dot{q}_1 dt + \frac{dD}{dt} dq_1 dt \right] dq_2 \dots$$

$$= - \left[ D \frac{dq_1}{dt} + \frac{dD}{dt} dq_1 \right] \mathcal{I}$$

$$\therefore d\mathcal{I} = (dq_1 \dots dq_n - dp_f)$$

for  $p_1$  co-ordinate

$$= - \left[ D \frac{dp_1}{dt} + \frac{dD}{dt} dp_1 \right] \mathcal{I}$$

The total time in phase point is,

$$\frac{\partial(\mathcal{I})}{dt} = - \left[ D \frac{dq_1}{dt} + \frac{dD}{dt} dq_1 \right] +$$

$$\left[ D \frac{dp_1}{dt} + \frac{dD}{dt} dp_1 \right] dt$$

$$= D \left[ \frac{dq_1}{dt} + \frac{dp_1}{dt} \right] + \left[ \frac{dD}{dt} dq_1 + \frac{dD}{dt} dp_1 \right] dt d\mathcal{I}$$

$$\therefore = \sum_{i=1}^n D \left[ \frac{dq_i}{dt} + \frac{dp_i}{dt} \right] + \left[ \frac{dD}{dt} dq_i + \frac{dD}{dt} dp_i \right] dt d\mathcal{I}$$

4 Hamilton's eq<sup>n</sup> is,

$$\frac{\partial \mathcal{H}}{\partial q_i} = \dot{p}_i, \quad \frac{\partial \mathcal{H}}{\partial p_i} = \dot{q}_i$$





**Shri Swami Vivekanand Shikshan Sanstha's  
VIVEKANAND COLLEGE (Autonomous), KOLHAPUR**

Class M.Sc - I Div \_\_\_\_\_ Roll No. 1332

Suppliment No. \_\_\_\_\_ Subject \_\_\_\_\_

Test / Tutorial No. \_\_\_\_\_

Q3 1. Macrostate →

The particles are distributed in the macrostate in compartmently. The 4 particles are distributed in the two equal space compartment. In this compartment particles randomly distributed. the way of the particles distributed in compartment is as follow.

Compartment	arrangement .				
	Distribution 1	Distribution 2	Distribution 3	Distribution 4	Distribution 5
compartment 1	0	1	2	3	4
compartment 2	4	3	2	1	0

The arrangement of the particles in two compartments is .

$(0,4), (1,3), (2,2), (3,1), (4,0)$

This is for 4 particles is distributed in two compartments .

i.e for n particles are distributed in two compartment is .

$(0,n) (n,n-1) \dots (n-1,n), (0,n)$



∴ The number of particles distributed in compartment is known as macrostate.

Microstates →

The distinct arrangement of the particles is known as microstates.

macrostate	arrangement.		Microstate
	I	II	
(0,4)	0	abcd	1
(1,3)	a	bcd	4
	b	acd	
	c	abd	
	d	abc	
(2,2)	ab	cd	6
	ac	bd	
	ad	cb	
	bc	ad	
	bd	ac	
	cd	ab	
(3,1)	bcd	a	4
	acd	b	
	abd	c	
	abc	d	



The arrangement of particles is the  
(0,4) Macrostate is 1 microstate, (1,3)  
Macrostate is 4 microstate, (2,2)  
Macrostate is 6 microstate, (3,1)  
Macrostate is 4 microstate, (4,0) Macrostate  
is 1 microstate.

each macrostate have same microstate.  
The example of microstate is the particle  
having  $2^4 = 16$ , then for  $n$  particle  
is  $2^n$ .

The total no. of microstate is  $2^n$ .

oh



Shri Swami Vivekanand Shikshan Sanstha's  
**VIVEKANAND COLLEGE (Autonomous), KOLHAPUR**

Class M.Sc - I Div \_\_\_\_\_ Roll No. 1333

Suppliment No. \_\_\_\_\_ Subject Physics

Test / Tutorial No. \_\_\_\_\_

Q. 1

~~1) a) microstates~~

~~→ 2) b) accessible microstate.~~

~~3) c)  $\delta(I_{nW}) = 0$~~

~~4) a) An equilibrium~~

~~3) c) thermal equilibrium system.~~

5





# Shri Swami Vivekanand Shikshan Sanstha's VIVEKANAND COLLEGE (Autonomous), KOLHAPUR

Aishwarya Suryakant Gaikwad

Class M.Sc I Div 11/20 Roll No. 1334  
Suppliment No. \_\_\_\_\_ Subject Statistical Mech.  
Test / Tutorial No. Internal Examination-2

Que. 1.

- 1) ~~Microstate.~~
- 2) ~~accessible microstates.~~
- 3)  ~~$\ln W = 0$ .~~
- 4) ~~An equilibrium.~~
- 5) ~~Thermal equilibrium of the system.~~

4  
Que. 2. Liouville's Theorem →

interna) super hypervolume points

$$\frac{dD}{dt} = 0.$$

Where,  $d\Gamma = dq_1 dq_2 \dots dq_f$ . which is position co-ordinate.  
 $dp_1 dp_2 \dots dp_f$  which is momentum co-ordinate

No. of density point are  $D(P, q, t)$ .

