

"Dissemination of Education for Knowledge, Science and Culture"  
-Shikshanmaharshi Dr. Bapuji Salunkhe  
Shri Swami Vivekanand Shikshan Sanstha, Kolhapur

**Vivekanand College, Kolhapur (Autonomous)**  
**Department of Physics**

**M.Sc. Part- I**  
**Electrodynamics**  
**Surprise Test**

Date : 23/04/2022  
Day: - Saturday

Total Marks: 20  
Time :- 2pm to 3pm

**Instructions:-**

- 1) All questions are compulsory.
- 2) Figures to the right indicate full marks.
- 3) Use of log table and calculator is allowed.

**Q. 1 ) Select most correct alternative.**

**(05)**

i) Displacement current is.....

- a) D                      b) J                      c)  $\partial D/\partial t$                       d)  $\partial J/\partial t$

ii ) The second Maxwell's equation is.....

- a)  $\nabla \cdot \vec{B} = 0$                       b)  $\nabla \cdot \vec{B} = \rho$                       c)  $\nabla \cdot \vec{B} = \sigma$                       d)  $\nabla \cdot \vec{B} = E$

iii ) Energy density in electric field is given as .....

- a)  $u_e = \frac{1}{2} \mu_0 H^2$                       b)  $u_e = \frac{1}{2} \epsilon_0 E^2$   
c)  $u_e = \frac{1}{2} \mu_0 H$                       d)  $u_e = \frac{1}{2} \mu_0 B^2$

iv ) The relation between magnetic flux density and vector potential is.....

- a)  $B = \text{Curl}(A)$                       b)  $A = \text{Curl}(B)$                       c)  $B = \text{Div}(A)$                       d)  $A = \text{Div}(B)$

v) Choose the correct alternative

- a)  $B = \mu H$  ;  $D = \epsilon E$                       b)  $D = \mu E$  ;  $B = \epsilon H$   
c)  $D = \mu H$  ;  $B = \epsilon E$                       d)  $B = \mu \epsilon H$  ;  $D = \mu \epsilon E$

**Q. 2 Write a short note on Lorentz Gauge.**

**(05)**

**Q. 3 Derive the relation for Poynting vector.**

**(10)**



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Vivekanand College, Kolhapur (Autonomous)

Department of Physics

M.Sc. Part- I

Electrodynamics

Surprise Test

Attendance Sheet

Date : 23/04/2022

Roll. No.	Name of Candidate	Sign
1601	Chougule Snehalda S.	Chougule
1603	Daryma Atmishet Ashok	Daryma
1604	Craikwad Aishwarya Sunkant	Craikwad
1605	Gaikwad Divya Ramesh	Divya
1606	Gawade Sayali Shantaram	Sawade
1608	Hirque Pravin Parakash	Hirque
1607	Nikhil Sandeep Jadhav	Jadhav
1609	Jarnade Wahida S.	Wahida
1611	Kakade Seema Vishnu	Kakade
1615	Kandekar Pooja Sanjay	Kandekar
1617	Khokhar Jaeej D	Khokhar
1618	Khot Priyanka Balaso	Khot
1623	Sammed Rajendra Jathe	Jathe
1627	Atarsha Bhimao Patil	Patil
1628	Prajay Jayasent Patil	Patil
1629	Patil Sanjayita Sanjay	Patil
1630	Patil Shrutika Jaysingh	Patil
1631	Rohan Raju Sonkamble	Rohan
1632	Sayyad Akshata J.	Sayyad

Teacher Incharge.....

(Mr. A.V. Shinde)



Head of the  
Department of Physics  
Vivekanand College, Kolhapur

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**Vivekanand College, Kolhapur (Autonomous)**  
**Department of Physics**

**M.Sc. Part- I**  
**Electrodynamics**  
**Surprise Test**  
**Result**

Date : 23/04/2022

Roll. No.	Marks	Roll. No.	Marks
1601	13	1625	-
1602	-	1626	-
1603	04	1627	05
1604	17	1628	06
1605	09	1629	10
1606	11	1630	11
1607	-	1631	11
1608	08	1632	09
1609	09		
1610	-		
1611	16		
1612	-		
1613	-		
1614	-		
1615	16		
1616	-		
1617	11		
1618	13		
1619	-		
1620	-		
1621	-		
1622	-		
1623	05		
1624	0-		

Teacher Incharge.....