No. of phase point between insmation of 1st Face

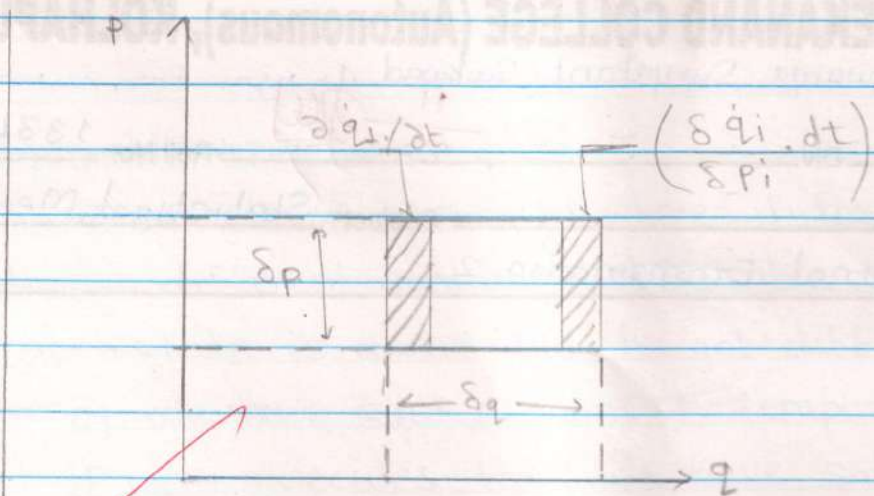
$$\therefore dV = dq_1 \cdot dq_2 \cdot dq_3 \cdot \dots \cdot dq_f$$

$$d\Gamma = dp_1 \cdot dp_2 \cdot dp_3 \cdot \dots \cdot dp_f$$

$$\therefore \text{Then, } d\Gamma = dq_1 \cdot dq_2 \cdot dq_3 \cdot \dots \cdot dq_f \cdot dp_1 \cdot dp_2 \cdot dp_3 \cdot \dots \cdot dp_f$$

$$d\Gamma = dV d\Gamma$$





Now, moment of system entering in co-ordinate. in 1<sup>st</sup> Face.

$$= D \cdot \frac{\partial \dot{q}_1}{\partial q_1} \cdot dt \cdot dq_2 \dots dq_F \cdot dP_1 \cdot dP_2 \dots dP_F$$

$$= D \cdot \frac{\partial \dot{q}_1}{\partial q_1} \cdot dt \cdot dq_2 \dots dq_F + \left[ D \left( \frac{\partial \dot{p}_1}{\partial p_1} \cdot dt \cdot dP_2 \cdot dP_3 \dots dP_F \right) \right]$$

Now, there, in leaving co-ordinate.

$$= D \dot{q}_1 \cdot dt \cdot dq_2 \dots dq_F + \left( D \dot{p}_1 \cdot dt \cdot dP_2 \dots dP_F \right)$$

$$= \left( D \cdot \dot{q}_1 \cdot dt \cdot dq_2 \dots dP_1 \right) + \left( D \cdot \frac{\partial \dot{p}_1}{\partial p_1} \cdot dt \cdot dP_2 \dots dP_F \right) \delta t$$

There is leaving and entering state. so we have.

= enter - leave.

$$= D \cdot \frac{\partial \dot{q}_1}{\partial q_1} \cdot dt \cdot dq_2 \dots dq_F - D \frac{\partial \dot{p}_1}{\partial p_1} \cdot dt \cdot dP_2 \dots dP_F$$

$$= \left( D \cdot \frac{\partial \dot{q}_1}{\partial q_1} \cdot dt - D \cdot \frac{\partial \dot{p}_1}{\partial p_1} \cdot dt \right) \cdot dq_2 \cdot dq_3 \dots dq_F \cdot dP_1 \cdot dP_2 \dots dP_F$$

$$\left( \frac{dD}{dt} \right) dt = D \left( \frac{\partial \dot{q}_1}{\partial q_1} \cdot dt - \frac{\partial \dot{p}_1}{\partial p_1} \cdot dt \right) \cdot d\Gamma \cdot \delta t$$

$$\therefore \frac{dD}{dt} = D \left( \frac{\partial \dot{q}_1}{\partial q_1} \cdot dt \cdot dq_2 \dots dq_F \cdot \frac{\partial \dot{p}_1}{\partial p_1} \cdot dt \cdot dP_2 \dots dP_F \right)$$



by Hamiltonian's eq<sup>n</sup>.

$$\frac{\partial q_i}{\partial p_i} = \frac{\partial p_i}{\partial q_i}$$

$$\text{but, } \frac{\partial q_i}{\partial \dot{p}_i} - \frac{\partial p_i}{\partial \dot{q}_i} = 0.$$

Now, we know that:

$$D(p, q, t)$$

$$\therefore \left( \frac{\partial D}{\partial t} \right)_{p, q} + \left( \frac{\partial D}{\partial t} \right)_{p, t} + \left( \frac{\partial D}{\partial t} \right)_{q, t} = 0.$$

OB  $\therefore \frac{\partial D}{\partial t} = 0.$



Que. 3.

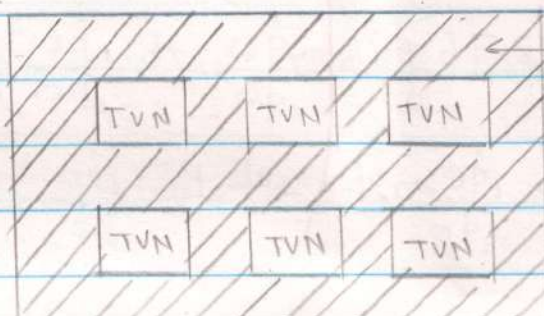
2. Ensemble →

Ensemble is a concept where, if there are system with ~~distigu~~ different contain ~~distiguisable~~ particle then the macro state is same but he got different microstates. For eg. we have system consist temperature, volume and no. of ~~part~~ molecules then we have same macro-state but different micro state cause of various nature of system compounts.

There are three types of Ensmemble.

- 1) Micro-canonical ensmemble.
- 2) Canonical ensmemble.
- 3) Grand Canonical ensmemble.

1) Micro-Canonical Ensmemble → In this system we consider a system having temperature, volume and no. of molecules. where we denote temperature as  $T$ , volume as  $V$  and no. of molecules with  $N$ . we distribute them int system ~~th~~ having 9 compartment. with walls where all compartment are separte with each other by rigid, impermeable and insulated wall where no. change in or transfer of any kind of things. this system we called as micro-canonical Ensmemble.



← Rigid, impermeable insulated walls.





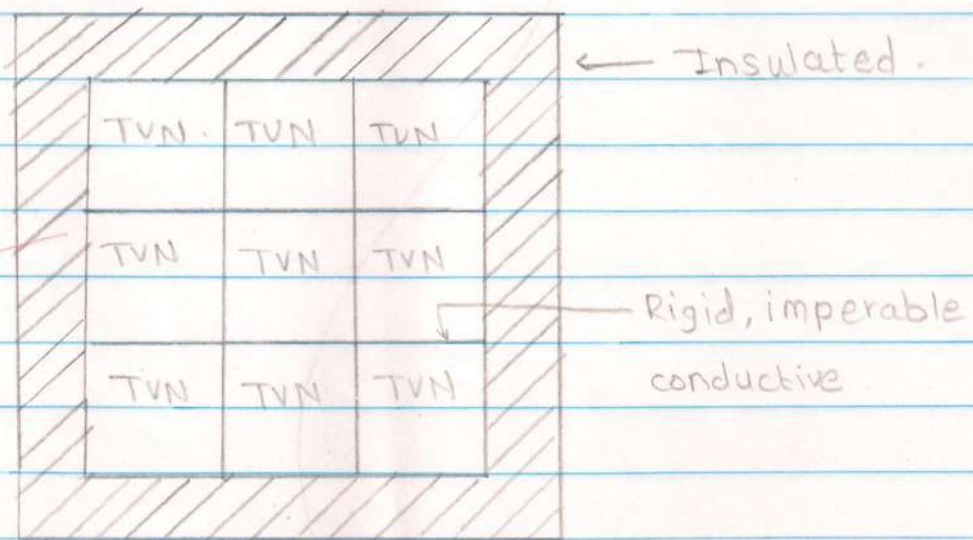
## Shri Swami Vivekanand Shikshan Sanstha's VIVEKANAND COLLEGE (Autonomous), KOLHAPUR

Class \_\_\_\_\_ Div \_\_\_\_\_ Roll No. \_\_\_\_\_

Suppliment No. \_\_\_\_\_ Subject \_\_\_\_\_

Test / Tutorial No. \_\_\_\_\_

2) Canonical Ensemble  $\rightarrow$  In this system we ~~g~~ again consider ~~th~~ a system having some kind of temperature, volume and no. of molecules. where we again denote them a temperature as  $T$ , volume as  $V$  and no of molecules with  $N$ . we distribut them in 9 compartment but now in canonical Ensemble there are walls ~~wt~~ which are rigid, imperamable but this time middel walls are conductive. which means teamparature is able to transfer this system know as Canonical Ensemble



3) Grand Canonical Ensemble  $\rightarrow$  In this system we consider system with a temperature, volume and No. of molecules. were, distance it separated by walls. this walls are rigid but permable and conductive.





# Shri Swami Vivekanand Shikshan Sanstha's VIVEKANAND COLLEGE (Autonomous), KOLHAPUR

Class MSC I Div \_\_\_\_\_ Roll No. 1335

Suppliment No. 1 Subject Statistical Mechanic

Test / Tutorial No. \_\_\_\_\_

Q1)

1)

→ microstates

2)

→ accessible microstates

3)

→  $\delta(\ln W) = 0$

4)

→ in equilibrium

5)

→ thermal equilibrium of the system.

→ the position of mechanical equilibrium does not change with

the position of the support of the system

→ the position of mechanical equilibrium does not change

with the position of the support of the system

→ the position of mechanical equilibrium does not change

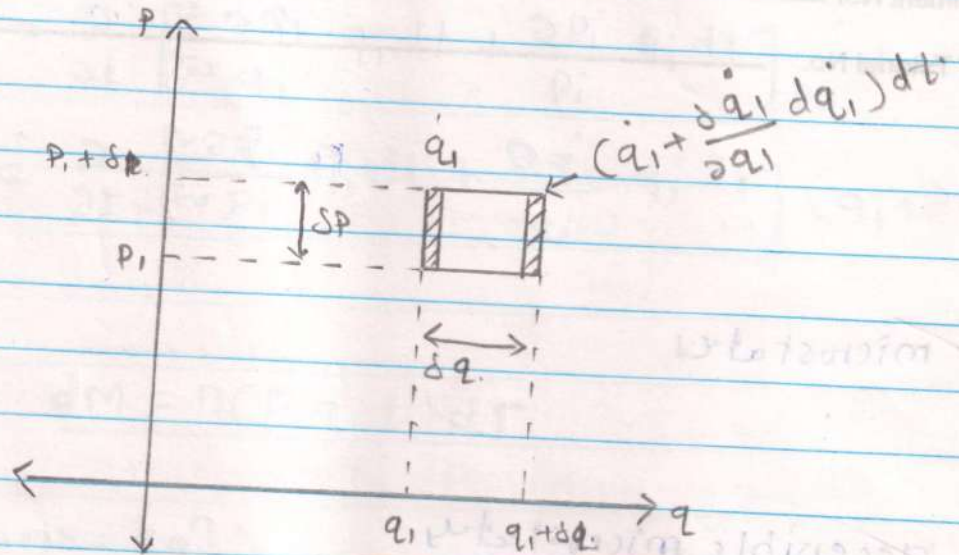
with the position of the support of the system



Q2.