*Shinde A V*  
(Mr. A.V. Shinde)

*M*  
Head of the  
Department of Physics  
Vivekanand College, Kolhapur



Shri Swami Vivekanand Shikshan Sanstha Kolhapur's

# VIVEKANAND COLLEGE, KOLHAPUR (AUTONOMOUS)

## SUPLIMENT

17/09

Signature  
of  
Supervisor

Suppliment No. :

Roll No. : 1604

Class : M.Sc. 1<sup>st</sup> [Sem II<sup>nd</sup>]

Subject : Electrodynamics

Test / Tutorial No. :

Div. :

10-1 Select correct alternatives.

1.) Displacement Current is denoted by -  
c.)  $\partial \vec{D} / \partial t$

2.) Second Maxwell's eq<sup>n</sup> is -  
b.)  $\nabla \cdot \vec{B} = 0$

3.) Energy density in electric field is given as  
d.)  $\frac{1}{2} \epsilon_0 E^2$

4.) The relation b/w mag. flux density - to vector Potential -

5.) Choose correct alternative -

c.)  $B = \mu H$

Write short note of on Lorentz's Gauge.

Lorentz's Gauge :- we know that, in electromagnetic field there are scalar and vector potential equation given by Maxwell's.

Scalar :- 
$$-\frac{\rho}{\epsilon} = \nabla^2 \phi + \frac{\partial}{\partial t} \left( \nabla \vec{A}' + \mu\epsilon \frac{\partial \phi}{\partial t} \right)$$

Vector :- 
$$-\mu\vec{J} = \nabla^2 \vec{A}' - \nabla \left( \nabla \vec{A}' + \mu\epsilon \frac{\partial \phi}{\partial t} \right)$$

Now,

from the Lorentz's condition -

$$\left[ \nabla \vec{A}' + \mu\epsilon \frac{\partial \phi}{\partial t} \right] = 0$$

hence, eqn (1) becomes,

$$-\frac{\rho}{\epsilon} = \nabla^2 \phi - \mu\epsilon \frac{\partial^2 \phi}{\partial t^2}$$

$$-\mu\vec{J} = \nabla^2 \vec{A}' - \mu\epsilon \frac{\partial^2 \vec{A}'}{\partial t^2}$$

further simplifying -

$$-\frac{\rho}{\epsilon} = \left[ \nabla^2 - \mu\epsilon \frac{\partial^2}{\partial t^2} \right] \phi$$

$$-\mu\vec{J} = \left[ \nabla^2 - \mu\epsilon \frac{\partial^2}{\partial t^2} \right] \vec{A}'$$

from the Phase velocity of electromagnetic field,

$$v = \frac{1}{\sqrt{\mu\epsilon}}$$

$$\Rightarrow \mu\epsilon = \frac{1}{v^2}$$

putting the value of  $\mu\epsilon$  in the above eqn -

$$\left. \begin{aligned} -\frac{\rho}{\epsilon} &= \left[ \nabla^2 - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right] \phi \\ -\mu J &= \left[ \nabla^2 - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right] \vec{A} \end{aligned} \right\} \text{--- (4)}$$

Here, we are consider -

$$\left[ \nabla^2 - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right] = \square^2 - \text{D'Alembertian operator.}$$

$$= \left[ \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right]$$

Now from eqn (4) becomes as -

$$\left. \begin{aligned} -\frac{\rho}{\epsilon} &= \square^2 \phi \\ -\mu J &= \square^2 \vec{A} \end{aligned} \right\} \text{--- (5)}$$

So, above equation shows coupled differential equation of vector potential  $\vec{A}$  & scalar  $\phi$ . Now we are introducing new scalar  $\lambda$ .

Here,

$$\begin{aligned} \vec{A}' &= \vec{A} + \Delta d \Rightarrow \vec{A} = \vec{A}' - \Delta d \\ \phi' &= \phi - \frac{\partial d}{\partial t} \Rightarrow \phi = \phi' + \frac{\partial d}{\partial t} \end{aligned}$$

from the Lorentz's condition -

$$\left[ \nabla \cdot \vec{A}' + \mu \epsilon \frac{\partial \phi}{\partial t} \right] = 0 \text{ --- [from old Lorentz's condition]}$$

Now putting the values of  $\vec{A}$  &  $\phi$

$$\left[ \nabla \cdot \vec{A}' + \mu \epsilon \frac{\partial \phi}{\partial t} \right] = 0$$

$$\left[ \nabla \cdot (\vec{A}' - \Delta d) + \mu \epsilon \frac{\partial}{\partial t} \left( \phi' + \frac{\partial d}{\partial t} \right) \right] = 0$$

$$\nabla \cdot \vec{A}' - \nabla^2 d + \mu \epsilon \frac{\partial \phi'}{\partial t} + \mu \epsilon \frac{\partial^2 d}{\partial t^2} = 0$$

$$\nabla \vec{A}' + \mu \epsilon \frac{\partial \phi'}{\partial t} = \nabla^2 d - \mu \epsilon \frac{\partial d}{\partial t}$$

$$\nabla \vec{A}' + \mu \epsilon \frac{\partial \phi'}{\partial t} = \left( \nabla^2 - \mu \epsilon \frac{\partial}{\partial t} \right) d \quad \text{--- (6)}$$

Phase velocity, we know it.

$$v = \frac{c}{\sqrt{\mu \epsilon}} \Rightarrow \mu \epsilon = \frac{1}{v^2}$$

from eqn (6)

$$\nabla \vec{A}' + \mu \epsilon \frac{\partial \phi'}{\partial t} = \left[ \nabla^2 - \frac{1}{v^2} \frac{\partial}{\partial t} \right] d \quad \text{--- (7)}$$

Hence,

$$\left[ \nabla^2 - \frac{1}{v^2} \frac{\partial}{\partial t} \right] = \square^2$$

Now eqn (7) is becomes,

$$\nabla \vec{A}' + \mu \epsilon \frac{\partial \phi'}{\partial t} = \square^2 d$$

from the Lorenz's condition

$$\square^2 d = 0$$

∴ In the electromagnetic field new vector potential  $\vec{A}'$  and scalar  $\phi'$  are and transformation of  $\vec{A} \rightarrow \vec{A}'$  and  $\phi \rightarrow \phi'$  shows Lorenz's gauge transformation.

Shri Swami Vivekanand Shikshan Sanstha Kolhapur's

# VIVEKANAND COLLEGE, KOLHAPUR (AUTONOMOUS)

## SUPPLIMENT

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of  
Supervisor

Suppliment No. :

Roll No. : 1611

Class : MSc - J (physics)

Subject : Electrodynamics

Test / Tutorial No. :

Div. :

1) a)  $\vec{D}$

2) b)  $\nabla \cdot \vec{B} = 0$

3) b)  $\frac{1}{2} \epsilon_0 E^2$

4) a)  $\nabla \times \vec{B} = \nabla \times \vec{A}$

5) c)  $B = \mu H$



Q.2 Poynting Vector

the work done is defined as

$$dW = \vec{F} \cdot d\vec{l} \quad \dots \textcircled{1}$$

where  $\vec{F}$  is Lorentz force acting on charge  $q$

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$

and  $d\vec{l}$  is small displacement

$$\vec{v} = \frac{d\vec{l}}{dt}$$

$$\therefore d\vec{l} = \vec{v} \cdot dt$$

eq<sup>n</sup> ① becomes

$$dW = q(\vec{E} + \vec{v} \times \vec{B}) \cdot \vec{v} \cdot dt$$

$$= q(\vec{E} \cdot \vec{v}) dt + q(\vec{v} \times \vec{v} \cdot \vec{B}) dt$$

$$dW = q(\vec{E} \cdot \vec{v}) dt$$

$$\frac{dW}{dt} = q(\vec{E} \cdot \vec{v}) \quad \dots \textcircled{2}$$

we know that charge  $q$  is defined as,

$$q = \int \rho \cdot dV \quad \rho = \frac{dq}{dV}$$

eq<sup>n</sup> ② becomes

$$\frac{dW}{dt} = \int \rho (\vec{E} \cdot \vec{v}) dV$$

$$dq = \rho dV$$

$$q = \int \rho dV$$

but current density  $\vec{J} = \rho \cdot \vec{v}$

$$\frac{dW}{dt} = \int \vec{J} \cdot \vec{E} \cdot dV$$

$$\frac{dW}{dt} = \int \vec{E} \cdot \vec{J} \cdot dV \quad \dots \textcircled{3}$$

above eq<sup>n</sup> ③ shows that, the total work done per unit time is dot product of integration of electric field  $\vec{E}$  & current density  $\vec{J}$  over the volume  $v$ .