↳

→ Liouville's Theorem in classical presentation.



$F \rightarrow$  degree of freedom

$p_1, p_2, \dots, p_f \rightarrow$  momentum.

$q_1, q_2, \dots, q_n \rightarrow$  position.

$$dM = p_1 p_2 p_3 \dots p_f$$

$$q_1 q_2 q_3 \dots q_f$$

$$dM = p_i q_i$$

Liouville's theorem:

Liouville's theorem said that the position of movement does not change with respect to time.

Density of phase movement does not change into time.

$$\frac{dD}{dt} \left[ \frac{\partial p_i}{\partial p_i} p_i + \frac{\partial q_i}{\partial q_i} q_i \right] dt$$

$$= \left[ \frac{\partial q_i}{\partial q_i} q_i + \frac{\partial p_i}{\partial p_i} p_i \right] dt (q_1, q_2, \dots, q_f)$$



Density Diff. Distribution.

$$D = D(p, q, t).$$

$$\frac{dD}{dt} = \left[ \frac{\partial D}{\partial p_i} \dot{p}_i + \frac{\partial D}{\partial q_i} \dot{q}_i \right] dt + (q_i, p_i, \dots, t)$$

$$\frac{dD}{dt} = \left( \frac{\partial D}{\partial p_i} \dot{p}_i dt \right) + \left( \frac{\partial D}{\partial q_i} \dot{q}_i dt \right) + (q_i, p_i, \dots, t)$$

$$\frac{dM}{dt} = \left[ \frac{\partial D}{\partial p_i} \dot{p}_i dt + \frac{\partial D}{\partial q_i} \dot{q}_i dt \right] - D \frac{\partial D}{\partial p_i} \dot{p}_i dt +$$

$$\frac{\partial D}{\partial q_i} \dot{q}_i dt.$$

Leaving point of phase is.

$$= \left[ \dot{q}_i + \frac{\partial \dot{q}_i}{\partial q_i} \dot{q}_i \right] dt + \left[ \frac{\partial q_i}{\partial q_i} q_i - \frac{\partial p_i}{\partial p_i} p_i \right]$$

$$= D \left[ \frac{dD}{\partial q_i} \dot{q}_i + \frac{d\dot{q}_i}{dq_i} q_i \right] + \left[ \frac{dD}{dp_i} \dot{p}_i + \frac{dp_i}{dp_i} p_i \right].$$

$$= [p_i, q_i, p_2, \dots, q_n, t]$$

Net phase point = enter - leaving.

$$\frac{dM}{dt} = \left( \frac{\partial D}{\partial p_i} \dot{p}_i dt + \frac{\partial D}{\partial q_i} \dot{q}_i dt \right) - \left[ \frac{\partial q_i}{\partial q_i} q_i dt + \frac{\partial p_i}{\partial p_i} p_i dt \right]$$

$$= \sum_{i=1}^n \left[ \frac{dD}{\partial q_i} \dot{q}_i + \frac{d\dot{q}_i}{dq_i} q_i \right] + \left[ \frac{dD}{dp_i} \dot{p}_i + \frac{dp_i}{dp_i} p_i \right].$$

$$= \sum_{i=1}^n \left[ \frac{\partial D}{\partial p_i} \dot{p}_i dt + \frac{\partial D}{\partial q_i} \dot{q}_i dt - \frac{\partial q_i}{\partial q_i} q_i dt + \right.$$

$$\left. \frac{\partial D}{\partial p_i} \dot{p}_i + \frac{dp_i}{dp_i} p_i \right].$$

$p_i$  the co-ordinate.

$$= (p_i + \delta p) \left( \frac{\partial D}{\partial p_i} \dot{p}_i dt \right).$$



rate change of no of phase point

$$\frac{\partial(dm)}{\partial t} dt = \frac{\partial}{\partial t} \left[ \frac{\partial D}{\partial t} D(p, q, t) \right]$$

$$= \frac{\partial}{\partial t} \left[ \sum_{i=1}^n \frac{\partial \Phi_i}{\partial q_i} q_i dt + \frac{\partial \dot{p}_i}{\partial p_i} p_i dt \right] p, q$$

$$= \frac{\partial}{\partial t} \left[ \sum_{i=1}^n \frac{\partial \Phi_i}{\partial p_i} p_i dt + \frac{\partial \dot{q}_i}{\partial q_i} q_i dt \right] (q_i + \Delta q)$$

$$dm = D(p, q, t) d\Gamma$$

Hamiltons eqn

$$\dot{p}_i = - \frac{\partial H}{\partial q_i} \quad \& \quad \dot{q}_i = \frac{\partial H}{\partial p_i}$$

$$\frac{\partial \dot{p}_i}{\partial p_i} = \frac{\partial \dot{q}_i}{\partial q_i} = \frac{\partial^2 H}{\partial p_i \partial q_i} + \frac{\partial^2 H}{\partial p_i \partial q_i}$$

$$\therefore \frac{\partial(dm)}{\partial t} = \frac{\partial}{\partial t} \left[ \frac{\partial \dot{p}_i}{\partial p_i} p_i dt + \frac{\partial \dot{q}_i}{\partial q_i} q_i dt \right] \quad \text{--- (A)}$$

$$dm = D(p, q, t) d\Gamma$$





# Shri Swami Vivekanand Shikshan Sanstha's VIVEKANAND COLLEGE (Autonomous), KOLHAPUR

Class Msc I Div \_\_\_\_\_ Roll No. 1335

Suppliment No. \_\_\_\_\_ Subject \_\_\_\_\_

Test / Tutorial No. 2

full dependance density  $D(P, Q, t)$

$$\frac{dD}{dt} = \frac{d}{dt} \left[ \frac{\partial p_i}{\partial p} p_i + \frac{\partial q_i}{\partial q} q_i \right] - \frac{\partial p_i}{\partial p} p_i + \frac{\partial q_i}{\partial q} q_i \quad \text{--- (B)}$$

than Adding eq<sup>n</sup> (A) + (B)

$$\boxed{\frac{dD}{dt} = 0}$$

The Liouville's theorem has the value's 0 becomes the density of phase space value remains zero. then the external perturbation can be affect in zero space phase