we know that Maxwells four eq<sup>ns</sup> are

$$i) \nabla \cdot \vec{E} / \nabla \cdot \vec{D} = 0$$

$$ii) \nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$iii) \nabla \cdot \vec{B} = 0$$

$$iv) \nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

Maxwells fourth eq<sup>ns</sup> is

$$\nabla \times \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$\therefore \vec{J} = \nabla \times \vec{H} - \frac{\partial \vec{D}}{\partial t}$$

premultiplying by  $\vec{E}$  we get

$$\vec{E} \cdot \vec{J} = \vec{E} (\nabla \times \vec{H}) - \vec{E} \cdot \frac{\partial \vec{D}}{\partial t} \quad \text{--- (4)}$$

$$\therefore \nabla (\vec{E} \times \vec{H}) = \vec{H} (\nabla \times \vec{E}) - \vec{E} (\nabla \times \vec{H})$$

$$\therefore \vec{E} (\nabla \times \vec{H}) = \vec{H} (\nabla \times \vec{E}) - \nabla (\vec{E} \times \vec{H})$$

$$\therefore \vec{E} (\nabla \times \vec{H}) = -\vec{H} \frac{\partial \vec{B}}{\partial t} - \nabla (\vec{E} \times \vec{H})$$

eq<sup>n</sup> (4) becomes

$$\vec{E} \cdot \vec{J} = -\vec{H} \frac{\partial \vec{B}}{\partial t} - \vec{E} \cdot \frac{\partial \vec{D}}{\partial t} - \nabla (\vec{E} \times \vec{H}) \quad \text{--- (5)}$$

Here we take partial derivatives of

$$\frac{\partial (\vec{H} \cdot \vec{B})}{\partial t} = \vec{H} \cdot \frac{\partial \vec{B}}{\partial t} + \vec{B} \cdot \frac{\partial \vec{H}}{\partial t}$$

$$\therefore \text{allo } \vec{H} \frac{\partial \vec{H}}{\partial t} + \text{allo } \vec{H} \frac{\partial \vec{H}}{\partial t} = 0 \text{ where}$$

$$\frac{\partial (\vec{H} \cdot \vec{B})}{\partial t} = -2 \text{allo } \vec{H} \frac{\partial \vec{H}}{\partial t}$$

$$\mu_0 \vec{H} \cdot \frac{\partial \vec{H}}{\partial t} = \frac{1}{2} \frac{\partial (\vec{B} \cdot \vec{H})}{\partial t}$$

$$\frac{\mu_0}{\epsilon_0} \vec{H} \cdot \frac{\partial \vec{B}}{\partial t} = \frac{1}{2} \frac{\partial (\vec{B} \cdot \vec{H})}{\partial t}$$

$$\vec{H} \cdot \frac{\partial \vec{B}}{\partial t} = \frac{\partial}{\partial t} \left( \frac{1}{2} \mu_0 H^2 \right)$$

$$\vec{H} \cdot \frac{\partial \vec{B}}{\partial t} = \frac{1}{\mu_0} \text{Um} \Rightarrow \text{Magnetic field in } \dots \text{ (6)}$$

where  $\text{Um} = \frac{\partial}{\partial t} \left( \frac{1}{2} \mu_0 H^2 \right)$

$$\therefore \frac{\partial (\vec{E} \cdot \vec{D})}{\partial t} = \vec{E} \cdot \frac{\partial \vec{D}}{\partial t} + \vec{D} \cdot \frac{\partial \vec{E}}{\partial t}$$

$$= \epsilon_0 \vec{E} \cdot \frac{\partial \vec{E}}{\partial t} + \epsilon_0 \vec{E} \cdot \frac{\partial \vec{E}}{\partial t}$$

$$\frac{\partial (\vec{E} \cdot \vec{D})}{\partial t} = 2 \epsilon_0 \vec{E} \cdot \frac{\partial \vec{E}}{\partial t}$$

$$\therefore \frac{\epsilon_0}{\epsilon_0} \vec{E} \cdot \frac{\partial \vec{D}}{\partial t} = \frac{1}{2} \frac{\partial (\vec{E} \cdot \epsilon_0 \vec{E})}{\partial t}$$

$$\vec{E} \cdot \frac{\partial \vec{D}}{\partial t} = \frac{\partial}{\partial t} \left( \frac{1}{2} \epsilon_0 E^2 \right)$$

$$\vec{E} \cdot \frac{\partial \vec{D}}{\partial t} = \text{Ue} \dots \dots \dots \text{(7)}$$

current density in  
= electric field in

where  $\text{Ue} = \frac{\partial}{\partial t} \left( \frac{1}{2} \epsilon_0 E^2 \right)$

So eqn (6) becomes

$$\vec{E} \cdot \vec{J} = - \frac{\partial (\text{Um})}{\partial t} - \frac{\partial (\text{Ue})}{\partial t} - \nabla (\vec{E} \times \vec{H})$$

Shri Swami Vivekanand Shikshan Sanstha Kolhapur's

**VIVEKANAND COLLEGE, KOLHAPUR (AUTONOMOUS)****SUPPLIMENT**Signature  
of  
Supervisor

Suppliment No. :

Roll No. : 1601

Class : Msc I

Subject : Electrodynamics

Test / Tutorial No. :

Div. :

1) Relation for Poynting Vector:

Let us consider  $q$  charges moving in electromagnetic field with electric field  $\vec{E}$  and magnetic field  $\vec{B}$  with velocity  $\vec{v}$ . Total work done by  $q$  charges in electromagnetic field is given by

$$dW = \vec{F} \cdot d\vec{l}$$

where  $\vec{F}$  = Lorentz force acting on  $q$  charge in electromagnetic field.

$d\vec{l}$  = Small displacement of  $q$  charge.

$$\text{We know } \vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$

$$d\vec{l} = \vec{v} dt$$

$$\therefore \vec{v} = \frac{d\vec{l}}{dt}$$

Total work done by  $q$  charge in electromagnetic field can be written as:

$$dW = q(\vec{E} \times \vec{v})$$

$$dW = q(\vec{E} + \vec{v} \times \vec{B}) \cdot \vec{v} dt$$

$$= q(\vec{E} \cdot \vec{v}) dt + q(\vec{v} \times \vec{B} \cdot \vec{v}) dt$$

$$= q(\vec{E} \cdot \vec{v}) dt + q(\vec{v} \cdot \vec{v} \times \vec{B}) dt$$

$$dW = q(\vec{E} \cdot \vec{v}) dt + 0$$

$$\frac{dW}{dt} = q(\vec{E} \cdot \vec{v}) \quad \text{--- (1)}$$

We know that volume density of electric charge is  $\rho$  and electromagnetic field is  $\vec{E}$ .

$$\rho = \frac{dq}{dv}$$

Total work done by volume density is

$$q = \int \rho dv$$

Above eq<sup>n</sup> becomes

$$\frac{dW}{dt} = \int \rho (\vec{E} \cdot \vec{v}) dv$$

Let  $\vec{J}$  be the velocity of volume density of electromagnetic field.

$$\vec{J} = \rho \vec{v}$$

$$\frac{dw}{dt} = \int (\mathbf{E} \cdot \mathbf{J}) dv \quad \text{--- (2)}$$

By maxwell's fourth equation

$$\nabla \times \vec{H} = \vec{J} + \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

$$\vec{J} = \nabla \times \vec{H} - \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

Pre-multiplying by  $\vec{E}$

$$\vec{E} \cdot \vec{J} = \vec{E} (\nabla \times \vec{H}) - \epsilon_0 \frac{\partial \vec{E} \cdot \vec{E}}{\partial t} \quad D = \epsilon_0 E$$

$$\vec{E} \cdot \vec{J} = \vec{E} (\nabla \times \vec{H}) - \epsilon_0 \frac{\partial \vec{E} \cdot \vec{E}}{\partial t} \quad \text{--- (3)}$$