03



Q3

1) Macrostate :-

a, b, c, d are the 4 particle in  
microstate which probability  $1/2$   
the compoundwise distribution.

Cor No	Compound	arrangement of particle				
		I	II	III	IV	V
1	1	0	1	2	3	4
2	2	4	3	2	1	0

their are compoundwise distribution has  
5 arrangement particle

$(0, 4)$   $(1, 3)$   $(2, 2)$   $(3, 1)$   $(4, 0)$ .

each compositionwise distribution of particle  
is known as microstate.

In the general form is

$(1, n+1)$   $(2, n+2)$  ...  $(n, n+1)$

$\downarrow$  total number has  $(n, n-1)$

2) microstate

macrostate	Arrangement wise distribution		microstate
	I	II	
(0,4)	abcd	o	1
(1,3)	a	bcd	4
	b	acd	
	c	abd	
	d	abc	
(2,2)	ab	ed	6
	ac	bd	
	ad	cb	
	bc	ad	
	bd	ac	
	ba	ed	
(3,1)	abc	d	4
	abd	c	
	acd	b	
	bcd	a	
(4,0)	abcd	o	1

(0,4) has only one microstate.

(1,3) has 4 microstate

(2,2) has 6 microstate



Q3

1) Macrostate :-

a, b, c, d are the 4 particle in microstate which probability  $1/2$  the compositionwise distribution.

Cor No	Compoundy	arrangement of particle				
		I	II	III	IV	V
1	1	0	1	2	3	4
2	2	4	3	2	1	0

their are compoundwise distribution has 5 arrangement particle

$(0, 4) (1, 3) (2, 2), (3, 1) (4, 0)$ .

each compositionwise distribution of particle is known as microstate.

In the general form is

$(1, n+1) (2, n+2) \dots (n, n+1)$

$\therefore$  total number has  $(n, n-1)$

2) microstate

macrostate	Arrangement wise distribution		microstate
	I	II	
(0,4)	abcd	0	1
(1,3)	a	bcd	4
	b	acd	
	c	abd	
	d	abc	
(2,2)	ab	cd	6
	ac	bd	
	ad	cb	
	bc	ad	
	bd	ac	
	ba	dc	
(3,1)	abc	d	4
	abd	c	
	dcd	b	
	bcd	a	
(4,0)	abcd	0	1

(0,4) has only one microstate.

(1,3) has 4 microstate

(2,2) has 6 microstate



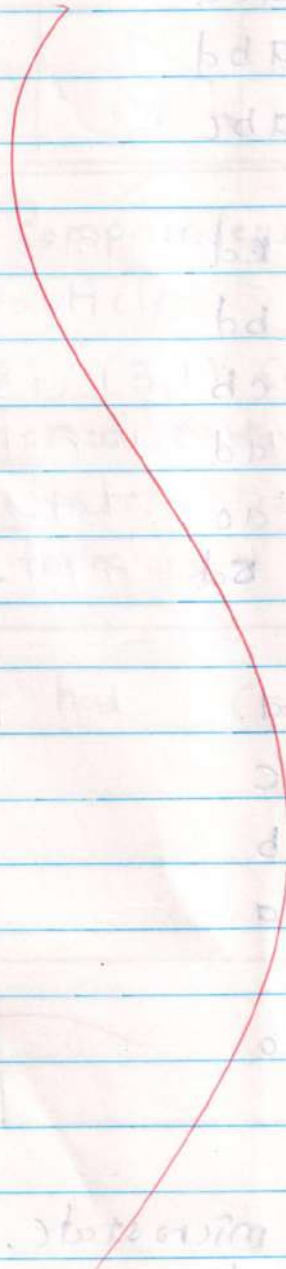
each particle compoundwise distribution of  
macrostate is known as microstate.

for example 16 microstates are

$$16 = 2^4$$

then  $2^n$

general form of microstate is  $2^n$





Shri Swami Vivekanand Shikshan Sanstha's  
**VIVEKANAND COLLEGE (Autonomous), KOLHAPUR**

Class M.Sc-I

Div. \_\_\_\_\_

Roll No. 1336

Suppliment No. \_\_\_\_\_

Subject physics

Test / Tutorial No. \_\_\_\_\_

M.Sc-I, Sem-II Internal Examination

Q1. 1. a. microstate

2. b. accessible microstate

3. c.  $\delta(\ln w) = 0$

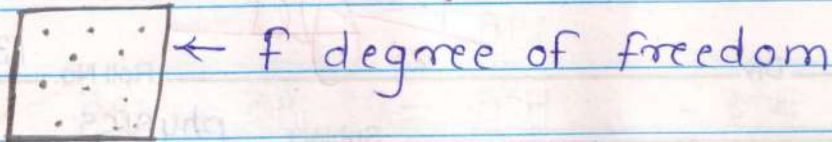
4. d. an excited

5. b. number of particles in the system

3



Q2. 1. Liouville's Theorem



Configuration of the system  
 position co-ordinate  $\Rightarrow \partial q_1, \partial q_2 \dots \partial q_f$   
 momentum co-ordinate  $\Rightarrow \partial p_1, \partial p_2 \dots \partial p_f$

$\therefore$  Consider the infinitesimal hyper-volume the no. of phase point density doesn't change with time

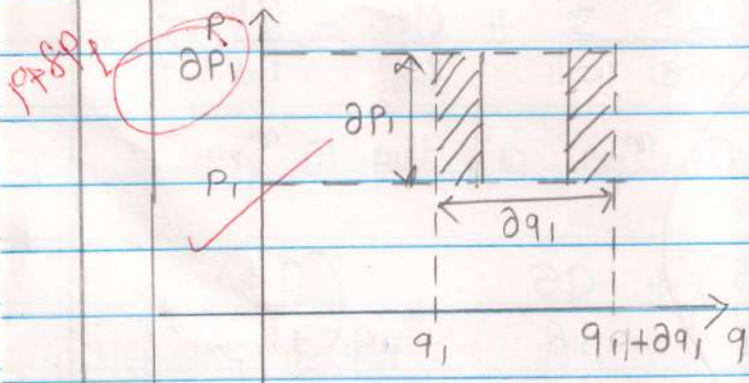
$$\frac{dD}{dt} = 0$$

The volume  $dT = \partial q_1, \partial q_2 \dots \partial q_f \partial p_1, \partial p_2 \dots \partial p_f$

$\therefore$  density distribution function is  $D = D(q, p, t)$

$\therefore$  No of phase points

$$dm = D(q, p, t) \partial q_1 \dots \partial q_f \partial p_1 \dots \partial p_f dT$$



the no. of phase point entering in the 1<sup>st</sup> face in time dt

$$\therefore D \partial q_1 \dots \partial q_f \partial p_1 \dots \partial p_f$$



Q2.

1. the no. of phase point leaving

$$\therefore D\dot{q}_1 dt \frac{\partial}{\partial q_1} \dots \frac{\partial}{\partial P_1} + \frac{\partial}{\partial q_1} (D\dot{q}_1 dt \frac{\partial}{\partial q_1} \dots \frac{\partial}{\partial P_1})$$

$$\therefore D\dot{q}_1 dt \frac{\partial}{\partial q_1} \dots \frac{\partial}{\partial P_1} + D \frac{\partial \dot{q}_1}{\partial q_1} dt + \frac{\partial D}{\partial q_1} \dot{q}_1 dt \frac{\partial}{\partial q_1} \dots \frac{\partial}{\partial P_1}$$

$\therefore$  the net no. of phase points entering  
= enter - leave

$$\therefore D\dot{q}_1 dt \frac{\partial}{\partial q_1} \dots \frac{\partial}{\partial P_1} - D\dot{q}_1 dt \frac{\partial}{\partial q_1} \dots \frac{\partial}{\partial P_1} - D \frac{\partial \dot{q}_1}{\partial q_1} dt + \frac{\partial D}{\partial q_1} \dot{q}_1$$

$$= - \left[ + D \frac{\partial \dot{q}_1}{\partial q_1} dt + \frac{\partial D}{\partial q_1} \dot{q}_1 \right] \delta q_1$$

$$= - \left( + D \frac{\partial \dot{q}_1}{\partial q_1} + \frac{\partial D}{\partial q_1} \dot{q}_1 \right) d\tau$$

for p-co-ordinate

$$= - \left[ D \frac{\partial \dot{p}_1}{\partial P_1} + \frac{\partial D}{\partial P_1} \dot{p}_1 \right] d\tau$$

$\therefore$  the total rate of change of no. of phase point in time dt

$$\therefore \frac{\partial}{\partial t} (dm) dt = - \left[ D \left( \frac{\partial \dot{q}_1}{\partial q_1} + \frac{\partial \dot{p}_1}{\partial P_1} \right) + \left( \frac{\partial D}{\partial q_1} \dot{q}_1 + \frac{\partial D}{\partial P_1} \dot{p}_1 \right) \right] dt$$



Q2 1. Acc. to Hamiltonian,

$$\dot{p}_i = -\frac{\partial H}{\partial q_i} \quad \dot{q}_i = \frac{\partial H}{\partial p_i}$$

$$\therefore \frac{\partial q_i}{\partial q_i} + \frac{\partial \dot{p}_i}{\partial p_i} = \frac{\partial^2 H}{\partial p_i \partial q_i} - \frac{\partial^2 H}{\partial p_i \partial q_i} = 0$$

Consider

$$\frac{\partial (dm)}{\partial t} = \left[ \sum_{i=1}^f \frac{\partial D}{\partial q_i} \dot{q}_i + \frac{\partial D}{\partial p_i} \dot{p}_i \right] dt dT$$

$$\therefore dD^{(part)} = (dm) dt dT$$

$$\therefore \frac{\partial D}{\partial t} dt dT = - \left[ \sum_{i=1}^f \frac{\partial D}{\partial q_i} \dot{q}_i + \frac{\partial D}{\partial p_i} \dot{p}_i \right] dt dT$$

$$\therefore \frac{\partial D}{\partial t} = - \sum_{i=1}^f \frac{\partial D}{\partial q_i} \dot{q}_i + \frac{\partial D}{\partial p_i} \dot{p}_i \quad \text{--- (1)}$$