From above eq<sup>n</sup> - eq<sup>n</sup> (3) become

$$\vec{E} \cdot \vec{J} = -\vec{H} \cdot \frac{\partial \vec{B}}{\partial t} - \epsilon_0 \frac{\partial \vec{E} \cdot \vec{E}}{\partial t} - \nabla \cdot (\vec{E} \times \vec{H}) \quad \text{--- (4)}$$

$$\text{Let } \frac{\partial (\vec{B} \cdot \vec{H})}{\partial t} = \vec{B} \cdot \frac{\partial \vec{H}}{\partial t} + \vec{H} \cdot \frac{\partial \vec{B}}{\partial t} \quad \vec{B} = \mu_0 \vec{H}$$

$$= \mu_0 \vec{H} \cdot \frac{\partial \vec{H}}{\partial t} + \mu_0 \vec{H} \cdot \frac{\partial \vec{H}}{\partial t}$$

$$\frac{\partial (\vec{B} \cdot \vec{H})}{\partial t} = 2 \mu_0 \vec{H} \cdot \frac{\partial \vec{H}}{\partial t} \quad \vec{H} = \frac{\vec{B}}{\mu_0}$$

$$= 2 \frac{\mu_0}{\mu_0} \vec{H} \cdot \frac{\partial \vec{B}}{\partial t}$$

$$\frac{\partial (\vec{B} \cdot \vec{H})}{\partial t} = 2 \vec{H} \cdot \frac{\partial \vec{B}}{\partial t}$$

$$B = \mu_0 \vec{H}$$

$$\vec{H} \cdot \frac{\partial \vec{B}}{\partial t} = \frac{1}{2} \frac{\partial (\vec{B} \cdot \vec{H})}{\partial t}$$

$$= \frac{1}{2} \mu_0 \frac{\partial \vec{H}^2}{\partial t}$$

$$= \frac{\partial}{\partial t} \left( \frac{1}{2} \mu_0 \vec{H}^2 \right)$$

$$\vec{H} \cdot \frac{\partial \vec{B}}{\partial t} = \frac{\partial}{\partial t} (\mu_0 m) \quad \text{--- (5)}$$

$\therefore \frac{1}{2} \mu_0 \vec{H}^2 = \mu_0 m$  Energy density of a charge in electromagnetic field.

We know,  $\frac{\partial (\vec{E} \cdot \vec{D})}{\partial t} = \vec{E} \cdot \frac{\partial \vec{D}}{\partial t} + \vec{D} \cdot \frac{\partial \vec{E}}{\partial t}$   $\vec{D} = \epsilon_0 \vec{E}$

$$= \vec{E} \epsilon_0 \frac{\partial \vec{E}}{\partial t} + \epsilon_0 \vec{E} \frac{\partial \vec{E}}{\partial t}$$

$$\frac{\partial (\vec{E} \cdot \vec{D})}{\partial t} = 2 \vec{E} \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

$$= 2 \vec{E} \frac{\epsilon_0}{\epsilon_0} \frac{\partial \vec{D}}{\partial t}$$

$$\frac{\partial (\vec{E} \cdot \vec{D})}{\partial t} = 2 \vec{E} \frac{\partial \vec{D}}{\partial t}$$

Shri Swami Vivekanand Shikshan Sanstha Kolhapur's

# VIVEKANAND COLLEGE, KOLHAPUR (AUTONOMOUS)

## SUPPLIMENT

Signature  
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Supervisor

Suppliment No. :

Roll No. : 1610

Class : M.Sc J

Subject : Electrodynamics.

Test / Tutorial No. :

Div. :

9/20

### 3. Lorentz Gauge

→ We know that scalar & vector potential is given by coupled differential.

$$\left. \begin{aligned} \frac{\rho}{\epsilon} &= \nabla^2 \phi - \frac{\partial^2 \phi}{\partial t^2} + \mu\epsilon \frac{\partial^2 \phi}{\partial t^2} \\ \mu\mathbf{J} &= \nabla^2 \vec{A} - \nabla \left( \nabla \cdot \vec{A} - \frac{\partial \phi}{\partial t} \right) + \mu\epsilon \frac{\partial^2 \vec{A}}{\partial t^2} \end{aligned} \right\} \text{--- (1)}$$

### Lorentz condition

$$\nabla^2 \vec{A} = -\mu\epsilon \frac{\partial^2 \vec{A}}{\partial t^2}$$

Hence eqn (1) becomes.