\(\therefore\) The full of probability density is given by

$$\therefore \frac{dD}{dt} = \frac{\partial D}{\partial t} + \sum_{i=1}^f \frac{\partial D}{\partial q_i} \frac{\partial q_i}{\partial t} + \sum_{i=1}^f \frac{\partial D}{\partial p_i} \frac{\partial p_i}{\partial t} \quad \text{--- (2)}$$

eq<sup>n</sup> (1) put in eq<sup>n</sup> (2) we get

$$\therefore \left( \frac{dD}{dt} \right)_{pq} = \frac{\partial D}{\partial t} + \left( \frac{\partial D}{\partial q} \right)_{p,t} + \left( \frac{\partial D}{\partial p} \right)_{q,t}$$

$$\therefore \boxed{\frac{dD}{dt} = 0}$$

The Theorem states that the rate of change





**Shri Swami Vivekanand Shikshan Sanstha's  
VIVEKANAND COLLEGE (Autonomous), KOLHAPUR**

Class M.Sc-I Div. \_\_\_\_\_ Roll No. 1336

Suppliment No. 1 Subject physics

Test / Tutorial No. M.Sc-I, Sem-II Internal Examination

Q3. 2. Concept of ensemble with its types

Ensemble -

It is the collection of large number of macroscopically identical and essentially independent system.

macroscopically identical means it have same values of temperature, pressure, volume, number of particles.

microscopically differ in parity, symmetry and quantum states.

Types of ensemble

- i. Micro-canonical ensemble
- ii. Canonical ensemble
- iii. Grand-canonical ensemble

i. Micro-canonical ensemble -

It is the collection of large no. of essentially independent system having same Energy, volume, and no. of particle

In this ensemble the system is separated



Q3. 2.

Energy	Energy
Volume	Volume
no. of parti	no. of parti
Energy	Energy
Volume	Volume
no. of parti	no. of parti

outer walls rigid  
impermeable and insulating

ii Canonical ensemble -

It is the collection of large number of essentially independent system having same Temperature, Volume, No. of particle

In this ensemble the system is separated by rigid impermeable and conducting walls

Temperature	$T$
Volume	$V$
no of parti	$N$
$T$	$T$
$V$	$V$
$N$	$N$

outer walls rigid  
impermeable insulating

Inner walls rigid impermeable conducting

iii Grand-canonical ensemble

It is the collection of large number of essentially independent system having same Temperature, Volume and chemical potential

In this ensemble system is separated by the permeable and conducting walls.

Temperature	$T$
Volume	$V$

outer walls rigid



Q.3

→ 2) Ensembles can be defined as It is the collection of no. of macroscopically identical but essentially independent system.

Here the term macroscopically identical means constituent system of ensembles having same microscopic condition like pressure, volume, temperature, no. of particles etc. Here again the term essentially independent means constituent system of ensembles having different microscopic condition like quantum state etc.

There are 3 type of ensembles.

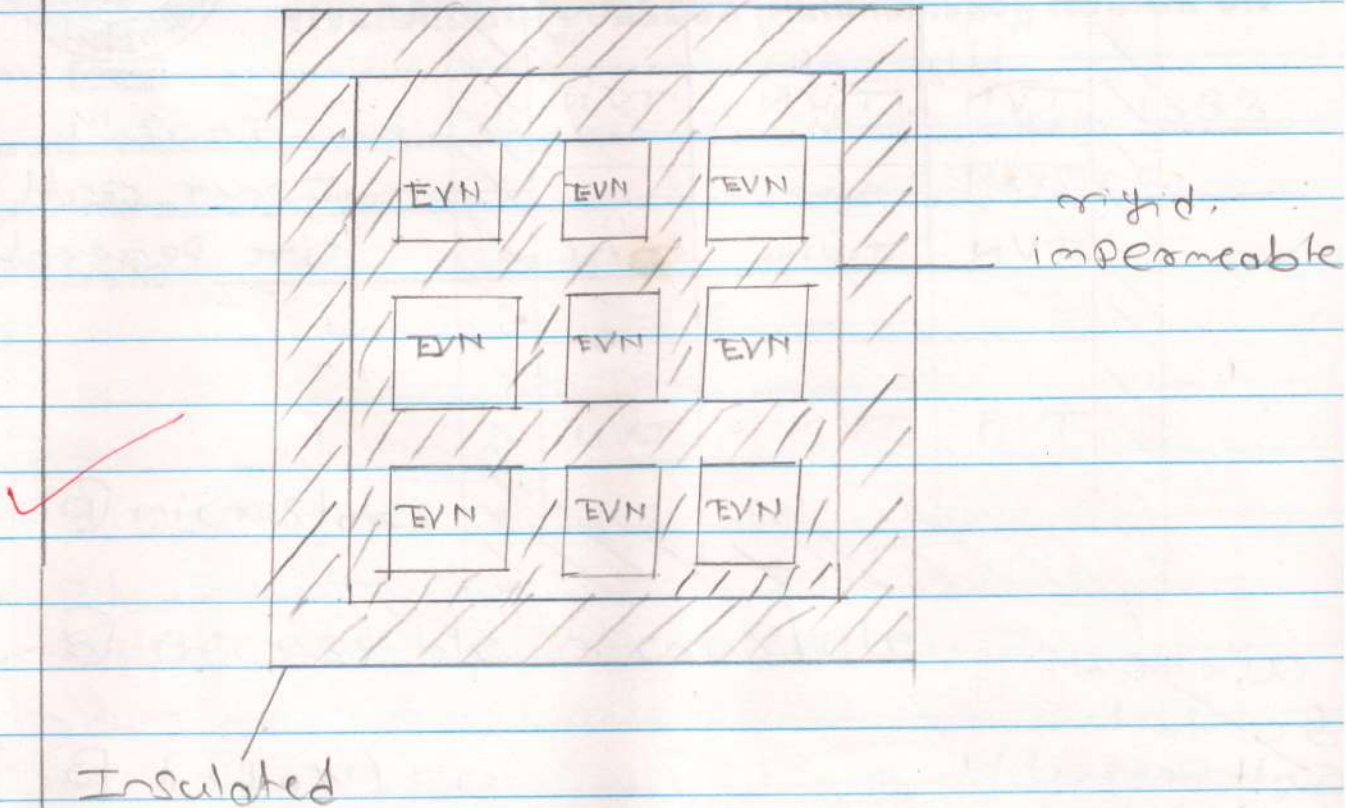
- 1) Microcanonical ensemble.
- 2) Canonical ensemble.
- 3) Grand canonical ensemble.