$$\left. \begin{aligned} \frac{\rho}{\epsilon} &= \nabla^2 \phi + \mu\epsilon \frac{\partial^2 \phi}{\partial t^2} \\ \mu\mathbf{J} &= \nabla^2 \vec{A} + \mu\epsilon \frac{\partial^2 \vec{A}}{\partial t^2} \end{aligned} \right\} \text{--- (2)}$$

We know that scalar the velocity of em wave is given

$$v = \frac{1}{\sqrt{\mu\epsilon}} = \frac{1}{\sqrt{2}}$$



$$\left. \begin{aligned} \frac{\rho}{\epsilon} &= \nabla^2 \phi - \frac{1}{v^2} \frac{\partial^2 \phi}{\partial t^2} \\ \mu \vec{J} &= \nabla^2 \vec{A} - \frac{1}{v^2} \frac{\partial^2 \vec{A}}{\partial t^2} \end{aligned} \right\} \text{--- (3)}$$

$$\left. \begin{aligned} \frac{\rho}{\epsilon} &= \left[ \nabla^2 \phi - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right] \phi \\ \mu \vec{J} &= \left[ \nabla^2 \vec{A} - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right] \vec{A} \end{aligned} \right\} \text{--- (4)}$$

$$\frac{\rho}{\epsilon} = \nabla^2 \vec{A} - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} = \square^2 \text{ (D'Alembert's operator)}$$

$$\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} - \frac{1}{v^2} \frac{\partial^2}{\partial t^2}$$

$$\left. \begin{aligned} \frac{\rho}{\epsilon} &= \square^2 \phi \\ \mu \vec{J} &= \square^2 \vec{A} \end{aligned} \right\} \text{--- (5)}$$

eqn (5) known as coupled differential eqn for scalar & vector potential by applying Lorentz condition. Now we will introduce scalar  $\lambda$  such that.

~~$\frac{\partial^2 \mu \epsilon \phi^2}{\partial t^2} = 0$  old Lorentz condition,~~

$$\vec{\nabla} \cdot \vec{A} + \nabla \lambda = 0$$

$$\vec{\nabla} \cdot \vec{A} - \frac{\partial \lambda}{\partial t} = 0$$

~~$\frac{\partial^2 \mu \epsilon \phi^2}{\partial t^2} = 0$  old Lorentz condition.~~

$$\vec{A}' = \frac{1}{c} \nabla \left( \frac{\partial \phi}{\partial t} - \frac{1}{v^2} \frac{\partial \phi}{\partial t} \right) + \frac{1}{c} \frac{\partial \vec{A}}{\partial t}$$

Now we know that velocity of em wave is give by

$$\frac{1}{\sqrt{\mu\epsilon}} = \frac{1}{v}$$

$$\vec{A}' = \left[ \nabla^2 - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right] \vec{A}$$

$$\frac{\partial \vec{A}'}{\partial t} + \mu\epsilon \frac{\partial \vec{A}}{\partial t} = \left[ \nabla^2 - \frac{1}{v^2} \frac{\partial^2}{\partial t^2} \right] \vec{A}$$

$$\frac{\partial^2 \vec{A}'}{\partial t^2} + \mu\epsilon \frac{\partial \vec{A}}{\partial t} = \frac{\partial^2 \vec{A}}{\partial t^2}$$

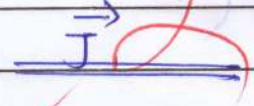
$$0 = \nabla^2 \phi$$

$$\frac{\partial \vec{A}}{\partial t} + \mu\epsilon \frac{\partial \vec{A}}{\partial t} = 0$$

The Lorentz condition term of scalar & vector potential  $\vec{A} \rightarrow \vec{A}'$  & satisfy scalar & vector potential  $\phi \rightarrow \phi'$ .

Q1

1) Displacement current is denoted by



2) Third Maxwell's eqn is  $\nabla \cdot \vec{B} = 0$

3) Energy density in electric field is given as

$$\frac{1}{2} \epsilon_0 E^2$$

4) The Relation between magnetic flux density & vector potential is  $\vec{B} = \nabla \times \vec{A}$

5) choose correct alternative

$$\beta = \frac{H}{u}$$