1) Microcanonical ensemble.

It is the large no. of microscopic condition but essentially independent system having same energy  $E$ , volume  $V$ , No of particle  $N$

Microcanonical ensemble are



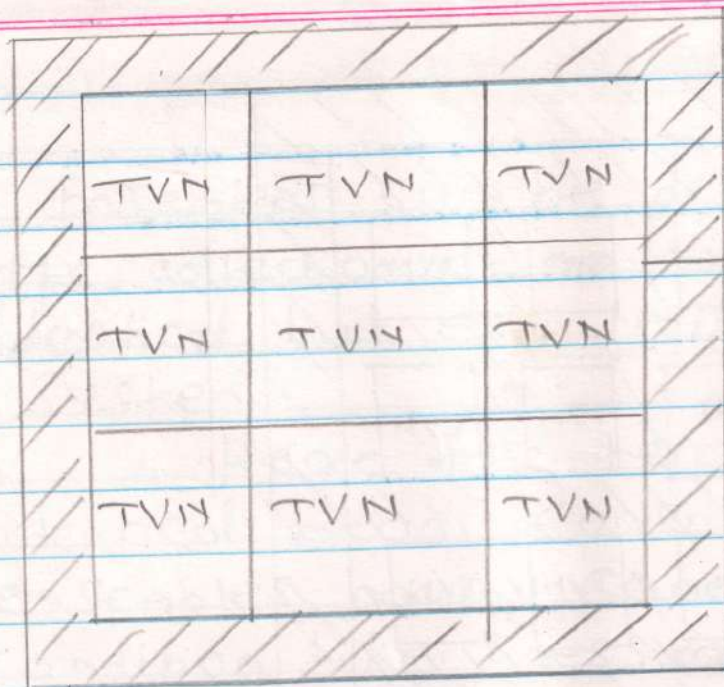


## 2) Canonical ensemble

It is the large no. of microscopical condition but essentially independent system having same ~~energy~~ temperature  $T$ , volume  $v$  & no of particle  $N$ .

Each canonical ensemble are separated by rigid, impermeable & perfectly insulated but conductive walls & outer wall are perfectly insulated.





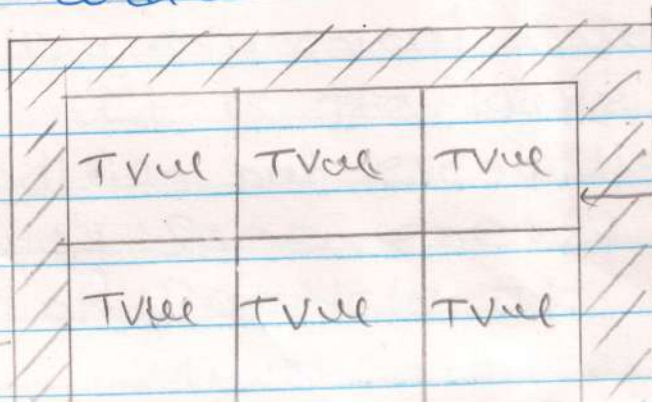
Inner wall are permeable.

Outer wall & conducting wall perfectly insulated.

### 3) Grand canonical system:

It is the large no. of microscopical condition but essentially independent system having same temperature  $T$ , volume  $v$  & chemical potential  $\mu$ .

Grand canonical ensembles are separated by rigid permeable & insulated walls.



Inner wall are permeable.

outer





Shri Swami Vivekanand Shikshan Sanstha's  
**VIVEKANAND COLLEGE (Autonomous), KOLHAPUR**

Class \_\_\_\_\_ Div \_\_\_\_\_ Roll No. 1333

Suppliment No. \_\_\_\_\_ Subject \_\_\_\_\_

Test / Tutorial No. \_\_\_\_\_

In this <sup>grand</sup> canonical system inner wall  
are rigid & permeable. but outer wall  
as-well as inner wall are insulated.

Canoni

Ensemble average:-

$$\bar{R} = \frac{\int_{-\infty}^{\infty} R(x) N(x) dx}{\int_{-\infty}^{\infty} N(x) dx}$$



Q.2

1) Liouville's Theorem.

Infinitesimal hyper volume no. of Phase Point density does not change with time

$$\frac{dD}{dt} = 0$$

where volume

$$dV = dq_1, dq_2, \dots, dq_f \quad dp_1, dp_2, \dots, dp_f$$
$$dT = dV \cdot D$$

density distribution function  $D = D(P, q, t)$

No of Phase Point  $dN = D(P, q, t)$

For instant phase space two dimensional the no. of Phase Point entering the phase space 1<sup>st</sup> face in time  $dt$ .

$$= D \frac{dq_1}{dt} dt \quad q_2 \dots dq_3 \dots dp_1 \dots dp_2 \dots dp_f$$

$$= D \, dq_1 dt \dots q_2 dt \dots dp_f$$

~~The no. of phase point~~

